

# Quadratic Equations

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## Practice Set 2.1

Q. 1. Write any two quadratic equations.

Answer :

$$y^2 + y + 8 = 0 \text{ and } m^2 + 9 = 0$$

Q. 2. Decide which of the following are quadratic equations.

(1)  $x^2 + 5x - 2 = 0$

(2)  $y^2 = 5y - 10$

(3)  $y^2 + \frac{1}{y} = 2$

(4)  $x + \frac{1}{x} = -2$

(5)  $(m + 2)(m - 5) = 0$

(6)  $m^3 + 3m^2 - 2 = 3m^3$

Answer :

1.  $x^2 + 5x - 2 = 0$  is a quadratic equation because it is the form of  $ax^2 + bx + c = 0$  and it has degree 2.

2.  $y^2 = 5y - 10$

$y^2 - 5y + 10 = 0 \therefore$  it is a quadratic equation because it is the form of  $ax^2 + bx + c = 0$  and it has degree 2.

3.  $y^2 + \frac{1}{y} = 2$

$$\Rightarrow y^3 + 1 = 2y \Rightarrow y^3 - 2y + 1$$

$\therefore$  it is not a quadratic equation because it is not in the form of  $ax^2 + bx + c = 0$  and it does not have degree 2.

$$4. x + \frac{1}{x} = -2$$

$$x^2 + 1 = -2x \Rightarrow x^2 + 2x + 1 = 0$$

$\therefore$  it is a quadratic equation because it is the form of  $ax^2 + bx + c = 0$  and it has degree 2.

$$5. (m + 2)(m - 5) = 0$$

$$\Rightarrow m(m - 5) + 2(m - 5) \Rightarrow m^2 - 5m + 2m - 10 \Rightarrow m^2 - 3m - 10 = 0$$

$\therefore$  it is a quadratic equation because it is the form of  $ax^2 + bx + c = 0$  and it has degree 2.

$$6. m^3 + 3m^2 - 2 = 3m^3$$

$$\Rightarrow m^3 + 3m^2 - 2 - 3m^3 = 0 \Rightarrow -2m^3 + 3m^2 - 2 = 0$$

$\therefore$  it is not a quadratic equation because it is not in the form of  $ax^2 + bx + c = 0$  and it does not have degree 2.

**Q. 3. Write the following equations in the form  $ax^2 + bx + c = 0$ , then write the values of a, b, c for each equation.**

(1)  $2y = 10 - y^2$

(2)  $(x-1)^2 = 2x + 3$

$$(3) x^2 + 5x = -(3-x)$$

$$(4) 3m^2 = 2m^2 - 9$$

$$(5) P(3 + 6p) = -5$$

$$(6) x^2 - 9 = 13$$

**Answer :**

$$(1) 2y = 10 - y^2$$

$$\Rightarrow 2y + y^2 - 10 = 0$$

$$y^2 + 2y - 10 = 0;$$

$$a = 1, b = 2, c = -10$$

$$(2) (x - 1)^2 = 2x + 3$$

$$\Rightarrow x^2 - 2x + 1 = 2x + 3$$

$$\Rightarrow x^2 - 2x - 2x + 1 - 3 = 0$$

$$\Rightarrow x^2 - 4x - 2 = 0;$$

$$(3) x^2 + 5x = -(3 - x) \Rightarrow x^2 + 5x = -3 + x$$

$$\Rightarrow x^2 + 5x - x + 3 = 0$$

$$\Rightarrow x^2 + 4x + 3 = 0;$$

$$a = 1, b = 4, c = 3$$

$$(4) 3m^2 = 2m^2 - 9 \Rightarrow 3m^2 - 2m^2 + 9 = 0$$

$$m^2 + 0m + 9 = 0$$

$$a = 1, b = 0, c = 9$$

$$(5) p(3 + 6p) = -5 \Rightarrow 3p + 6p^2 + 5 = 0$$

$$6p^2 + 3p + 5 = 0;$$

$$a = 6, b = 3, c = 5$$

$$(6) x^2 - 9 = 13 \Rightarrow x^2 - 9 - 13 = 0$$

$$x^2 + 0x - 22 = 0$$

$$a = 1, b = 0, c = -22$$

**Q. 4. Determine whether the values given against each of the quadratic equation are the roots of the equation.**

$$(1) x^2 + 4x - 5 = 0, x = 1, -1$$

$$(2) 2m^2 - 5m = 0, m = 2, \frac{5}{2}$$

**Answer:**

$$1) x^2 + 4x - 5 = 0$$

$$\text{Put } x = 1$$

$$\Rightarrow 1^2 + 4 \times 1 - 5$$

$$\Rightarrow 1 + 4 - 5 = 0$$

Put  $x = -1$

$$\Rightarrow (-1)^2 + 4(-1) - 5$$

$$\Rightarrow 1 - 4 - 5 = -8$$

$\therefore x = 1$  is a root of the equation and  $x = -1$  is not a root of the equation.

$$2) 2m^2 - 5m = 0$$

Put  $m = 2, \Rightarrow 2(2)^2 - 5 \times 2 \Rightarrow 2 \times 4 - 10 \Rightarrow 8 - 10 \Rightarrow -2$

Put  $m = \frac{5}{2}, \Rightarrow 2\left(\frac{5}{2}\right)^2 - 5 \times \frac{5}{2} \Rightarrow 2 \times \frac{25}{4} - \frac{25}{2} \Rightarrow \frac{25}{2} - \frac{25}{2} = 0$

$\therefore m = 2$  is not root of the equation and  $m = \frac{5}{2}$  is a root of the equation.

**Q. 5. Find k if  $x = 3$  is a root of equation  $kx^2 - 10x + 3 = 0$ .**

**Answer :**

$$kx^2 - 10x + 3 = 0 \text{ Put } x = 3$$

$$\Rightarrow k(3)^2 - 10 \times 3 + 3 = 0$$

$$\Rightarrow 9k - 30 + 3 = 0$$

$$\Rightarrow 9k = 30 - 3$$

$$\Rightarrow 9k = 27$$

$$\Rightarrow k = \frac{27}{9} = 3$$

**Q. 6.** One of the roots of equation  $5m^2 + 2m + k = 0$  is  $\frac{-7}{5}$ . Complete the following activity to find the value of 'k'.

**Answer :**

is a root of quadratic equation  $kx^2 - 10x + 3 = 0$

$\therefore$  Put  $m = -\frac{7}{5}$  in the equation.

$$\Rightarrow 5 \times \left(-\frac{7}{5}\right)^2 + 2 \times \left(-\frac{7}{5}\right) + k = 0$$

$$\Rightarrow 5 \times \frac{49}{25} - \frac{14}{5} + k = 0$$

$$\Rightarrow \frac{35}{5} + k = 0$$

$$\Rightarrow k = -7$$

### Practice Set 2.2

**Q. 1 A.** Solve the following quadratic equation by factorization.

$$x^2 - 15x + 54 = 0$$

**Answer :**

$$x^2 - 15x + 54 = 0$$

$$\Rightarrow x^2 - 6x - 9x + 54 = 0$$

$$\Rightarrow x(x - 6) - 9(x - 6) = 0$$

$$\Rightarrow (x - 6)(x - 9) = 0$$

$$x - 6 = 0 \Rightarrow x = 6$$

$$x - 9 = 0 \Rightarrow x = 9$$

Hence,  $x = 6$  and  $x = 9$  are roots of the equation.

**Q. 1 B. Solve the following quadratic equation by factorization.**

$$x^2 + x - 20 = 0$$

**Answer :**

$$x^2 + x - 20 = 0$$

$$\Rightarrow x^2 + 5x - 4x - 20 = 0$$

$$\Rightarrow x(x + 5) - 4(x + 5) = 0$$

$$\Rightarrow (x + 5)(x - 4) = 0$$

$$x + 5 = 0 \Rightarrow x = -5$$

$$x - 4 = 0 \Rightarrow x = 4$$

Hence,  $x = -5$  and  $x = 4$  are roots of the equation.

**Q. 1 C. Solve the following quadratic equation by factorization.**

$$2y^2 + 27y + 13 = 0$$

**Answer :**

$$2y^2 + 27y + 13 = 0$$

$$\Rightarrow 2y^2 + 26y + y + 13 = 0$$

$$\Rightarrow 2y(y + 13) + (y + 13) = 0$$

$$\Rightarrow (2y + 1)(y + 13) = 0$$

$$2y + 1 = 0 \Rightarrow 2y = -1 \Rightarrow y = -\frac{1}{2}$$

$$y + 13 = 0 \Rightarrow y = -13$$

Hence,  $y = -13$  and  $y = -\frac{1}{2}$  are roots of the equation.

**Q. 1 D. Solve the following quadratic equation by factorization.**

$$5m^2 = 22m + 15$$

**Answer :**

$$5m^2 - 22m - 15 = 0$$

$$\Rightarrow 5m^2 - 3m + 25m - 15$$

$$\Rightarrow m(5m - 3) + 5(5m - 3)$$

$$\Rightarrow (m + 5)(5m - 3)$$

$$m + 5 = 0 \Rightarrow m = -5$$

$$5m - 3 = 0 \Rightarrow 5m = 3 \Rightarrow m = \frac{3}{5}$$



∴ Hence,  $m = -5$  and  $m = \frac{3}{5}$  are roots of the equation.

**Q. 1 E. Solve the following quadratic equation by factorization.**

$$2x^2 - 2x + \frac{1}{2} = 0$$

**Answer :**

$$2x^2 - 2x + \frac{1}{2} = 0$$

$$\Rightarrow 4x^2 - 4x + 1 = 0$$

$$\Rightarrow 4x^2 - 2x - 2x + 1$$

$$\Rightarrow 2x(2x - 1) - 1(2x - 1)$$

$$\Rightarrow (2x - 1)(2x - 1)$$

$$\Rightarrow 2x - 1 = 0 \Rightarrow x = \frac{1}{2}, \frac{1}{2}$$

Hence  $x = \frac{1}{2}, \frac{1}{2}$  are roots of the equation

**Q. 1 F. Solve the following quadratic equation by factorization.**

$$6x - \frac{2}{x} = 1$$

**Answer :**

$$6x^2 - 2 = x$$

$$\Rightarrow 6x^2 - x - 2 = 0$$

$$\Rightarrow 3x(2x + 1) - 2(2x + 1) = 0$$

$$\Rightarrow (3x - 2)(2x + 1) = 0$$

$$3x - 2 = 0 \Rightarrow 3x = 2 \Rightarrow x = \frac{2}{3}$$

$$2x + 1 = 0 \Rightarrow 2x = -1 \Rightarrow x = -\frac{1}{2}$$

Hence,  $x = \frac{2}{3}$  and  $x = -\frac{1}{2}$  are roots of the equation.

**Q. 1 G. Solve the following quadratic equation by factorization.**

$$\sqrt{2}x^2 + 7x + 5\sqrt{2} = 0$$

**to solve this quadratic equation by factorization, complete the following activity.**

**Answer :**

$$\sqrt{2}x^2 + 7x + 5\sqrt{2} = 0$$

$$\sqrt{2}x^2 + 5x + 2x + 5\sqrt{2} = 0$$

$$x(\sqrt{2}x + 5) + \sqrt{2}(\sqrt{2}x + 5) = 0$$

$$(x + \sqrt{2})(\sqrt{2}x + 5) = 0$$

$$(x + \sqrt{2}) = 0 \text{ or } (\sqrt{2}x + 5) = 0$$

$$x = -\frac{5}{\sqrt{2}} \text{ or } x = -\sqrt{2}$$

$\therefore -\frac{5}{\sqrt{2}}$  and  $-\sqrt{2}$  are roots of the equation.

**Q. 1 H. Solve the following quadratic equation by factorization.**

$$3x^2 - 2\sqrt{6}x + 2 = 0$$

**Answer :**

$$\Rightarrow 3x^2 - \sqrt{6}x - \sqrt{6}x + 2 = 0$$

$$\Rightarrow \sqrt{3}x(\sqrt{3}x - \sqrt{2}) - \sqrt{2}(\sqrt{3}x - \sqrt{2}) = 0$$

$$\Rightarrow (\sqrt{3}x - \sqrt{2})(\sqrt{3}x - \sqrt{2}) = 0$$

$$\Rightarrow (\sqrt{3}x - \sqrt{2}) = 0 \text{ or } (\sqrt{3}x - \sqrt{2}) = 0$$

$$x = \frac{\sqrt{2}}{\sqrt{3}} \text{ or } x = \frac{\sqrt{2}}{\sqrt{3}}$$

**Q. 1 I. Solve the following quadratic equation by factorization.**

$$2m(m-24) = 50$$

**Answer :**

$$2m(m-24) = 50$$

$$2m^2 - 48m - 50 = 0$$

$$\Rightarrow 2m^2 - 50m + 2m - 50 = 0$$

$$\Rightarrow 2m(m-25) + 2(m-25) = 0$$

$$\Rightarrow (2m+2)(m-25) = 0$$

$$\Rightarrow 2m + 2 = 0 \text{ or } m - 25 = 0$$

$$\Rightarrow m = -1 \text{ or } m = 25$$

Hence,  $m = -1$  or  $m = 25$  are roots of the equation.

**Q. 1 J. Solve the following quadratic equation by factorization.**

$$25m^2 = 9$$

**Answer :**

$$25m^2 = 9$$

$$\Rightarrow m^2 = \frac{9}{25}$$

$$\Rightarrow m = \sqrt{\frac{9}{25}}$$

$$\Rightarrow m = \pm \frac{3}{5}$$

Hence,  $m = \pm \frac{3}{5}$  are roots of the equation.

**Q. 1 K. Solve the following quadratic equation by factorization.**

$$7m^2 = 21m$$

**Answer :**

$$7m^2 - 21m = 0$$

$$\Rightarrow 7m(m - 3) = 0$$

$$\Rightarrow 7m = 0 \text{ or } m - 3 = 0$$

Hence,  $m = 0$  or  $m = 3$  are roots of the equation.

**Q. 1 L. Solve the following quadratic equation by factorization.**

$$m^2 - 11 = 0$$

**Answer :**

$$m^2 - 11 = 0$$

$$\Rightarrow m^2 = 11$$

$$\Rightarrow m = \sqrt{11}$$

$$\Rightarrow m = \pm 11$$

Hence,  $m = \pm 11$  are roots of the equation.

### Practice Set 2.3

**Q. 1 A. Solve the following quadratic equation by completing the square method.**

$$x^2 + x - 20 = 0$$

**Answer :**

$$x^2 + x - 20 = 0$$

$$\Rightarrow x^2 + x + \frac{1}{4} - \frac{1}{4} - 20 = 0$$

$$\Rightarrow \left(x^2 + x + \frac{1}{4}\right) + \left(\frac{1}{4} - 20\right) = 0$$

$$\Rightarrow \left(x + \frac{1}{2}\right)^2 - \frac{1 + 80}{4} = 0$$

$$\Rightarrow \left(x + \frac{1}{2}\right)^2 = \frac{81}{4}$$

$$\Rightarrow x + \frac{1}{2} = \sqrt{\frac{81}{4}}$$

$$\Rightarrow x + \frac{1}{2} = \pm \frac{9}{2}$$

$$\Rightarrow x + \frac{1}{2} = \frac{9}{2} \text{ or } x + \frac{1}{2} = -\frac{9}{2}$$

$$\Rightarrow x = \frac{9}{2} - \frac{1}{2} \text{ or } x = -\frac{9}{2} - \frac{1}{2}$$

$$\Rightarrow x = \frac{8}{2} \text{ or } x = -\frac{10}{2}$$

$$\Rightarrow x = 4 \text{ or } x = -5$$

**Q. 1 B. Solve the following quadratic equation by completing the square method.**

$$x^2 + 2x - 5 = 0$$

**Answer :**

$$x^2 + 2x - 5 = 0,$$

$$\Rightarrow x^2 + 2x + 1 - 1 - 5 = 0$$

$$\Rightarrow (x^2 + 2x + 1) - (1 + 5) = 0$$

$$\Rightarrow (x + 1)^2 - 6 = 0$$

$$\Rightarrow (x + 1)^2 = 6$$

$$\Rightarrow x + 1 = \sqrt{6}$$

$$\Rightarrow x + 1 = \pm\sqrt{6}$$

$$\Rightarrow x + 1 = \sqrt{6} \text{ or } x + 1 = -\sqrt{6}$$

$$\Rightarrow x = \sqrt{6} - 1 \text{ or } x = -\sqrt{6} - 1$$

**Q. 1 C. Solve the following quadratic equation by completing the square method.**

$$m^2 - 5m = -3$$

**Answer :**

$$m^2 - 5m + 3 = 0$$

$$\Rightarrow m^2 - 5m + \frac{25}{4} - \frac{25}{4} + 3 = 0 \quad \left( \text{Adding and Subtracting } \frac{25}{4} \right)$$

$$\Rightarrow \left( m^2 - 5m + \frac{25}{4} \right) = \frac{25}{4} - 3$$

$$\Rightarrow \left( m - \frac{5}{2} \right)^2 = \frac{25-12}{4}$$

$$\Rightarrow \left( m - \frac{5}{2} \right)^2 = \frac{13}{4}$$

$$\Rightarrow m - \frac{5}{2} = \sqrt{\frac{13}{4}}$$

$$\Rightarrow m - \frac{5}{2} = \pm \frac{\sqrt{13}}{2}$$

$$\Rightarrow m - \frac{5}{2} = \frac{\sqrt{13}}{2} \text{ or } m - \frac{5}{2} = -\frac{\sqrt{13}}{2}$$

$$\Rightarrow m = \frac{\sqrt{13}}{2} + \frac{5}{2} \text{ or } m = -\frac{\sqrt{13}}{2} - \frac{5}{2}$$

$$\Rightarrow m = \frac{\sqrt{13}+5}{2} \text{ or } m = \frac{-\sqrt{13}-5}{2}$$

**Q. 1 D. Solve the following quadratic equation by completing the square method.**

$$9y^2 - 12y + 2 = 0$$

**Answer :**

$$9y^2 - 12y + 2 = 0$$

$$(3y)^2 - 2 \times 3y \times 4 + (4)^2 - (4)^2 + 2 = 0$$

$$(3y)^2 - 2 \times 3y \times 4 + (4)^2 - 16 + 2 = 0$$

$$(3y - 4)^2 - 14 = 0$$

$$(3y - 4)^2 = 14$$

$$3y - 4 = \sqrt{14} \text{ or } 3y = 4 + \sqrt{14} \Rightarrow y = \frac{4 + \sqrt{14}}{3}$$

**Q. 1 E. Solve the following quadratic equation by completing the square method.**

$$2y^2 + 9y + 10 = 0$$

**Answer :**

$$2y^2 + 9y + 10 = 0$$

Steps involved in solving quadratic equation by completing the square method are –

**1. Making the first variable free of coefficient**

Dividing by the coefficient of 2, we get,



$$\Rightarrow y^2 + \frac{9}{2}y + 5 = 0$$

2. The coefficient of linear variable(variable with degree 1) is then squared and then added and subtracted from the equation.

$$\Rightarrow y^2 + \frac{9}{2}y + \frac{81}{16} - \frac{81}{16} + 5 = 0$$

3. Take out the terms following the formula  $(a + b)^2 = a^2 + b^2 + 2 a b$

$$\Rightarrow \left(y^2 + \frac{9}{2}y + \frac{81}{16}\right) - \left(\frac{81}{16} - 5\right) = 0$$

$$\Rightarrow \left(y + \frac{9}{2}\right)^2 = \frac{81}{16} - 5$$

$$\Rightarrow \left(y + \frac{9}{2}\right)^2 = \frac{81-80}{16}$$

$$\Rightarrow \left(y + \frac{9}{2}\right)^2 = \frac{1}{16}$$

$$\Rightarrow y + \frac{9}{2} = \sqrt{\frac{1}{16}}$$

$$\Rightarrow y + \frac{9}{2} = \pm \frac{1}{4}$$

$$\Rightarrow y + \frac{9}{2} = \frac{1}{4} \text{ or } y + \frac{9}{2} = -\frac{1}{4}$$

$$\Rightarrow y = \frac{1}{4} - \frac{9}{2} \text{ or } y = -\frac{1}{4} - \frac{9}{2}$$

$$\Rightarrow y = \frac{1-18}{4} \text{ or } y = \frac{-1-18}{4}$$

$$\Rightarrow y = -\frac{17}{4} \text{ or } y = -\frac{19}{4}$$

**Q. 1 F. Solve the following quadratic equation by completing the square method.**

$$5x^2 = 4x + 7 = 0$$

**Answer :**

$$5x^2 - 4x - 7 = 0$$

$$\Rightarrow x^2 - \frac{4}{5}x - \frac{7}{5} = 0$$

$$\Rightarrow x^2 - \frac{4}{5}x + \frac{4}{25} = \frac{7}{5} + \frac{4}{25} \quad \left( \text{Adding and Subtracting } \frac{4}{25} \right)$$

$$\Rightarrow \left( x + \frac{2}{5} \right)^2 = \frac{35+4}{25}$$

$$\Rightarrow \left( x + \frac{2}{5} \right)^2 = \frac{39}{25}$$

$$\Rightarrow x + \frac{2}{5} = \sqrt{\frac{39}{25}}$$

$$\Rightarrow x + \frac{2}{5} = \pm \frac{\sqrt{39}}{5}$$

$$x = \frac{\sqrt{39}}{5} - \frac{2}{5} \quad \text{or} \quad x = -\frac{\sqrt{39}}{5} - \frac{2}{5}$$

$$x = \frac{\sqrt{39} - 2}{5} \quad \text{or} \quad x = \frac{-\sqrt{39} - 2}{5}$$

### Practice Set 2.4

**Q. 1. Compare the given quadratic equations to the general form and write values of a, b, c.**

(1)  $x^2 - 7x + 5 = 0$

$$(2) 2m^2 = 5m - 5$$

$$(3) y^2 = 7y$$

**Answer :**

(1)

$$x^2 - 7x + 5 = 0 \text{ and } ax^2 + bx + c = 0$$

$$a = 1, b = -7, c = 5$$

(2)

$$2m^2 - 5m + 5 = 0 \text{ and } ax^2 + bx + c$$

$$a = 2, b = -5, c = 5$$

(3)

$$y^2 - 7y + 0 = 0 \text{ and } ax^2 + bx + c = 0$$

$$a = 1, b = -7, c = 0$$

**Q. 2 A. Solve using formula.**

$$x^2 + 6x + 5 = 0$$

**Answer :**

$$x^2 + 6x + 5 = 0$$

$$\Rightarrow x^2 + 6x + 5 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 1, b = 6 \text{ and } c = 5$$

$$\therefore b^2 - 4ac = 6^2 - 4(1)(5)$$

$$= 36 - 20$$

$$= 16$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-6 \pm \sqrt{16}}{2 \times 1} = \frac{-6 \pm 4}{2}$$

$$\Rightarrow x = \frac{-6+4}{2} \text{ or } x = \frac{-6-4}{2}$$

$$\Rightarrow x = -\frac{2}{2} \text{ or } x = -\frac{10}{2}$$

$$\Rightarrow x = -1 \text{ or } x = -5$$

**Q. 2 B. Solve using formula.**

$$x^2 - 3x - 2 = 0$$

**Answer :**

$$\Rightarrow x^2 + 3x - 2 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 1, b = 3 \text{ and } c = -2$$

$$\therefore b^2 - 4ac = 3^2 - 4(1)(-2)$$

$$= 9 + 8$$

$$= 17$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow x = \frac{-3 \pm \sqrt{17}}{2 \times 1}$$

$$\Rightarrow x = \frac{-3 \pm \sqrt{17}}{2}$$

$$\Rightarrow x = \frac{-3 + \sqrt{17}}{2} \text{ or } x = \frac{-3 - \sqrt{17}}{2}$$

**Q. 2 C. Solve using formula.**

$$3m^2 + 2m - 7 = 0$$

**Answer :**

$$\Rightarrow 3m^2 + 2m - 7 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 3, b = 2 \text{ and } c = -7$$

$$\therefore b^2 - 4ac = 2^2 - 4(3)(-7)$$

$$= 4 + 84$$

$$= 88$$

$$m = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow m = \frac{-2 \pm \sqrt{88}}{2 \times 3}$$

$$\Rightarrow m = \frac{-2 \pm \sqrt{88}}{6}$$

$$\Rightarrow m = \frac{-2 + 2\sqrt{22}}{6} \text{ or } m = \frac{-2 - 2\sqrt{22}}{6}$$

$$\Rightarrow m = \frac{-1 + \sqrt{22}}{3} \text{ or } m = \frac{-1 - \sqrt{22}}{3}$$

**Q. 2 D. Solve using formula.**

$$5m^2 - 4m - 2 = 0$$

**Answer :**

$$\Rightarrow 5m^2 - 4m - 2 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 5, b = -4 \text{ and } c = -2$$

$$\therefore b^2 - 4ac = (-4)^2 - 4(5)(-2)$$

$$= 16 + 40$$

$$= 56$$

$$m = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow m = \frac{-(-4) \pm \sqrt{56}}{2 \times 5}$$

$$\Rightarrow m = \frac{4 \pm 2\sqrt{14}}{10}$$

$$\Rightarrow m = \frac{4 + 2\sqrt{14}}{10} \text{ or } m = \frac{4 - 2\sqrt{14}}{10}$$

$$\Rightarrow m = \frac{2 + \sqrt{14}}{5} \text{ or } m = \frac{2 - \sqrt{14}}{5}$$

**Q. 2 E. Solve using formula.**

$$y^2 + \frac{1}{3}y = 2$$

**Answer :**

$$3y^2 + y - 6 = 0$$

$$\Rightarrow 3y^2 + y - 6 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 3, b = 1 \text{ and } c = -6$$

$$\therefore b^2 - 4ac = 1^2 - 4(3)(-6)$$

$$= 1 + 72$$

$$= 73$$

$$Y = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow y = \frac{-1 \pm \sqrt{73}}{2 \times 3}$$

$$\Rightarrow y = \frac{-1 \pm \sqrt{73}}{6}$$

$$\Rightarrow y = \frac{-1 + \sqrt{73}}{6} \text{ or } y = \frac{-1 - \sqrt{73}}{6}$$

**Q. 2 F. Solve using formula.**

$$5x^2 + 13x + 8 = 0$$

**Answer :**

$$\Rightarrow 5x^2 + 13x + 8 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 5, b = 13 \text{ and } c = 8$$

$$\therefore b^2 - 4ac = 13^2 - 4(5)(8)$$

$$= 169 - 160$$

$$= 9$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow x = \frac{-13 \pm \sqrt{9}}{2 \times 5}$$

$$\Rightarrow x = \frac{-13 \pm 3}{10}$$

$$\Rightarrow x = \frac{-13 + 3}{10} \text{ or } x = \frac{-13 - 3}{10}$$

$$\Rightarrow x = \frac{-10}{10} \text{ or } x = \frac{-16}{10}$$

$$\Rightarrow x = -1 \text{ or } x = -\frac{8}{5}$$

**Q. 3. With the help of the flow chart given below solve the equation  $x^2 + 2\sqrt{3}x + 3 = 0$  using the formula.**

**Answer :**

$$\Rightarrow x^2 + 2\sqrt{3}x + 3 = 0 \text{ compare with } ax^2 + bx + c = 0$$



$$\Rightarrow a = 1, b = 2\sqrt{3} \text{ and } c = 3$$

$$\therefore b^2 - 4ac = (2\sqrt{3})^2 - 4(1)(3)$$

$$= 12 - 12$$

$$= 0$$

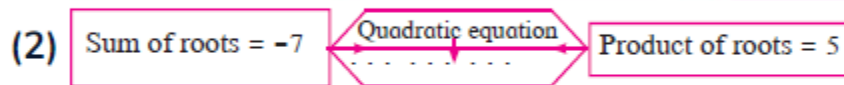
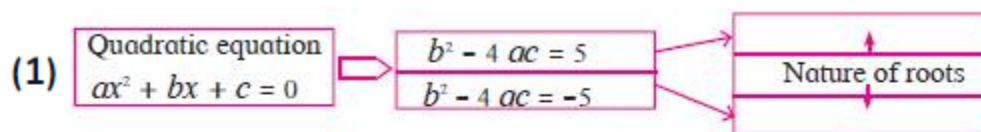
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow x = \frac{-2\sqrt{3} \pm \sqrt{0}}{2 \times 1}$$

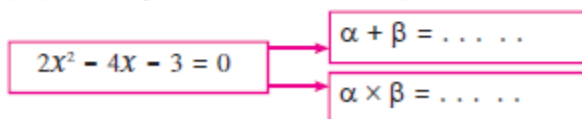
$$\Rightarrow x = \frac{-2\sqrt{3}}{2}$$

### Practice Set 2.5

Q. 1. Activity: Fill in the gaps and complete.



(3) If  $\alpha, \beta$  are roots of quadratic equation,



Answer :

(1) Roots are distinct and real when  $b^2 - 4ac = 5$ , not real when  $b^2 - 4ac = -5$ .

(2)  $x^2 + 7x + 5 = 0$

(3)

$$\alpha + \beta = 2, \alpha \times \beta = -\frac{3}{2}$$

**Q. 2 A. Find the value of discriminant.**

$$x^2 + 7x - 1 = 0$$

**Answer :**

$$\Rightarrow x^2 + 7x - 1 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 1, b = 7 \text{ and } c = -1$$

$$\therefore b^2 - 4ac = 7^2 - 4(1)(-1)$$

$$= 49 + 4$$

$$= 53$$

**Q. 2 B. Find the value of discriminant.**

$$2y^2 - 5y + 10 = 0$$

**Answer :**

$$\Rightarrow 2y^2 - 5y + 10 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 2, b = -5 \text{ and } c = 10$$

$$\therefore b^2 - 4ac = -5^2 - 4(2)(10)$$

$$= 25 - 80$$

$$= -55$$

**Q. 2 C. Find the value of discriminant.**

$$\sqrt{2}x^2 + 4x + 2\sqrt{2} = 0$$

**Answer :**

$$\Rightarrow \sqrt{2}x^2 + 4x + 2\sqrt{2} = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = \sqrt{2}, b = 4 \text{ and } c = 2\sqrt{2}$$

$$\therefore b^2 - 4ac = 4^2 - 4(\sqrt{2})(2\sqrt{2})$$

$$= 16 - 16$$

$$= 0$$

**Q. 3 A. Determine the nature of roots of the following quadratic equation.**

$$x^2 - 4x + 4 = 0$$

**Answer :**

$$\Rightarrow x^2 - 4x + 4 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 1, b = -4 \text{ and } c = 4$$

$$\therefore b^2 - 4ac = -4^2 - 4(1)(4)$$

$$= 16 - 16$$

$$= 0$$

$\therefore b^2 - 4ac = 0$  . hence, roots are real and equal

**Q. 3 B. Determine the nature of roots of the following quadratic equation.**

$$2y^2 - 7y + 2 = 0$$

**Answer :**

$$\Rightarrow 2y^2 - 7y + 2 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 2, b = -7 \text{ and } c = 2$$

$$\therefore b^2 - 4ac = -7^2 - 4(2)(2)$$

$$= 49 - 16$$

$$= 23$$

$\therefore b^2 - 4ac > 0$ . Hence, roots are real and unequal

**Q. 3 C. Determine the nature of roots of the following quadratic equation.**

$$m^2 + 2m + 9 = 0$$

**Answer :**

$$\Rightarrow m^2 + 2m + 9 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 1, b = 2 \text{ and } c = 9$$

$$\therefore b^2 - 4ac = 2^2 - 4(1)(9)$$

$$= 4 - 36$$

$$= -32$$

$\therefore b^2 - 4ac < 0$  .hence, roots are not real.

**Q. 4. Form the quadratic equation from the roots given below.**

(1) 0 and 4

(2) 3 and -10

(3)  $\frac{1}{2}, -\frac{1}{2}$

(4)  $2 - \sqrt{5}, 2 + \sqrt{5}$

(1) Let  $\alpha = 0$  and  $\beta = 4$

$$\therefore \alpha + \beta = 0 + 4 = 4 \text{ and } \alpha\beta = 0 \times 4 = 0$$

$\therefore$  and quadratic equation is,  $x^2 - (\alpha + \beta)x + \alpha\beta = 0$

$$\therefore x^2 - (4)x + (0) = 0$$

$$\therefore x^2 - 4x = 0$$

(2) Let  $\alpha = 3$  and  $\beta = -10$

$$\therefore \alpha + \beta = 3 - 10 = -7 \text{ and } \alpha\beta = 3 \times -10 = -30$$

$\therefore$  and quadratic equation is,  $x^2 - (\alpha + \beta)x + \alpha\beta = 0$

$$\therefore x^2 - (-7)x + (-30) = 0$$

$$\therefore x^2 + 7x - 30 = 0$$

(3) Let  $\alpha = \frac{1}{2}$  and  $\beta = -\frac{1}{2}$

$$\therefore \alpha + \beta = \frac{1}{2} - \frac{1}{2} = 0 \text{ and } \alpha\beta = \frac{1}{2} \times -\frac{1}{2} = -\frac{1}{4}$$

$\therefore$  and quadratic equation is,  $x^2 - (\alpha + \beta)x + \alpha\beta = 0$

$$\therefore x^2 - (0)x + \left(-\frac{1}{4}\right) = 0$$

$$\therefore x^2 - \frac{1}{4} = 0$$

$$\therefore 4x^2 - 1 = 0$$

(4) Let  $\alpha = 2 - \sqrt{5}$  and  $\beta = 2 + \sqrt{5}$

$$\therefore \alpha + \beta = 2 - \sqrt{5} + 2 + \sqrt{5} = 4 \text{ and } \alpha\beta = (2 - \sqrt{5})(2 + \sqrt{5}) = 4 - 5 = 1$$

$\therefore$  and quadratic equation is,  $x^2 - (\alpha + \beta)x + \alpha\beta = 0$

$$\therefore x^2 - (4)x + (1) = 0$$

$$\therefore x^2 - 4x + 1 = 0$$

**Q. 5. Sum of the roots of a quadratic equation is double their product. Find k if equation is**

$$x^2 - 4kx + k + 3 = 0$$

**Answer :** According to question

$$\alpha + \beta = 2\alpha\beta$$

$$\Rightarrow 4k = 2(k + 3)$$

$$\Rightarrow 4k = 2k + 6$$

$$\Rightarrow 4k - 2k = 6$$

$$\Rightarrow 2k = 6$$

$$\Rightarrow k = 3$$

**Q. 6.**  $\alpha, \beta$  are roots of  $y^2 - 2y - 7 = 0$  find,

(1)  $\alpha^2 + \beta^2$

(2)  $\alpha^3 + \beta^3$

**Answer :**

$$y^2 - 2y - 7 = 0$$

$$\alpha + \beta = 2 \text{ and } \alpha\beta = -7$$

$$(1). (\alpha + \beta)^2 = \alpha^2 + \beta^2 + 2\alpha\beta$$

$$\Rightarrow (2)^2 = \alpha^2 + \beta^2 + 2(-7)$$

$$\Rightarrow 4 + 14 = \alpha^2 + \beta^2$$

$$\Rightarrow \alpha^2 + \beta^2 = 18$$

$$(2). (\alpha + \beta)^3 = \alpha^3 + \beta^3 + 3\alpha\beta(\alpha + \beta)$$

$$\Rightarrow (2)^3 = \alpha^3 + \beta^3 + 3(-7)(2)$$

$$\Rightarrow 8 + 42 = \alpha^3 + \beta^3$$

$$\Rightarrow \alpha^3 + \beta^3 = 50$$

**Q. 7 A.** The roots of each of the following quadratic equation are real and equal, find k.

$$3y^2 + ky + 12 = 0$$

**Answer :**

$$\Rightarrow 3y^2 - ky + 12 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 3, b = -k \text{ and } c = 12$$

$$\therefore b^2 - 4ac = -k^2 - 4(3)(12)$$

$$= k^2 - 144$$

If roots are equal and real then,  $\therefore b^2 - 4ac = 0$

$$k^2 - 144 = 0$$

$$\Rightarrow k^2 = 144$$

$$\Rightarrow k = \pm 12$$

$$\therefore k = 12 \text{ and } k = -12$$

**Q. 7 B.** The roots of each of the following quadratic equation are real and equal, find k.

$$kx(x-2) + 6 = 0$$

**Answer :**

$$kx(x-2) + 6 = 0 \Rightarrow kx^2 - 2kx + 6 = 0$$

$$\Rightarrow kx^2 - 2kx + 6 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = k, b = -2k \text{ and } c = 6$$



$$\therefore b^2 - 4ac = (-2k)^2 - 4(k)(6)$$

$$= 4k^2 - 24k$$

If roots are equal and real then,  $\therefore b^2 - 4ac = 0$

$$4k^2 - 24k = 0$$

$$\Rightarrow 4k(k - 6) = 0$$

$$\Rightarrow 4k = 0 \text{ and } k - 6 = 0$$

$$\therefore k = 0 \text{ and } k = 6$$

### Practice Set 2.6

**Q. 1. Product of Pragati's age 2 years ago and 3 years hence is 84. Find her present age.**

**Answer :**

Let her present age be  $x$

According to question,

$$(x - 2)(x + 3) = 84$$

$$\Rightarrow x^2 + x - 6 = 84$$

$$\Rightarrow x^2 + x - 90 = 0$$

$$\Rightarrow x^2 + 10x - 9x - 90 = 0$$

$$\Rightarrow x(x + 10) - 9(x + 10) = 0$$

$$\Rightarrow (x - 9)(x + 10) = 0$$

$$\Rightarrow x - 9 = 0 \text{ or } x + 10 = 0$$

$$\Rightarrow x = 9 \text{ or } x = -10$$

As age cannot be in negative,  $\therefore$  Pragati's age is 9 years.

**Q. 2. The sum of squares of two consecutive natural numbers is 244; find the numbers.**

**Answer :** Let the two consecutive natural numbers be  $x$  and  $x + 2$ . Then,

$$x^2 + (x + 2)^2 = 244$$

$$\Rightarrow x^2 + x^2 + 4x + 4 = 244$$

$$\Rightarrow 2x^2 + 4x - 240 = 0$$

$$\Rightarrow x^2 + 2x - 120 = 0$$

$$\Rightarrow x^2 + 12x - 10x - 120 = 0$$

$$\Rightarrow x(x + 12) - 10(x + 12) = 0$$

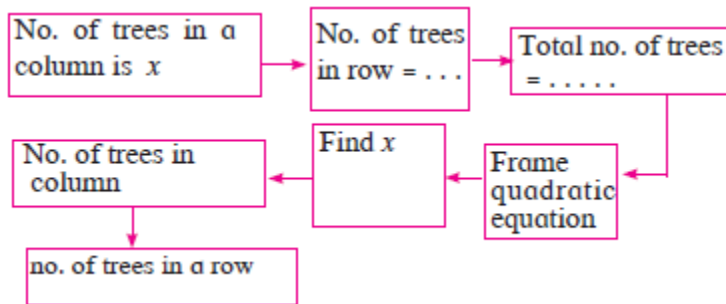
$$\Rightarrow (x + 12)(x - 10) = 0$$

$$x + 12 = 0 \text{ or } x - 10 = 0$$

$$x = -12 \text{ or } x = 10$$

No.s cannot be negative,  $\therefore$  numbers are 10 and 12

**Q. 3.** In the orange garden of Mr. Madhusudan there are 150 orange trees. The number of trees in each row is 5 more than that in each column. Find the number of trees in each row and each column with the help of following flow chart.



**Answer :** Let the number of columns be  $x$

$$\therefore \text{rows} = x + 5$$

$$x(x + 5) = 150$$

$$\Rightarrow x^2 + 5x - 150 = 0$$

$$\Rightarrow x^2 + 15x - 10x - 150 = 0$$

$$\Rightarrow x(x + 15) - 10(x + 15) = 0$$

$$\Rightarrow (x + 15)(x - 10) = 0$$

$$x + 15 = 0 \text{ or } x - 10 = 0$$

$$x = -15 \text{ or } x = 10$$

Hence, columns cannot be negative.  $\therefore$  columns are 10

and rows are 15.

**Q. 4.** Vivek is older than Kishor by 5 years. The sum of the reciprocals of their ages is  $\frac{1}{6}$ . Find their present ages.

**Answer :**

Let Kishor's present age be  $x$ . Then, vivek's age =  $x + 5$

$$\therefore \frac{1}{x} + \frac{1}{x+5} = \frac{1}{6}$$

$$\Rightarrow \frac{x+5+x}{x(x+5)} = \frac{1}{6} \Rightarrow 6(5 + 2x) = x^2 + 5x$$

$$\Rightarrow 30 + 12x = x^2 + 5x$$

$$\Rightarrow x^2 + 5x - 12x - 30 = 0$$

$$\Rightarrow x^2 - 7x - 30 = 0$$

$$\Rightarrow x^2 - 10x + 3x - 30 = 0$$

$$\Rightarrow x(x - 10) + 3(x - 10) = 0$$

$$\Rightarrow (x - 10)(x + 3) = 0$$

$$x - 10 = 0 \text{ or } x + 3 = 0$$

$$x = 10 \text{ or } x = -3$$

Hence, age cannot be negative.  $\therefore$  age of Kishor is 10

and age of Vivek is 15.

**Q. 5. Suyash scored 10 marks more in second test than that in the first. 5 times the score of the second test is the same as square of the score in the first test. Find his score in the first test.**

**Answer :** Let the score of first test be  $x$ . Then, second test score =  $x + 10$ .

$$\therefore 5(x + 10) = x^2$$

$$\Rightarrow 5x + 50 = x^2$$

$$\Rightarrow x^2 - 5x - 50 = 0$$

$$\Rightarrow x^2 - 10x + 5x - 50 = 0$$

$$\Rightarrow x(x - 10) + 5(x - 10) = 0$$

$$\Rightarrow (x - 10)(x + 5) = 0$$

$$x - 10 = 0 \text{ or } x + 5 = 0$$

$$x = 10 \text{ or } x = -5$$

Hence, score of first test is 10 as marks are not negative.

**Q. 6. Mr. Kasam runs a small business of making earthen pots. He makes certain number of pots on daily basis. Production cost of each pot is ₹40 more than 10 times total number of pots, he makes in one day. If production cost of all pots per day is ₹600, find production cost of one pot and number of pots he makes per day.**

**Answer :** Let the number of pots made by Mr. Kasam each day be  $x$ . Then, production cost of each pot =

$$₹40 + 10(x)$$

$$\therefore \text{total cost} = (40 + 10x)x = 40x + 10x^2$$

$$10x^2 + 40x = 600$$

$$\Rightarrow 10x^2 + 40x - 600 = 0$$

$$\Rightarrow x^2 + 4x - 60 = 0$$

$$\Rightarrow x^2 - 6x + 10x - 60 = 0$$

$$\Rightarrow x(x - 6) + 10(x - 6) = 0$$

$$\Rightarrow (x - 6)(x + 10) = 0$$

$$x - 6 = 0 \text{ or } x + 10 = 0$$

$$x = 6 \text{ or } x = -10$$

Hence number of pots made cannot be negative.  $\therefore$  number of pots he made each day = 6

$$\text{Cost of one pot} = 40 + 10(6) = 40 + 60 = ₹100$$

**Q. 7. Pratik takes 8 hours to travel 36 km downstream and return to the same spot. The speed of boat in still water is 12 km. per hour. Find the speed of water current.**

**Answer :**

Let the speed of water current be  $x$ .

$$\therefore T_1 = \frac{D_1}{S_1} = \frac{36}{12+x} \text{ hr}$$

$$T_2 = \frac{D_2}{S_2} = \frac{36}{12-x} \text{ hr}$$

$$8 \text{ hr} = \frac{36}{12+x} + \frac{36}{12-x}$$

$$8 = \frac{[36(12-x) + 36(12+x)]}{144-x^2}$$

$$8 = \frac{36(12-x+12+x)}{144-x^2}$$

$$144-x^2 = \frac{36 \times 24}{8}$$

$$144-x^2 = 108$$

$$144 - 108 = x^2$$

$$\Rightarrow 36 = x^2$$

$$\Rightarrow x = \pm 6$$

Speed of water current is 6km/hr

**Q. 8. Pintu takes 6 days more than those of Nishu to complete certain work. If they work together they finish it in 4 days. How many days would it take to complete the work if they work alone.**

**Answer :**

Suppose Nishu alone takes  $x$  days to finish work. Then , Pintu alone can finish in  $(x + 6)$ days.

$$\Rightarrow \text{Nishu's one day work} + \text{Pintu's one day work} = \frac{1}{x} + \frac{1}{x+6}$$

$$\text{(Nishu + Pintu)'s one day work} = \frac{1}{4}$$

$$\therefore \frac{1}{x} + \frac{1}{x+6} = \frac{1}{4}$$

$$\therefore \frac{1}{x} + \frac{1}{x+6} = \frac{1}{4}$$

$$\Rightarrow \frac{x+6+x}{x(x+6)} = 4$$

$$\Rightarrow 4(x+6+x) = x(x+6)$$

$$\Rightarrow 4x + 24 + 4x = x^2 + 6x$$

$$\Rightarrow x^2 + 6x - 8x - 24 = 0$$

$$\Rightarrow x^2 - 2x - 24 = 0$$

$$\Rightarrow x^2 - 6x + 4x - 24 = 0$$

$$\Rightarrow x(x-6) + 4(x-6) = 0$$

$$\Rightarrow (x-6)(x+4) = 0$$

$$x-6 = 0 \text{ or } x+4 = 0$$

$$x = 6 \text{ or } x = -4$$

$x = -4$  is not possible, as no of days can't be negative.

Nishu will take 6 days alone and Pintu takes 12 days alone.

**Q. 9. If 460 is divided by a natural number, quotient is 6 more than five times the divisor and remainder is 1. Find quotient and divisor.**

**Answer :** Let the divisor be  $x$ . Then, Quotient be  $6 + 5x$

Now according to question,

dividend = divisor  $\times$  quotient + remainder.

$$\Rightarrow 460 = x \times (6 + 5x) + 1$$

$$\Rightarrow 459 = 5x^2 + 6x$$

$$\Rightarrow 5x^2 + 6x - 459 = 0$$

$$\Rightarrow 5x^2 - 45x + 51x - 459 = 0$$

$$\Rightarrow 5x(x-9) + 51(x-9) = 0$$

$$\Rightarrow (5x-51)(x-9) = 0$$

$$5x-51 = 0 \text{ or } x-9 = 0$$

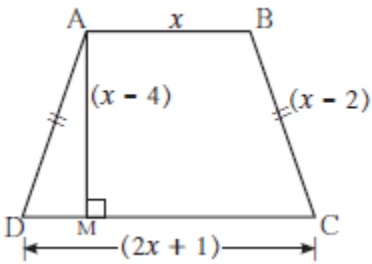
$$x = \frac{51}{5} \text{ or } x = 9$$

$\therefore$  divisor = 9 and quotient =  $6 + 5 \times 9 = 6 + 45 = 51$

$\therefore$  Divisor = 9, quotient = 51



Q. 10. In the adjoining fig. □ABCD is a trapezium AB||CD and its area is 33 cm<sup>2</sup>. From the information given in the figure find the lengths of all sides of the □ABCD. Fill in the empty boxes to get the solution.



Answer :

□ ABCD is a trapezium.

AB||CD

$$A(\square ABCD) = \frac{1}{2}(AB + CD) \times AM$$

$$33 = \frac{1}{2}(x + 2x + 1) \times (x - 4)$$

$$\therefore 3x(x - 7) + 10(x - 7) = 0$$

$$\therefore (3x + 10)(x - 7) = 0$$

$$\therefore 3x + 10 = 0 \text{ or } x - 7 = 0$$

$$\therefore x = -\frac{10}{3} \text{ or } x = 7$$

But length is never negative.

$$\therefore x \neq \frac{10}{3}$$

$$\therefore x = 7$$

AB = 7 cm, CD = 15 cm, AD = BC = 5 cm.

## Problem Set 2

**Q. 1 A. Choose the correct answer for the following question.**

**Which one is the quadratic equation?**

A.  $\frac{5}{x} - 3 = x^2$

B.  $x(x + 5) = 2$

C.  $n - 1 = 2n$

D.  $\frac{1}{x^2}(x + 2) = x$

**Answer :**

In option A  $\frac{5}{x} - 3 = x^2 \Rightarrow 5 - 3x = x^3$ . hence , it is not a quadratic equation.

In Option B  $x(x + 5) = 2 \Rightarrow x^2 + 5x - 2 = 0$ , it is a quadratic equation.

In Option C  $n - 1 = 2n \Rightarrow 2n - n = -1 \Rightarrow n = -1$ , it is not a quadratic equation.

In Option D  $\frac{1}{x^2}(x + 2) = x \Rightarrow x + 2 = x^3$ , hence, it is not a quadratic equation.

**Q. 1 B. Choose the correct answer for the following question.**

**Out of the following equations which one is not a quadratic equation?**

A.  $x^2 + 4x = 11 + x^2$

B.  $x^2 = 4x$

C.  $5x^2 = 90$

D.  $2x - x^2 = x^2 + 5$

**Answer :**

$$x^2 + 4x - 11 - x^2 = 0 \Rightarrow 4x - 11 = 0$$

In all other options highest degree of equation is 2, which also the degree of quadratic equation. But in Option A, degree of polynomial is 1

**Q. 1 C. Choose the correct answer for the following question.**

**The roots of  $x^2 + kx + k = 0$  are real and equal, find k.**

- A. 0**
- B. 4**
- C. 0 or 4**
- D. 2**

**Answer :**

$x^2 + kx + k = 0$ , equation has real and equal roots.

$$\therefore b^2 - 4ac = 0$$

$$\Rightarrow k^2 - 4(1)k = 0$$

$$\Rightarrow k(k - 4) = 0$$

$$k = 0 \text{ or } k - 4 = 0 \Rightarrow k = 4$$

$$\therefore k = 0 \text{ or } 4$$

**Q. 1 D. Choose the correct answer for the following question.**

For  $\sqrt{2}x^2 - 5x + \sqrt{2} = 0$  find the value of the discriminant.

A. -5

B. 17

C. 2

D.  $2\sqrt{2} - 5$

**Answer :**

$$\Rightarrow \sqrt{2}x^2 + 5x + \sqrt{2} = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = \sqrt{2}, b = 5 \text{ and } c = \sqrt{2}$$

$$\therefore b^2 - 4ac = 5^2 - 4(\sqrt{2})(\sqrt{2})$$

$$= 25 - 8$$

$$= 17$$

**Q. 1 E. Choose the correct answer for the following question.**

Which of the following quadratic equations has roots 3, 5?

A.  $x^2 - 15x + 8 = 0$

B.  $x^2 - 8x + 15 = 0$

C.  $x^2 + 3x + 5 = 0$

D.  $x^2 + 8x - 15 = 0$

**Answer :**

In option A,

$$\Rightarrow x^2 - 15x + 8 = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{15 \pm \sqrt{-15^2 - 4(1)(8)}}{2 \times 1} = \frac{15 \pm \sqrt{225 - 80}}{2} = \frac{15 \pm \sqrt{145}}{2}$$

In option B

$$x^2 - 8x + 15 = 0$$

$$x^2 - 5x - 3x + 15 = 0$$

$$\Rightarrow x(x - 5) - 3(x - 5) = 0$$

$$\Rightarrow (x - 5)(x - 3) = 0$$

$$x - 5 = 0 \text{ or } x - 3 = 0$$

$$x = 5 \text{ and } x = 3$$

In option c,

$$\Rightarrow x^2 + 3x + 5 = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-3 \pm \sqrt{3^2 - 4(1)(5)}}{2 \times 1} = \frac{-3 \pm \sqrt{9 - 20}}{2} = \frac{(-3 \pm \sqrt{-11})}{2}$$

In option d

$$x^2 + 8x - 15 = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-8 \pm \sqrt{8^2 - 4(1)(15)}}{2 \times 1} = \frac{-8 \pm \sqrt{64 - 60}}{2} = \frac{(-8 \pm 2)}{2}$$

$$x = \frac{-8 + 2}{2} = -\frac{6}{2} = -3 \text{ or } x = \frac{-8 - 2}{2} = -\frac{10}{2} = -5$$

**Q. 1 F. Choose the correct answer for the following question.**

**Out of the following equations, find the equation having the sum of its roots -5.**

- A.  $3x^2 - 15x + 3 = 0$
- B.  $x^2 - 5x + 3 = 0$
- C.  $x^2 + 3x - 5 = 0$
- D.  $3x^2 + 15x + 3 = 0$

Answer :

Sum of the roots i.e.  $\alpha + \beta = -\frac{b}{a}$

$\therefore$  in option A,  $\alpha + \beta = -\frac{-15}{3} = 5$

$\therefore$  in option B,  $\alpha + \beta = -\frac{-5}{1} = 5$

$\therefore$  in option C,  $\alpha + \beta = -\frac{3}{1} = 3$

$\therefore$  in option D,  $\alpha + \beta = -\frac{15}{3} = -5$

**Q. 1 G. Choose the correct answer for the following question.**

$\sqrt{5}m^2 - \sqrt{5}m + \sqrt{5} = 0$  which of the following statement is true for this given equation?

- A. Real and unequal roots
- B. Real and equal roots
- C. Roots are not real
- D. Three roots.

Answer :

$\Rightarrow \sqrt{5}m^2 + \sqrt{5}m + \sqrt{5} = 0$  compare with  $ax^2 + bx + c = 0$

$\Rightarrow a = \sqrt{5}, b = \sqrt{5}$  and  $c = \sqrt{5}$

$\therefore b^2 - 4ac = \sqrt{5}^2 - 4(\sqrt{5})(\sqrt{5})$

$$= 5 - 20$$

$$= -15$$

∴  $b^2 - 4ac < 0$  . hence, roots are not real.

**Q. 1 H. Choose the correct answer for the following question.**

**One of the roots of equation  $x^2 + mx - 5 = 0$  is 2; find m.**

A. -2

B.  $-\frac{1}{2}$

C.  $\frac{1}{2}$

D. 2

**Answer :**

$x^2 + mx - 5 = 0$  , Put value of  $x = 2$

$$2^2 + 2m = 5 \Rightarrow 2m = 5 - 4 \Rightarrow m = \frac{1}{2}$$

**Q. 2. Which of the following equations is quadratic?**

(1)  $x^2 + 2x + 11 = 0$

(2)  $x^2 - 2x + 5 = x^2$

(3)  $(x + 2)^2 = 2x^2$

**Answer :**

1.  $x^2 + 2x - 11 = 0$  is a quadratic equation because it is the form of  $ax^2 + bx + c = 0$  and it has degree 2.

2.  $x^2 - 2x + 5 = x^2$

$-2x + 5 = 0 \therefore$  it is not a quadratic equation because it is not in the form of  $ax^2 + bx + c = 0$  and it doesn't have degree 2.

$$3. (x + 2)^2 = 2x^2 \Rightarrow x^2 + 4x + 4 = 2x^2$$

$x^2 - 4x - 4 = 0$  is a quadratic equation because it is the form of  $ax^2 + bx + c = 0$  and it has degree 2.

**Q. 3 A. Find the value of discriminant for each of the following equation.**

$$2y^2 - y + 2 = 0$$

**Answer :**

$$\Rightarrow 2y^2 - y + 2 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 2, b = -1 \text{ and } c = 2$$

$$\therefore b^2 - 4ac = (-1)^2 - 4(2)(2)$$

$$= 1 - 16$$

$$= -15$$

**Q. 3 B. Find the value of discriminant for each of the following equation.**

$$5m^2 - m = 0$$

**Answer :**

$$\Rightarrow 5m^2 - m = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 5, b = -1 \text{ and } c = 0$$

$$\therefore b^2 - 4ac = (-1)^2 - 4(5)(0)$$

$$= 1$$



**Q. 3 C. Find the value of discriminant for each of the following equation.**

$$\sqrt{5}x^2 - x - \sqrt{5} = 0$$

**Answer :**

$$\Rightarrow \sqrt{5}x^2 - x - \sqrt{5} = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = \sqrt{5}, b = -1 \text{ and } c = -\sqrt{5}$$

$$\therefore b^2 - 4ac = -1^2 - 4(\sqrt{5})(-\sqrt{5})$$

$$= 1 + 20$$

$$= 21$$

**Q. 4. One of the roots of quadratic equation  $2x^2 + kx - 2 = 0$  is -2, find k.**

**Answer :**

$$2x^2 + kx - 2 = 0$$

$$\Rightarrow 2 \times (-2)^2 - 2k - 2 = 0$$

$$\Rightarrow 8 - 2 - 2k = 0$$

$$\Rightarrow 6 = 2k$$

$$k = 3$$

**Q. 5 A. Two roots of quadratic equations are given ; frame the equation.**

**10 and -10**

**Answer :**

$$\text{Let } \alpha = 10 \text{ and } \beta = -10$$

$$\therefore \alpha + \beta = 10 - 10 = 0 \quad \alpha\beta = 10(-10) = -100$$

$$\therefore \text{and quadratic equation is, } x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$\Rightarrow x^2 - 0(x) - 100 = 0$$

$$\Rightarrow x^2 - 100 = 0$$

**Q. 5 B. Two roots of quadratic equations are given ; frame the equation.**

**$1-3\sqrt{5}$  and  $1 + 3\sqrt{5}$**

**Answer :**

$$\text{Let } \alpha = 1 - 3\sqrt{5} \text{ and } \beta = 1 + 3\sqrt{5}$$

$$\therefore \alpha + \beta = 1 - 3\sqrt{5} + 1 + 3\sqrt{5} = 2 \text{ and } \alpha\beta = (1 - 3\sqrt{5}) \times (1 + 3\sqrt{5})$$

$$= 1 - 45 = -44$$

$$\therefore \text{ and quadratic equation is, } x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$\therefore x^2 - (2)x + (-44) = 0$$

$$\therefore x^2 - 2x - 44 = 0$$

**Q. 5 C. Two roots of quadratic equations are given ; frame the equation.**

**0 and 7**

**Answer :**

$$\therefore \text{ Let } \alpha = 0 \text{ and } \beta = 7$$

$$\therefore \alpha + \beta = 0 + 7 = 7 \text{ and } \alpha\beta = 0 \times 7 = 0$$

$$\therefore \text{ and quadratic equation is, } x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$\therefore x^2 - (7)x + (0) = 0$$

$$\therefore x^2 - 7x = 0$$

**Q. 6 A. Determine the nature of roots for each of the quadratic equation.**

$$3x^2 - 5x + 7 = 0$$

**Answer :**

$$\Rightarrow 3x^2 - 5x + 7 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 3, b = -5 \text{ and } c = 7$$

$$\therefore b^2 - 4ac = -5^2 - 4(3)(7)$$

$$= 25 - 147$$

$$= -122$$

$\therefore b^2 - 4ac < 0$  .hence, roots are not real.

**Q. 6 B. Determine the nature of roots for each of the quadratic equation.**

$$\sqrt{3}x^2 + \sqrt{2}x - 2\sqrt{3} = 0$$

**Answer :**

$$\Rightarrow \sqrt{3}x^2 + \sqrt{2}x + 2\sqrt{3} = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = \sqrt{3}, b = \sqrt{2} \text{ and } c = -2\sqrt{3}$$

$$\therefore b^2 - 4ac = \sqrt{2}^2 - 4(\sqrt{3})(-2\sqrt{3})$$

$$= 2 + 24$$

$$= 26$$

$\therefore b^2 - 4ac > 0$  .hence, roots are real and unequal .

**Q. 6 C. Determine the nature of roots for each of the quadratic equation.**

$$m^2 - 2m + 1 = 0$$

**Answer :**

$$\Rightarrow m^2 - 2m + 1 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 1, b = -2 \text{ and } c = 1$$

$$\therefore b^2 - 4ac = -2^2 - 4(1)(1)$$

$$= 4 - 4$$

$$= 0$$

$\therefore b^2 - 4ac = 0$  . hence, roots are real and equal.

**Q. 7 A. Solve the following quadratic equation.**

$$\frac{1}{x+5} = \frac{1}{x^2}$$

**Answer :**

$$x^2 = x + 5$$

$$\Rightarrow x^2 - x - 5 = 0$$

$$\Rightarrow x^2 - x - 5 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 1, b = -1 \text{ and } c = -5$$

$$\therefore b^2 - 4ac = -1^2 - 4(1)(-5)$$

$$= 1 + 20$$

$$= 21$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow x = \frac{1 \pm \sqrt{21}}{2 \times 1}$$

$$\Rightarrow x = \frac{1 \pm \sqrt{21}}{2}$$

$$\Rightarrow x = \frac{1 + \sqrt{21}}{2} \text{ or } x = \frac{1 - \sqrt{21}}{2}$$

**Q. 7 B. Solve the following quadratic equation.**

$$x^2 - \frac{3x}{10} - \frac{1}{10} = 0$$

**Answer :**

$$10x^2 - 3x - 1 = 0$$

$$\Rightarrow 10x^2 - 3x - 1 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 10, b = -3 \text{ and } c = -1$$

$$\therefore b^2 - 4ac = -3^2 - 4(10)(-1)$$

$$= 9 + 40$$

$$= 49$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow x = \frac{3 \pm \sqrt{49}}{2 \times 10}$$

$$\Rightarrow x = \frac{3 \pm 7}{20}$$

$$\Rightarrow x = \frac{3+7}{20} \text{ or } x = \frac{3-7}{20}$$

$$\Rightarrow x = \frac{10}{20} \text{ or } x = \frac{-4}{20}$$

$$\Rightarrow x = \frac{1}{2} \text{ or } x = -\frac{1}{5}$$

**Q. 7 C. Solve the following quadratic equation.**

$$(2x + 3)^2 = 25$$

**Answer :**

$$4x^2 + 12x + 9 - 25 = 0 \Rightarrow 4x^2 + 12x - 16 = 0$$

$$\Rightarrow x^2 + 3x - 4 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 1, b = 3 \text{ and } c = -4$$

$$\therefore b^2 - 4ac = 3^2 - 4(1)(-4)$$

$$= 9 + 16$$

$$= 25$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow x = \frac{-3 \pm \sqrt{25}}{2 \times 1}$$

$$\Rightarrow x = \frac{-3 \pm 5}{2}$$

$$\Rightarrow x = \frac{-3 + 5}{2} \text{ or } x = \frac{-3 - 5}{2}$$

$$\Rightarrow x = \frac{2}{2} \text{ or } x = \frac{-8}{2}$$

$$\Rightarrow x = 1 \text{ or } x = -4$$

**Q. 7 D. Solve the following quadratic equation.**

$$m^2 + 5m + 5 = 0$$

**Answer :**

$$\Rightarrow m^2 + 5m + 5 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 1, b = 5 \text{ and } c = 5$$

$$\therefore b^2 - 4ac = 5^2 - 4(1)(5)$$

$$= 25 - 20$$

$$= 5$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow x = \frac{-5 \pm \sqrt{5}}{2 \times 1}$$

$$\Rightarrow x = \frac{-5 \pm \sqrt{5}}{2}$$

$$\Rightarrow x = \frac{-5 + \sqrt{5}}{2} \text{ or } x = \frac{-5 - \sqrt{5}}{2}$$

**Q. 7 E. Solve the following quadratic equation.**

$$5m^2 + 2m + 1 = 0$$

**Answer :**

$$\Rightarrow 5m^2 + 2m + 1 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 5, b = 2 \text{ and } c = 1$$

$$\therefore b^2 - 4ac = 2^2 - 4(5)(1)$$

$$= 4 - 20$$

$$= -16$$

Hence, roots are not real.

**Q. 7 F. Solve the following quadratic equation.**

$$x^2 - 4x - 3 = 0$$

**Answer :**

$$\Rightarrow x^2 - 4x - 3 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = 1, b = -4 \text{ and } c = -3$$

$$\therefore b^2 - 4ac = -4^2 - 4(1)(-3)$$

$$= 16 + 12$$

$$= 28$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow x = \frac{4 \pm \sqrt{28}}{2 \times 1}$$

$$\Rightarrow x = \frac{4 \pm 2\sqrt{7}}{2}$$

$$\Rightarrow x = \frac{4 + 2\sqrt{7}}{2} \text{ or } x = \frac{4 - 2\sqrt{7}}{2}$$

$$\Rightarrow x = \frac{2(2 + \sqrt{7})}{2} \text{ or } x = \frac{2(2 - \sqrt{7})}{2}$$

$$\Rightarrow x = 2 + \sqrt{7} \text{ or } x = 2 - \sqrt{7}$$

**Q. 8. Find m if  $(m-12)x^2 + 2(m-12)x + 2 = 0$  has real and equal roots.**

**Answer :**

$$\Rightarrow (m-12)x^2 - (2m-24)x + 2 = 0 \text{ compare with } ax^2 + bx + c = 0$$

$$\Rightarrow a = m - 12, b = -2m + 24 \text{ and } c = 2$$

$$\therefore b^2 - 4ac = (-2m + 24)^2 - 4(m-12)(2)$$

$$= 4m^2 - 96m + 576 - 8m + 96$$

$$= 4m^2 - 104m + 672$$



$$= m^2 - 26m + 168$$

If roots are equal and real then,  $\therefore b^2 - 4ac = 0$

$$m^2 - 26m + 168 = 0$$

$$\Rightarrow m^2 - 12m - 14m + 168 = 0$$

$$\Rightarrow m(m - 12) - 14(m - 12) = 0$$

$$\Rightarrow (m - 12)(m - 14) = 0$$

$$m = 12 \text{ or } m = 14$$

**Q. 9. The sum of two roots of a quadratic equation is 5 and sum of their cubes is 35, find the equation.**

**Answer :**

$$\alpha + \beta = 5$$

$$\Rightarrow \alpha^3 + \beta^3 = 35$$

$$\therefore \alpha^3 + \beta^3 = (\alpha + \beta)(\alpha^2 - \alpha\beta + \beta^2)$$

$$\Rightarrow 35 = 5(\alpha^2 + \beta^2 + 2\alpha\beta - 3\alpha\beta)$$

$$\Rightarrow 35 = 5\{(\alpha + \beta)^2 - 3\alpha\beta\}$$

$$\Rightarrow 7 = 25 - 3\alpha\beta$$

$$\Rightarrow 3\alpha\beta = 18$$

$$\Rightarrow \alpha\beta = 6$$

$$x^2 - (\alpha + \beta)x + \alpha\beta \Rightarrow x^2 - 5x + 6 = 0$$

**Q. 10. Find quadratic equation such that its roots are square of sum of the roots and square of difference of the roots of equation**

$$2x^2 + 2(p + q)x + p^2 + q^2 = 0$$

**Answer :**

Let's assume roots are m and n.

So, we want the equation whose roots would be  $(m + n)^2$  and  $(m - n)^2$

So, the sum of the roots of our desired equation would be  $2(m + n)^2$  and product of the roots would be  $(m + n)^2(m - n)^2$

What we know from given equation are:

$$m + n = -(p + q)$$

$$\text{and } mn = \frac{p^2 + q^2}{2}$$

the sum and product are:

$$\begin{aligned} s &= 2(m^2 + n^2) = 2(m + n)^2 - 2mn \\ &= 2(p + q)^2 - (p^2 + q^2) = 2 \times 2pq = 4pq \end{aligned}$$

and

$$\begin{aligned} P &= (m + n)^2(m - n)^2 \\ &= (p + q)^2(m + n)^2 - 4mn \\ &= (p + q)^2(p + q)^2 - 2(p^2 + q^2) \\ &= (p + q)^2(2pq - p^2 - q^2) \\ &= -(p + q)^2(p - q)^2 \end{aligned}$$

$$= -(p^2 - q^2)^2$$

Our desired equation would be  $x^2 - sx + P = 0$

So,  $x^2 - 4pqx - (p^2 - q^2)^2 = 0$  is our desired equation

**Q. 11. Mukund possesses ₹50 more than what Sagar possesses. The product of the amount they have is 15,000. Find the amount each one has.**

**Answer :** Let Sagar has  $x$  amount

Mukund's amount =  $x + 50$

$$x(x + 50) = 15000$$

$$\Rightarrow x^2 + 50x - 15000 = 0$$

Splitting the middle term we get:-

$$\Rightarrow x^2 - 100x + 150x - 15000 = 0$$

$\Rightarrow x(x - 100) + 150(x - 100) \Rightarrow (x - 100)(x + 150) \therefore x = (-150)$ ,  $100x = 100$  as money cant be negative therefore we ignore  $(-150) \therefore$  Sagar has 100Rs and Mukund has 150Rs

**Q. 12. The difference between squares of two numbers is 120. The square of smaller number is twice the greater number. Find the numbers.**

**Answer :** Let the two numbers be  $a$  and  $b$ , such that,  $a > b$ .

As per the given conditions,

The difference of the square of the two numbers is 120.

$$a^2 - b^2 = 120 \dots I$$

The square of smaller number is 2 times the larger number.

$$b^2 = 2a \dots II$$

Put the value of  $b^2$  from eq. II in Eq. I, it gives

$$a^2 - 2a = 120$$

$$a^2 - 2a - 120 = 0$$

$$\Rightarrow a^2 + 10a - 12a - 120 = 0$$

$$\Rightarrow a(a + 10) - 12(a + 10) = 0$$

$$\Rightarrow (a + 10)(a - 12) = 0$$

$$a + 10 = 0 \text{ or } a - 12 = 0$$

$$a = -10 \text{ or } a = 12$$

$$b = \sqrt{2a} \Rightarrow b = \sqrt{2(12)} \Rightarrow b = \sqrt{24}$$

$$b = \pm\sqrt{24}$$

$$12 \text{ and } \sqrt{24} \text{ or } 12 \text{ and } -\sqrt{24}$$

**Q. 13. Ranjana wants to distribute 540 oranges among some students. If 30 students were more each would get 3 oranges less. Find the number of students.**

**Answer :** Total oranges = 540

Initial student = x

Initial orange for 1 student = n

$$nx = 540$$

$$(n - 3)(x + 30) = 540$$

$$nx = (n - 3)(x + 30)$$

$$nx = nx + 30n - 3x - 90$$

$$30n = 3x + 90$$

$$x = \frac{30n - 90}{3}$$

$$x = 10n - 30$$

$$\therefore nx = 540$$

$$n(10n - 30) = 540$$

$$n(n - 3) = 54$$

$$n^2 - 3n - 54 = 0$$

$$n^2 - 9n + 6n - 54 = 0$$

$$n(n - 9) + 6(n - 9) = 0$$

$$(n - 9)(n + 6) = 0$$

$$\Rightarrow n - 9 = 0 \text{ or } n + 6 = 0$$

$$\Rightarrow n = 9 \text{ or } n = -6 (\because$$

$$nx = 540 \Rightarrow x = \frac{540}{9} \Rightarrow x = 60$$

$\therefore$  number of students = 60 students.

**Q. 14. Mr. Dinesh owns an agricultural farm at village Talvel. The length of the farm is 10 meter more than twice the breadth. In order to harvest rain water, he dug a square shaped pond inside the farm. The side of pond is  $\frac{1}{3}$  of the breadth of the farm. The area of the farm is 20 times the area of the pond. Find the length and breadth of the farm and of the pond.**

**Answer :**

Let the breadth of the farm be  $x$ .

$$\therefore \text{length of the farm} = 2x + 10$$

$$\text{side of the pond} = \frac{x}{3}$$

According to the question,

$$\text{area of farm} = 20(\text{area of pond})$$

$$\Rightarrow x(2x + 10) = 20 \left(\frac{x}{3}\right)^2$$

$$\Rightarrow 2x^2 + 10x = \frac{20x^2}{9}$$

$$\Rightarrow 10x = \frac{20x^2}{9} - 2x^2$$

$$\Rightarrow 10x = \frac{20x^2 - 18x^2}{9}$$

$$\Rightarrow 90x = 2x^2 \Rightarrow 2x^2 - 90x$$

$$\Rightarrow x(2x - 90) = 0$$

$$\Rightarrow x = 0 \text{ or } 2x - 90 = 0$$

$$x = \frac{90}{2} = 45$$

$$\therefore \text{length of the farm} = 2x + 10 = 2(45) + 10 = 100$$

$$\text{side of the pond} = \frac{x}{3} = \frac{45}{3} = 15$$

Breadth 45 m. length 100 m, side of the pond 15 m.

**Q. 15. A tank fills completely in 2 hours if both the taps are open. If only one of the taps is open at the given time, the smaller tap takes 3 hours more than the larger one to fill the tank. How much time does each tap take to fill the tank completely?**

**Answer :**

Let the time taken by larger tap alone be  $x$  hr. Then ,

Time taken by smaller tap be  $x + 3$  hr

In an hour, the larger tap can fill  $\frac{1}{x}$  tank.

∴ In an hour, the larger tap can fill  $\frac{1}{x+3}$  tank.

Two taps together can fill a tank in 2 hr.

But in an hour, taps fill in  $\frac{1}{2}$  hr of the tank.

$$\therefore \frac{1}{x} + \frac{1}{x+3} = \frac{1}{2}$$

$$\Rightarrow 2(x + 3 + x) = x(x + 3)$$

$$\Rightarrow 4x + 6 = x^2 + 3x$$

$$\Rightarrow x^2 + 3x - 4x - 6 = 0$$

$$\Rightarrow x^2 - x - 6 = 0$$

$$\Rightarrow x^2 - 3x + 2x - 6 = 0$$

$$\Rightarrow x(x - 3) + 2(x - 3) = 0$$

$$\Rightarrow (x - 3)(x + 2) = 0$$

$$x - 3 = 0 \text{ or } x + 2 = 0$$

$$x = 3 \text{ or } x = -2$$

$x = 3$  because time taken cannot be negative

For larger tap 3 hours and for smaller tap 6 hours.