## Statistics

## Practice Set 6.1

Q. 1. The following table shows the number of students and the time they utilized daily for their studies. Find the mean time spent by students for their studies by direct method.

| Time (hrs.) | $0-2$ | $2-4$ | $4-6$ | $6-8$ | $8-10$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 7 | 18 | 12 | 10 | 3 |

## Answer:

| Time | Class mark $\left(\mathrm{x}_{\mathrm{i}}\right)$ | No of students $\left(\mathrm{f}_{\mathrm{i}}\right)$ | $\mathrm{x}_{\mathrm{i}} \times \mathrm{f}_{\mathrm{i}}$ |
| :---: | :---: | :---: | :---: |
| $0-2$ | 1 | 7 | 7 |
| $2-4$ | 3 | 18 | 54 |
| $4-6$ | 5 | 12 | 60 |
| $6-8$ | 7 | 10 | 70 |
| $8-10$ | 9 | 3 | 27 |
| Total |  | $\sum \mathrm{f}_{\mathrm{i}}=50$ | $\sum \mathrm{x}_{\mathrm{i}} \times \mathrm{f}_{\mathrm{i}}=218$ |

$$
\Rightarrow \text { Mean }=\overline{\mathrm{x}}=\frac{\sum \mathrm{x}_{\mathrm{i}} \times \mathrm{f}_{\mathrm{i}}}{\sum \mathrm{f}_{\mathrm{i}}}=\frac{218}{50}=4.36
$$

$\Rightarrow$ Mean $\overline{\mathrm{x}}=4.36$
Q. 2. In the following table, the toll paid by drivers and the number of vehicles is shown. Find the mean of the toll by 'assumed mean' method.

| Toll | $300-400$ | $400-500$ | $500-600$ | $600-700$ | $700-800$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of drivers | 80 | 110 | 120 | 70 | 40 |

## Answer:

| Time | Class <br> mark $\left(x_{i}\right)$ | $p_{i}=x_{i}-A$ <br> $p_{i}=x_{i}-550$ | $p_{i}=\frac{d_{i}}{100}$ | No of <br> Drivers ( $\left.f_{i}\right)$ | $p_{i} \times f_{i}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $300-400$ | 350 | -200 | -2 | 80 | -160 |
| $400-500$ | 450 | -100 | -1 | 110 | -110 |
| $500-600$ | $550=A$ | 0 | 0 | 120 | 0 |
| $600-700$ | 650 | 100 | 1 | 70 | 70 |
| $700-800$ | 750 | 200 | 2 | 40 | 80 |
| Total |  |  |  | $\sum f_{i}=420$ | $\sum p_{i} \times f_{i}=-120$ |

$\Rightarrow$ Mean $=\bar{p}=\frac{\sum p_{\mathrm{i}} \times \mathrm{f}_{\mathrm{i}}}{\sum \mathrm{f}_{\mathrm{i}}}=\frac{-120}{420}=-0.2857$
$\Rightarrow \mathrm{p}^{-} \times 100=-28.57$
$\Rightarrow$ Mean $\overline{\mathrm{x}}=\mathrm{A}+100 \overline{\mathrm{p}}$
$\Rightarrow \overline{\mathrm{x}}=550+(-28.57)$
$\Rightarrow$ Mean $\overline{\mathrm{x}}=521.43$

Mean toll is Rs 521.43
Q. 3. A milk centre sold milk to 50 customers. The table below gives the number of customers and the milk they purchased. Find the mean of the milk sold by direct method.

| Milk Sold (Litre) | $1-2$ | $2-3$ | $3-4$ | $4-5$ | $5-6$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of Customers | 17 | 13 | 10 | 7 | 3 |

## Answer :

| Milk sold | Class mark $\left(\mathrm{x}_{\mathrm{i}}\right)$ | No of customers $\left(\mathrm{f}_{\mathrm{i}}\right)$ | $\mathrm{x}_{\mathrm{i}} \times \mathrm{f}_{\mathrm{i}}$ |
| :---: | :---: | :---: | :---: |
| $1-2$ | 1.5 | 17 | 25.5 |
| $2-3$ | 2.5 | 13 | 32.5 |
| $3-4$ | 3.5 | 10 | 35 |
| $4-5$ | 4.5 | 7 | 31.5 |
| $5-6$ | 5.5 | 3 | 16.5 |
| Total |  | $\sum f_{i}=50$ | $\sum x_{i} \times f_{i}=141$ |

$\Rightarrow$ Mean $=\overline{\mathrm{x}}=\frac{\sum \mathrm{x}_{\mathrm{i}} \times \mathrm{f}_{\mathrm{i}}}{\sum \mathrm{f}_{\mathrm{i}}}=\frac{141}{50}=2.82$ litre
$\Rightarrow$ Mean $\overline{\mathrm{x}}=2.82$ litre

Mean of the milk sold is 2.82 litre
Q. 4. A frequency distribution table for the production of oranges of some farm owners is given below. Find the mean production of oranges by 'assumed mean' method.

| Production <br> (Thousand rupees) | $25-30$ | $30-35$ | $35-40$ | $40-45$ | $45-50$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of farm owners | 20 | 25 | 15 | 10 | 10 |

## Answer:

| Production | Class mark $\left(\mathrm{x}_{\mathrm{i}}\right)$ | $\mathrm{p}_{\mathrm{i}}=\mathrm{x}_{\mathrm{i}}-\mathrm{A}$ <br> $\mathrm{p}_{\mathrm{i}}=\mathrm{x}_{\mathrm{i}}-37.5$ | No of Owners <br> $\left(\mathrm{f}_{\mathrm{i}}\right)$ | $\mathrm{p}_{\mathrm{i}} \times \mathrm{f}_{\mathrm{i}}$ |
| :---: | :---: | :---: | :---: | :---: |
| $25-30$ | 27.5 | -10 | 20 | -200 |
| $30-35$ | 32.5 | -5 | 25 | -125 |
| $35-40$ | $37.5=\mathrm{A}$ | 0 | 15 | 0 |
| $40-45$ | 42.5 | 5 | 10 | 50 |
| $45-50$ | 47.5 | 10 | 10 | 100 |
| Total |  |  | $\sum f_{i}=80$ | $\sum p_{i} \times f_{\mathrm{i}}=-175$ |

$\Rightarrow$ Mean $\overline{\mathrm{P}}=\frac{\sum \mathrm{p}_{\mathrm{i}} \times \mathrm{f}_{\mathrm{i}}}{\sum \mathrm{f}_{\mathrm{i}}}=\frac{-175}{80}=-2.19$

Mean $\overline{\mathrm{x}}=\overline{\mathrm{P}}+37.5$
$=37.5-2.19$
$=35.31$
$\Rightarrow$ The amount is given in thousands or rupees
$\therefore 35.31 \times 1000=\operatorname{Rs} 35130$
Q. 5. A frequency distribution of funds collected by 120 workers in a company for the drought affected people are given in the following table. Find the mean of the funds by 'step deviation' method.

| Fund (Rupees) | $0-500$ | $500-1000$ | $1000-1500$ | $1500-2000$ | $2000-2500$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of workers | 35 | 28 | 32 | 15 | 10 |

Answer:

| Fund | Class <br> $\operatorname{mark}\left(\mathrm{x}_{\mathrm{i}}\right)$ | $\mathrm{d}_{\mathrm{i}}=\mathrm{x}_{\mathrm{i}}-\mathrm{A}$ <br> $\mathrm{d}_{\mathrm{i}}=\mathrm{x}_{\mathrm{i}}-1250$ | $p_{i}=\frac{d_{\mathrm{i}}}{100}$ | No of <br> workers $\left(\mathrm{f}_{\mathrm{i}}\right)$ | $\mathrm{p}_{\mathrm{i}} \times \mathrm{f}_{\mathrm{i}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $0-500$ | 250 | -1000 | -10 | 35 | -350 |
| $500-1000$ | 750 | -500 | -5 | 28 | -140 |
| $1000-1500$ | $1250=\mathrm{A}$ | 0 | 0 | 32 | 0 |
| $1500-2000$ | 1750 | 500 | 5 | 15 | 75 |
| $2000-2500$ | 2250 | 1000 | 10 | 10 | 100 |
| Total |  |  |  | $\sum f_{i}=120$ | $\sum p_{i} \times f_{i}=315$ |

$$
\begin{aligned}
& \Rightarrow \text { Mean }=\overline{\mathrm{p}}=\frac{\sum \mathrm{p}_{\mathrm{i}} \times \mathrm{f}_{\mathrm{i}}}{\sum \mathrm{f}_{\mathrm{i}}}=\frac{-315}{120}=-2.625 \\
& \Rightarrow \overline{\mathrm{P}} \times 100=-262.5
\end{aligned}
$$

$$
\Rightarrow \text { Mean } \overline{\mathrm{x}}=\mathrm{A}+100 \overline{\mathrm{p}}
$$

$\Rightarrow \overline{\mathrm{x}}=1250-262.5$
$\Rightarrow \overline{\mathrm{x}}=987.5$

## $\therefore$ Mean of the funds is Rs 987.5

Q. 6. The following table gives the information of frequency distribution of weekly wages of 150 workers of a company. Find the mean of the weekly wages by 'step deviation' method.

| Weekly wages (Rupees) | $1000-2000$ | $2000-3000$ | $3000-4000$ | $4000-5000$ |
| :---: | :---: | :---: | :---: | :---: |
| No. of workers | 25 | 45 | 50 | 30 |

## Answer :

| Fund | Class <br> $\operatorname{mark}\left(\mathrm{x}_{\mathrm{i}}\right)$ | $p_{i}=\frac{d_{i}}{100}$ | No of workers <br> $\left(\mathrm{f}_{\mathrm{i}}\right)$ | $\mathrm{p}_{\mathrm{i}} \times \mathrm{f}_{\mathrm{i}}$ |
| :---: | :---: | :---: | :---: | :---: |
| $1000-2000$ | 1500 | 15 | 25 | 375 |
| $2000-3000$ | 2500 | 25 | 45 | 1125 |
| $3000-4000$ | 3500 | 35 | 50 | 1750 |
| $4000-5000$ | 4500 | 45 | 30 | 1350 |
| Total |  |  | $\sum f_{i}=150$ | $\sum p_{i} \times f_{i}=4600$ |

Mean $=\overline{\mathrm{p}}=\frac{\sum \mathrm{p}_{\mathrm{i}} \times \mathrm{f}_{\mathrm{i}}}{\sum \mathrm{f}_{\mathrm{i}}}=\frac{4600}{150}=30.6667$
$\Rightarrow \overline{\mathrm{P}} \times 100=3066.677$
$\Rightarrow$ Mean $\overline{\mathrm{x}}=100 \overline{\mathrm{p}}$
$\Rightarrow \overline{\mathrm{x}}=3066.67$
$\therefore$ Mean of weekly wages is Rs 3066.67

## Practice Set 6.2

Q. 1. The following table shows classification of number of workers and the number of hours they work in a software company. Find the median of the number of hours they work.

| Daily No. of hours | $8-10$ | $10-12$ | $12-14$ | $14-16$ |
| :---: | :---: | :---: | :---: | :---: |
| Number of workers | 150 | 500 | 300 | 50 |

## Answer:

| Daily hours <br> Class | No of workers <br> $\left(\mathrm{f}_{\mathrm{i}}\right)$ | Cumulative frequency <br> less than(cf) |
| :---: | :---: | :---: |
| $8-10$ | 150 | 150 |
| $10-12$ | 500 | 650 |
| $12-14$ | 300 | 950 |
| $14-16$ | 50 | 1000 |

$\Rightarrow \mathrm{N}=1000$
$\frac{\mathrm{N}}{2}=500$
$\Rightarrow 500$ Lies in class 10-12
$\Rightarrow$ Median class 10-12
$L=$ lower limit of median class $=10$
$\mathrm{N}=$ sum of frequencies $=1000$
$\mathrm{h}=$ class interval of median class $=2$
$\mathrm{f}=$ frequency of median class $=500$
cf $=$ cumulative frequency of class preceding median class $=150$
$\Rightarrow$ Median $=\mathrm{L}+\left[\frac{\frac{\mathrm{N}}{2}-\mathrm{cf}}{\mathrm{f}}\right] \times \mathrm{h}$
$\Rightarrow$ Median $=10+\left[\frac{500-150}{500}\right] \times 2$
$\Rightarrow$ Median $=11.4$
Q. 2. The frequency distribution table shows the number of mango trees in a grove and their yield of mangoes. Find the median of data.

| No. of Mangoes | $50-100$ | $100-150$ | $150-200$ | $200-250$ | $250-300$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No.of trees | 33 | 30 | 90 | 80 | 17 |

## Answer:

| No of mangoes <br> Class | No of trees <br> $\left(\mathrm{f}_{\mathrm{i}}\right)$ | Cumulative frequency <br> less than(cf) |
| :---: | :---: | :---: |
| $50-100$ | 33 | 33 |
| $100-150$ | 30 | 63 |
| $150-200$ | 90 | 153 |
| $200-250$ | 80 | 233 |
| $250-300$ | 17 | 250 |

$\Rightarrow \mathrm{N}=250$
$\frac{\mathrm{N}}{2}=125$
$\Rightarrow 125$ Lies in class 100-150
$\Rightarrow$ Median class 100-150
$L=$ lower limit of median class $=100$
$\mathrm{N}=$ sum of frequencies $=250$
$h=$ class interval of median class $=50$
$f=$ frequency of median class $=30$
$\mathrm{cf}=$ cumulative frequency of class preceding median class $=33$

$$
\begin{aligned}
& \Rightarrow \text { Median }=\mathrm{L}+\left[\frac{\frac{\mathrm{N}}{2}-\mathrm{cf}}{\mathrm{f}}\right] \times \mathrm{h} \\
& \begin{aligned}
\Rightarrow \text { Median }= & 100+\left[\frac{\frac{250}{2}-33}{30}\right] \times 50 \\
& \Rightarrow 100+\left[\frac{125-33}{30}\right] \times 50
\end{aligned} \\
& \Rightarrow \text { Median }=253.33
\end{aligned}
$$

Q. 3. The following table shows the classification of number of vehicles and their speeds on Mumbai-Pune express way. Find the median of the data.

| Average Speed of <br> Vehicles (Km/hr) | $60-64$ | $64-69$ | $69-74$ | $75-79$ | $79-84$ | $84-89$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of vehicles | 10 | 34 | 55 | 85 | 10 | 6 |

## Answer:

The class is discontinuous between 69-74 and 75-79
Converting the to continuous class

| Avg speed <br> Class | Continuous <br> class | No of trees <br> $\left(f_{i}\right)$ | Cumulative frequency <br> less than(cf) |
| :---: | :---: | :---: | :---: |
| $60-64$ | $59.5-64.5$ | 10 | 10 |
| $64-69$ | $64.5-69.5$ | 34 | 44 |
| $69-74$ | $69.5-74.5$ | 55 | 99 |
| $75-79$ | $74.5-79.5$ | 85 | 184 |
| $79-84$ | $79.5-84.5$ | 10 | 194 |
| $84-89$ | $84.5-89.5$ | 6 | 200 |

$\Rightarrow \mathrm{N}=200$
$\frac{\mathrm{N}}{2}=100$
$\Rightarrow 100$ Lies in class 74.5-79.5
$\Rightarrow$ Median class 74.5-79.5
$L=$ lower limit of median class $=74.5$
$\mathrm{N}=$ sum of frequencies $=200$
$\mathrm{h}=$ class interval of median class $=5$
$f=$ frequency of median class $=85$
cf $=$ cumulative frequency of class preceding median class $=99$
$\Rightarrow$ Median $=\mathrm{L}+\left[\frac{\frac{\mathrm{N}}{2}-\mathrm{cf}}{\mathrm{f}}\right] \times \mathrm{h}$
$\Rightarrow$ Median $=75+\left[\frac{100-99}{85}\right] \times 5$
$\Rightarrow$ Median $=74.558$
Q. 4. The production of electric bulbs in different factories is shown in the following table. Find the median of the productions.

| No. of bulbs <br> Produced (Thusands) | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of factories | 12 | 35 | 20 | 15 | 8 | 7 | 8 |

## Answer:

| No of bulbs <br> Class | No of factories <br> $\left(\mathrm{f}_{\mathrm{i}}\right)$ | Cumulative frequency <br> less than(cf) |
| :---: | :---: | :---: |
| $30-40$ | 12 | 12 |
| $40-50$ | 35 | 47 |
| $50-60$ | 20 | 67 |
| $60-70$ | 15 | 82 |
| $70-80$ | 8 | 90 |
| $80-90$ | 7 | 97 |
| $90-100$ | 8 | 105 |

$\Rightarrow \mathrm{N}=105$
$\frac{\mathrm{N}}{2}=52.5$
$\Rightarrow 52.5$ Lies in class 50-60
$\Rightarrow$ Median class 50-60
$\mathrm{L}=$ lower limit of median class $=50$
$\mathrm{N}=$ sum of frequencies $=105$
$h=$ class interval of median class $=10$
$\mathrm{f}=\mathrm{frequency}$ of median class $=20$
$\mathrm{cf}=$ cumulative frequency of class preceding median class $=47$

## Practice Set 6.3

Q. 1. The following table shows the information regarding the milk collected from farmers on a milk collection centre and the content of fat in the milk, measured by a lactometer. Find the mode of fat content.

| Content of fat (\%) | $2-3$ | $3-4$ | $4-5$ | $5-6$ | $6-7$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Milk collected (Litre) | 30 | 70 | 80 | 60 | 20 |

## Answer :

| Content of fat (\%) | Milk collected (Litre) |
| :---: | :---: |
| $2-3$ | 30 |
| $3-4$ | $70-\mathrm{f}_{0}$ |
| $4-5$ | $80-\mathrm{f}_{1}$ |
| $5-6$ | $60-\mathrm{f}_{2}$ |
| $6-7$ | 20 |

$\Rightarrow$ Maximum amount of milk collected in class 4-5
$\Rightarrow 4-5$ is modal class
$\mathrm{L}=$ lower limit of modal class $=4$
$h=$ class interval of modal class $=1$
$\mathrm{f}_{1}=$ frequency of modal class $=80$
$\mathrm{f}_{2}=$ frequency of class succeeding modal class $=60$
$\mathrm{f}_{0}=$ frequency of class preceding modal class $=70$
$\Rightarrow$ Mode $=\mathrm{L}+\left[\frac{\mathrm{f}_{1}-\mathrm{f}_{\mathrm{o}}}{2 \mathrm{f}_{1}-\mathrm{f}_{0}-\mathrm{f}_{2}}\right] \times \mathrm{h}$
$\Rightarrow$ Mode $=4+\left[\frac{80-70}{2 \times 80-70-60}\right] \times 1$
$\Rightarrow$ Mode $=4+\left[\frac{10}{30}\right] \times 1$
$\Rightarrow$ Mode $=4.33$ litre
Q. 2. Electricity used by some families is shown in the following table. Find the mode for use of electricity.

| Use of electricity (Unit) | $0-20$ | $20-40$ | $40-60$ | $60-80$ | $80-100$ | $100-120$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of families | 13 | 50 | 70 | 100 | 80 | 17 |

Answer :

| Use of electricity <br> (Unit) | No. of families |
| :---: | :---: |
| $0-20$ | 13 |
| $20-40$ | 50 |
| $40-60$ | $70-\mathrm{f}_{0}$ |
| $60-80$ | $100-\mathrm{f}_{1}$ |
| $80-100$ | $80-\mathrm{f}_{2}$ |
| $100-120$ | 17 |

$\Rightarrow$ Maximum amount of Electricity in class 60-80
$\Rightarrow 60-80$ is modal class
$\mathrm{L}=$ lower limit of modal class $=60$
$\mathrm{h}=$ class interval of modal class $=20$
$f_{1}=$ frequency of modal class $=100$
$\mathrm{f}_{2}=$ frequency of class succeeding modal class $=80$
$\mathrm{f}_{0}=$ frequency of class preceding modal class $=70$
$\Rightarrow$ Mode $=L+\left[\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}}\right] \times h$
$\Rightarrow$ Mode $=60+\left[\frac{100-70}{2 \times 100-70-80}\right] \times 20$
$\Rightarrow$ Mode $=60+\left[\frac{30}{50}\right] \times 20$
$\Rightarrow$ Mode $=72$ families
Q. 3. Grouped frequency distribution of supply of milk to hotels and the number of hotels is given in the following table. Find the mode of the supply of milk.

| Milk (Litre) | $1-3$ | $3-5$ | $5-7$ | $7-9$ | $9-11$ | $11-13$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of hotels | 7 | 5 | 15 | 20 | 35 | 18 |

## Answer:

| Milk (Litre) | No of hotels |
| :---: | :---: |
| $1-3$ | 7 |
| $3-5$ | 5 |
| $5-7$ | 15 |
| $7-9$ | $20-\mathrm{f}_{0}$ |
| $9-11$ | $35-\mathrm{f}_{1}$ |
| $11-13$ | $18-\mathrm{f}_{2}$ |

$\Rightarrow$ Maximum amount of Electricity in class 9-11
$\Rightarrow 9-11$ is modal class
$L=$ lower limit of modal class $=9$
$\mathrm{h}=$ class interval of modal class $=2$
$f_{1}=$ frequency of modal class $=35$
$\mathrm{f}_{2}=$ frequency of class succeeding modal class $=18$
$\mathrm{f}_{0}=$ frequency of class preceding modal class $=20$
$\Rightarrow$ Mode $=L+\left[\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}}\right] \times h$
$\Rightarrow$ Mode $=9+\left[\frac{35-20}{2 \times 35-18-20}\right] \times 2$
$\Rightarrow$ Mode $=9+\left[\frac{15}{32}\right] \times 2$
$\Rightarrow$ Mode $=9.94$ hotels
Q. 4. The following frequency distribution table gives the ages of 200 patients treated in a hospital in a week. Find the mode of ages of the patients.

| Age (Years) | Less than 5 | $5-9$ | $10-14$ | $15-19$ | $20-24$ | $25-29$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of patients | 38 | 32 | 50 | 36 | 24 | 20 |

## Answer:

| Age (years) |  | No of patients |
| :---: | :---: | :---: |
| $0-4$ | $-0.5-4.5$ | 38 |
| $5-9$ | $4.5-9.5$ | $32-\mathrm{f}_{0}$ |
| $10-14$ | $9.5-14.5$ | $50-\mathrm{f}_{1}$ |
| $15-19$ | $14.5-19.5$ | $36-\mathrm{f}_{2}$ |
| $20-24$ | $19.5-24.5$ | 24 |
| $25-29$ | $24.5-29.5$ | 20 |

$\Rightarrow$ Maximum amount of Electricity in class 9.5-14.5
$\Rightarrow 9.5-14.5$ is modal class
$\mathrm{L}=$ lower limit of modal class $=9.5$
$\mathrm{h}=$ class interval of modal class $=5$
$\mathrm{f}_{1}=$ frequency of modal class $=50$
$\mathrm{f}_{2}=$ frequency of class succeeding modal class $=36$
$f_{0}=$ frequency of class preceding modal class $=32$
$\Rightarrow$ Mode $=L+\left[\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}}\right] \times h$
$\Rightarrow$ Mode $=9.5+\left[\frac{50-32}{2 \times 50-36-32}\right] \times 5$
$\Rightarrow$ Mode $=9.5+\left[\frac{18}{32}\right] \times 5$
$\Rightarrow$ Mode $=12.31$ years
Mode age of the patient 12.31 years

## Practice Set 6.4

Q. 1. Draw a histogram of the following data.

| Height of student (cm) | $135-140$ | $140-145$ | $145-150$ | $150-155$ |
| :---: | :---: | :---: | :---: | :---: |
| No. of students | 4 | 12 | 16 | 8 |

## Answer :


Q. 2. The table below shows the yield of jowar per acre. Show the data by histogram.

| Yields per acre (quintal) | $2-3$ | $4-5$ | $6-7$ | $8-9$ | $10-11$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of farmers | 30 | 50 | 55 | 40 | 20 |

## Answer:

| Continuous class | $1.5-3.5$ | $3.5-5.5$ | $5.5-7.5$ | $7.5-9.5$ | $9.5-11.5$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| frequency | 30 | 50 | 55 | 40 | 20 |


Q. 3. In the following table, the investment made by 210 families is shown. Present it in the form of a histogram.

| Investment <br> (Thousand Rupees) | $10-15$ | $15-20$ | $20-25$ | $25-30$ | $30-35$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of families | 30 | 50 | 60 | 55 | 15 |

Answer :

Q. 4. Time alloted for the preparation of an examination by some students is shown in the table. Draw a histogram to show the information.

| Time (minutes) | $60-80$ | $80-100$ | $100-120$ | $120-140$ | $140-160$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 14 | 20 | 24 | 22 | 16 |

## Answer :



## Practice Set 6.5

Q. 1. Observe the following frequency polygon and write the answers of the questions below it.


Marks
fig 6.6
(1) Which class has the maximum number of students?
(2) Write the classes having zero frequency.
(3) What is the class-mark of the class, having frequency of 50 students?
(4) Write the lower and upper class limits of the class whose class mark is 85.
(5) How many students are in the class 80-90?

Answer :
(1) Class 60-70 has maximum number of students
(2) Class 20-30 and class 90-100 have zero frequency
(3) Frequency 50 students is for class 50-60

Class mark for this class is 55
(4) Class mark is 85 for class $80-90$

Lower limit $=80$
Upper limit $=90$
(5) There are 15 students in class 80-90
Q. 2. Show the following data by a frequency polygon.

| Electricity bill (Rs) | $0-200$ | $200-400$ | $400-600$ | $600-800$ | $800-1000$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Families | 240 | 300 | 450 | 350 | 160 |

## Answer:


Q. 3. The following table shows the classification of percentages of marks of students and the number of students. Draw a frequency polygon from the table.

| Result <br> (Percentage) | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 7 | 33 | 45 | 65 | 47 | 18 | 5 |

## Answer :



## Practice Set 6.6

Q. 1. The age group and number of persons, who donated blood in a blood donation camp is given below. Draw a pie diagram from it.

| Age group (Yrs) | $20-25$ | $25-30$ | $30-35$ | $35-40$ |
| :---: | :---: | :---: | :---: | :---: |
| No. of persons | 80 | 60 | 35 | 25 |

Answer : Let us find the measures of central angles and show them in a table.
Know that,
Measures of central angles $=\frac{\text { No. of persons }}{\text { Total number of persons }} \times 360^{\circ}$

| Age group <br> (yrs) | No. of <br> persons | Measure of central <br> angles |
| :---: | :---: | :---: |
| $20-25$ | 80 | $\frac{80}{200} \times 360^{\circ}=144^{\circ}$ |
| $25-30$ | 60 | $\frac{60}{200} \times 360^{\circ}=108^{\circ}$ |
| $30-35$ | 35 | $\frac{35}{200} \times 360^{\circ}=63^{\circ}$ |
| $35-40$ | 25 | $\frac{25}{200} \times 360^{\circ}=45^{\circ}$ |
| Total | 200 | $360^{\circ}$ |

Now we shall show the table into a pie chart.

Q. 2. The marks obtained by a student in different subjects are shown. Draw a pie diagram showing the information.

| Subject | English | Marathi | Science | Mathematics | Social <br> science | Hindi |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Marks | 50 | 70 | 80 | 90 | 60 | 50 |

Answer : Let us find the measures of central angles and show them in a table.
Know that,
Measures of central angles $=\frac{\text { Marks }}{\text { Total Marks }} \times 360^{\circ}$

| Subject | Marks | Measure of central <br> angles |
| :---: | :---: | :---: |
| English | 50 | $\frac{50}{400} \times 360^{\circ}=45^{\circ}$ |
| Marathi | 70 | $\frac{70}{400} \times 360^{\circ}=63^{\circ}$ |
| Science | 80 | $\frac{80}{400} \times 360^{\circ}=72^{\circ}$ |
| Mathematics | 90 | $\frac{90}{400} \times 360^{\circ}=81^{\circ}$ |
| Social <br> Science | 60 | $\frac{60}{400} \times 360^{\circ}=54^{\circ}$ |
| Hindi | 50 | $\frac{50}{400} \times 360^{\circ}=45^{\circ}$ |
| Total | 400 | $360^{\circ}$ |

Now we shall show the table into a pie chart.

Q. 3. In a tree plantation programme, the number of trees planted by students of different classes is given in the following table. Draw a pie diagram showing the information.

| Standard | 5 th | 6 th | 7 th | 8 th | 9 th | 10 th |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of trees | 40 | 50 | 75 | 50 | 70 | 75 |

## Answer :

Let us find the measures of central angles and show them in a table.
Know that,

$$
\text { Measures of central angles }=\frac{\text { No. of trees }}{\text { Total number of trees }} \times 360^{\circ}
$$

| Standard | No. of <br> trees | Measure of central angles |
| :---: | :---: | :---: |
| $5^{\text {th }}$ | 40 | $\frac{40}{360} \times 360^{\circ}=40^{\circ}$ |
| $6^{\text {th }}$ | 50 | $\frac{50}{360} \times 360^{\circ}=50^{\circ}$ |
| $7^{\text {th }}$ | 75 | $\frac{75}{360} \times 360^{\circ}=75^{\circ}$ |
| $8^{\text {th }}$ | 50 | $\frac{50}{360} \times 360^{\circ}=50^{\circ}$ |
| $9^{\text {th }}$ | 70 | $\frac{70}{360} \times 360^{\circ}=70^{\circ}$ |
| $10^{\text {th }}$ | 75 | $\frac{75}{360} \times 360^{\circ}=75^{\circ}$ |
| Total | 360 | $360^{\circ}$ |

Now we shall show the table into a pie chart.

Q. 4. The following table shows the percentages of demands for different fruits registered with a fruit vendor. Show the information by a pie diagram.

| Fruits | Mango | Sweet line | Apples | Cheeku | Oranges |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Percentages <br> of demand | 30 | 15 | 25 | 20 | 10 |

Answer : Let us find the measures of central angles and show them in a table.

Know that,
Measures of central angles $=\frac{\text { Percentages of demand }}{\text { Total percentages of demand }} \times 360^{\circ}$

| Fruits | Percentages <br> of demand | Measure of central angles |
| :---: | :---: | :---: |
| Mango | 30 | $\frac{30}{100} \times 360^{\circ}=108^{\circ}$ |
| Sweetline | 15 | $\frac{15}{100} \times 360^{\circ}=54^{\circ}$ |
| Apples | 25 | $\frac{25}{100} \times 360^{\circ}=90^{\circ}$ |
| Cheeku | 20 | $\frac{20}{100} \times 360^{\circ}=72^{\circ}$ |
| Oranges | 10 | $\frac{10}{100} \times 360^{\circ}=36^{\circ}$ |
| Total | 100 | $360^{\circ}$ |

Now we shall show the table into a pie chart.

Q. 5. The pie diagram in figure 6.13 shows the proportions of different workers in a town.

Answer the following questions with its help.
(1) If the total workers is 10,000; how many of them are in the field of construction?
(2) How many workers are working in the administration?
(3) What is the percentage of workers in production?

fig 6.13
Answer : (1) Given: total number of workers $=10000$
And central angle for number of workers in construction $=72^{\circ}$
And we know that,
Central angle for workers in construction

$$
=\frac{\text { No. of workers in construction }}{\text { Total number of workers }} \times 360^{\circ}
$$

No. of workers in construction $=$
$\Rightarrow \frac{\text { Central angle for workers in construction } \times \text { Total no.of workers }}{360^{\circ}}$
$\Rightarrow$ No. of workers in construction $=\frac{72^{\circ} \times 10000}{360^{\circ}}$
$\Rightarrow$ No. of workers in construction $=2000$
Thus, number of workers in the field of construction $=2000$.
(2) We know that,

Central angle for workers in admin $=\frac{\text { No. of workers in admin }}{\text { Total number of workers }} \times 360^{\circ}$
$\Rightarrow$ No. of workers in admin $=\frac{\text { Central angle for workers in admin } \times \text { Total no.of workers }}{360^{\circ}}$
$\Rightarrow$ No. of workers in admin $=\frac{36^{\circ} \times 10000}{360^{\circ}}$
$\Rightarrow$ No. of workers in admin $=1000$
Thus, number of workers working in administration =1000
(3) First, let us find the number of workers working in production.

We know that,
Central angle for workers in production $=\frac{\text { No. of workers in production }}{\text { Total number of workers }} \times 360^{\circ}$
$\Rightarrow$ No. of workers in production $=\frac{\text { Central angle for workers in production } \times \text { Total no.of workers }}{360^{\circ}}$
$\Rightarrow$ No. of workers in production $=\frac{90^{\circ} \times 10000}{360^{\circ}}$
$\Rightarrow$ No. of workers in production $=2500$
In terms of percentage,
Percentage of workers in production $=\frac{\text { No. of workers in production }}{\text { Total no. of workers }} \times 100$
Percentage of workers in production $=\frac{\text { No. of workers in production }}{\text { Total no. of workers }} \times 100$
$\Rightarrow$ Percentage of workers in production $=\frac{2500}{10000} \times 100$

Thus, percentage of workers in production $=\mathbf{2 5 \%}$
Q. 6. The annual investments of a family are shown in the adjacent pie diagram. Answer the following questions based on it.
(1) If the investment in shares is Rs 2000/, find the total investment.
(2) How much amount is deposited in bank?
(3) How much more money is invested in immovable property than in mutual fund?
(4) How much amount is invested in post?

fig 6.14

## Answer:

(1) Given: Investment in shares = Rs. 2000

And central angle for investment in shares $=60^{\circ}$
And we know that,

$$
\text { Central angle for investment in shares }=\frac{\text { Investment in shares }}{\text { Total investment }} \times 360^{\circ}
$$

$$
\Rightarrow \text { Total investment }=\frac{\text { Investment in shares }}{\text { Central angle for investment in shares }} \times 360^{\circ}
$$

$$
\Rightarrow \text { Total investment }=\frac{2000}{60^{\circ}} \times 360^{\circ}
$$

$$
\Rightarrow \text { Total investment }=12000
$$

Thus, total investment is Rs. 12000.
(2) We know that, total investment = Rs. 12000

Central angle for deposits in banks $=90^{\circ}$

And we know that,
Central angle for deposits in bank $=\frac{\text { Deposits in bank }}{\text { Total investment }} \times 360^{\circ}$
$\Rightarrow$ Deposits in bank $=\frac{\text { Central angle for deposits in bank } \times \text { Total investment }}{360^{\circ}}$
$\Rightarrow$ Deposits in bank $=\frac{90^{\circ} \times 12000}{360^{\circ}}$
$\Rightarrow$ Deposits in bank $=3000$
Thus, deposits in bank is Rs. 3000.
(3) Firstly, let us find money invested in immovable property.

We know that, total investment = Rs. 12000
Central angle for investment in immovable property $=120^{\circ}$
And we know that,
Central angle for investment in immovable property

$$
=\frac{\text { Investment in immovable property }}{\text { Total investment }} \times 360^{\circ}
$$

Investment in immovable property $=$
$\Rightarrow \frac{\text { Central angle for investment in immovable property } \times \text { Total investment }}{360^{\circ}}$
$\Rightarrow$ Investment in immovable property $=\frac{120^{\circ} \times 12000}{360^{\circ}}$
$\Rightarrow$ Investment in immovable property $=4000$
Now, let us find money invested in mutual fund.
We know that, total investment = Rs. 12000
Central angle for investment in mutual fund $=60^{\circ}$

And we know that,
Central angle for investment in mutual fund $=\frac{\text { Investment in mutual fund }}{\text { Total investment }} \times 360^{\circ}$
$\Rightarrow$ Investment in mutual fund $=\frac{\text { Central angle for investment in mutual fund } \times \text { Total investment }}{360^{\circ}}$
$\Rightarrow$ Investment in mutual fund $=\frac{60^{\circ} \times 12000}{360^{\circ}}$
$\Rightarrow$ Investment in mutual fund $=2000$
Subtract (ii) from (i),
The additional money invested in immovable property than mutual fund $=$ (Investment in immovable property) - (Investment in mutual fund)
$=4000-2000$
$=2000$
Thus, Rs. 2000 more money is invested in immovable property than mutual fund.
(4) We know that, total investment = Rs. 12000

Central angle for investment in post $=30^{\circ}$
And we know that,
Central angle for investment in post $=\frac{\text { Investment in post }}{\text { Total investment }} \times 360^{\circ}$
$\Rightarrow$ Investment in post $=\frac{\text { Central angle for investment in post } \times \text { Total investment }}{360^{\circ}}$
$\Rightarrow$ Investment in post $=\frac{30^{\circ} \times 12000}{360^{\circ}}$
$\Rightarrow$ Investment in post $=1000$
Thus, investment in post is Rs. 1000.

## Miscellaneous Problems 6

Q. 1 A. Find the correct answer from the alternatives given.

The persons of O- blood group are 40\%. The classification of persons based on blood groups is to be shown by a pie diagram. What should be the measures of angle for the persons of $\mathbf{O}$ - blood group?
A. $114^{\circ}$
B. $140^{\circ}$
C. $104^{\circ}$
D. $144^{\circ}$

Answer : Given is, percentage of persons of O-blood group $=40 \%$
$\Rightarrow$ Sample of persons of O-blood group $=40$
\& Total sample of persons $=100$
( $\because, 40 / 100$ implies that out of 100 samples, 40 are persons of O-blood group)
And we know,
Central angle for persons of O - blood group

$$
=\frac{\text { Sample of persons of } 0-\text { blood group }}{\text { Total sample of persons }} \times 360^{\circ}
$$

$\Rightarrow$ Central angle for persons of $0-$ blood group $=\frac{40}{100} \times 360^{\circ}$
$\Rightarrow$ Central angle for persons of O- blood group $=144^{\circ}$
Thus, the correct option is (D).
Q. 1 B . Find the correct answer from the alternatives given.

Different expenditures incurred on the construction of a building were shown by a pie diagram. The expenditure Rs 45,000 on cement was shown by a sector of central angle of $75^{\circ}$. What was the total expenditure of the construction?
A. 2,16,000
B. 3,60,000
C. 4,50,000
D. 7,50,000

Answer : The pie diagram shows, the central angle for expenditure on cement $=75^{\circ}$

Also, expenditure on cement $=$ Rs. 45,000
We know that,
Central angle for expenditure on cement

$$
=\frac{\text { Expenditure on cement }}{\text { Total expenditure on the contruction }} \times 360^{\circ}
$$

$\Rightarrow$ Total expenditure on the construction $=\frac{\text { Expenditure on cement }}{\text { Central angle for expenditure on cement }} \times 360^{\circ}$
$\Rightarrow$ Total expenditure on the construction $=\frac{45000}{75^{\circ}} \times 360^{\circ}$
$\Rightarrow$ Total expenditure on the construction $=216000$
Thus, the correct option is (A).
Q. 1 C . Find the correct answer from the alternatives given.

Cumulative frequencies in a grouped frequency table are useful to find ...
A. Mean
B. Median
C. Mode
D. All of these

Answer : The cumulative frequency of a set of data or class intervals of a frequency table is the sum of the frequencies of the data up to a required level. It can be used to determine the number of items that have values below a particular level.

Mean is simple or arithmetic average of a range of values or quantities, computed by dividing the total of all values by the number of values. And The mode of a set of data values is the value that appears most often.

While, median is the middle value of the set of ordered data. The position of the median is given by $\{(\mathrm{n}+1) / 2\}^{\text {th }}$ value, where n is the number of values in a set of data.

So, the formula can be applied in the cumulative frequency in an arranged data to find the median.

Thus, $(B)$ is the correct option.

## Q. 1 D. Find the correct answer from the alternatives given.

The formula to find mean from a grouped frequency table is
$\bar{x}=A \frac{\sum f_{i} u_{i}}{\sum f_{i}} \times h g$
In the formula $\mathbf{u}_{i}=$ $\qquad$
A. $\frac{X_{1}+A}{g}$
B. $(x-A$
C. $\frac{X_{1}-A}{g}$
D. $\frac{A-X_{i}}{g}$

Answer : Among the given option, $\left(X_{i}-A\right) / g$ is the correct option.
Where $X_{i}=$ values in the given data corresponding to $i^{\text {th }}$ position.
$A=$ Assumed mean
$g$ = class size
Thus, (C) is the correct option.
Q. 1 E. Find the correct answer from the alternatives given.

| Distance Covered per litre (km) | $12-14$ | $14-16$ | $16-18$ | $18-20$ |
| :---: | :---: | :---: | :---: | :---: |
| No. of cars | 11 | 12 | 20 | 7 |

The median of the distances covered per litre shown in the above data is in the group.....
A. 12-14
B. 14-16
C. $16-18$
D. 18-20

## Answer:

| Distance <br> $(\mathrm{km})$ | No. of <br> cars (f) | Cumulative <br> frequency (cf) |
| :---: | :---: | :---: |
| $12-14$ | 11 | 11 |
| $14-16$ | 12 | $\mathbf{2 3}$ |
| $16-18$ | $\mathbf{2 0}$ | 43 |
| $18-20$ | 7 | 50 |

Here, $(\mathrm{n} / 2)^{\text {th }}=(50 / 2)^{\text {th }}=25^{\text {th }}$ term
$c f=23<25 \Rightarrow$ Median class $=16-18$
Median class is the next class of interval of cumulative frequency.
Thus, option (C) is correct.
Q. 1 F. Find the correct answer from the alternatives given.

| No. of trees planted by each student | $1-3$ | $4-6$ | $7-9$ | $10-12$ |
| :---: | :---: | :---: | :---: | :---: |
| No. of students | 7 | 8 | 6 | 4 |

The above data is to be shown by a frequency polygon. The coordinates of the points to show number of students in the class 4-6 are . . . .
A. $(4,8)$
B. $(3,5)$
C. $(5,8)$
D. $(8,4)$

Answer : First, draw a table converting the given class into continuous class.

| Class | Continuous <br> Class | Class <br> mark | Frequency |
| :---: | :---: | :---: | :---: |
| $1-3$ | $0.5-3.5$ | 2 | 7 |
| $4-6$ | $3.5-6.5$ | 5 | 8 |
| $7-9$ | $6.5-9.5$ | 8 | 6 |
| $10-12$ | $9.5-12.5$ | 11 | 4 |

Drawing it into a frequency polygon.


| Class | Continuous <br> Class | Class <br> mark | Frequency | Coordinate |
| :---: | :---: | :---: | :---: | :---: |
| $1-3$ | $0.5-3.5$ | 2 | 7 | $(2,7)$ |
| $4-6$ | $3.5-6.5$ | 5 | 8 | $(5,8)$ |
| $7-9$ | $6.5-9.5$ | 8 | 6 | $(8,6)$ |
| $10-12$ | $9.5-12.5$ | 11 | 4 | $(11,4)$ |

So, the coordinates of the points to show number of students in the class 4-6 are $(5,8)$.
Thus, option (C) is correct.
Q. 2. The following table shows the income of farmers in a grape season. Find the mean of their income.

| Income <br> (Thousand Rupees) | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Farmers | 10 | 11 | 15 | 16 | 18 | 14 |

## Answer :

| Class <br> (Income in <br> Rs. 1000 ) | Class Mark <br> $x_{i}$ | Frequency <br> (farmers) <br> $f_{i}$ | Class Mark $\times$ <br> Frequency <br> $x_{i} f_{i}$ |
| :---: | :---: | :---: | :---: |
| $20-30$ | 25 | 10 | 250 |
| $30-40$ | 35 | 11 | 385 |
| $40-50$ | 45 | 15 | 675 |
| $50-60$ | 55 | 16 | 880 |
| $60-70$ | 65 | 18 | 1170 |
| $70-80$ | 75 | 14 | 1050 |
| TOTAL |  | $\Sigma \mathrm{f}_{\mathrm{i}}=84$ | $\Sigma \mathrm{xif}_{\mathrm{i}}=4410$ |

Mean is given by
Mean $=\frac{\sum \mathrm{x}_{\mathrm{i}} \mathrm{f}_{\mathrm{i}}}{\sum \mathrm{f}_{\mathrm{i}}}$
$\Rightarrow$ Mean $=4410 / 84$
$\Rightarrow$ Mean $=52.5$

Now, since the income is given in thousand rupees.
Then, Mean $=52.5 \times 1000$
$\Rightarrow$ Mean $=52500$

Thus, mean income is Rs. 52,500.
Q. 4. The weekly wages of 120 workers in a factory are shown in the following frequency distribution table. Find the mean of the weekly wages.

| Weekly wages <br> (Rupees) | $0-2000$ | $2000-4000$ | $4000-6000$ | $6000-8000$ |
| :---: | :---: | :---: | :---: | :---: |
| No. of workers | 15 | 35 | 50 | 20 |

## Answer :

| Class <br> (Weekly wages <br> in Rs.) | Class Mark <br> $\mathrm{x}_{\mathrm{i}}$ | Frequency <br> (No. of workers) <br> $\mathrm{f}_{\mathrm{i}}$ | Class Mark $\times$ <br> Frequency <br> $\mathrm{x}_{\mathrm{i}} \mathrm{f}_{\mathrm{i}}$ |
| :---: | :---: | :---: | :---: |
| $0-2000$ | 1000 | 15 | 15000 |
| $2000-4000$ | 3000 | 35 | 105000 |
| $4000-6000$ | 5000 | 50 | 250000 |
| $6000-8000$ | 7000 | 20 | 140000 |
| TOTAL |  | $\Sigma \mathrm{f}_{\mathrm{i}}=120$ | $\sum \mathrm{x}_{\mathrm{i}} \mathrm{f}_{\mathrm{i}}=510000$ |

Mean is given by
Mean $=\frac{\sum \mathrm{x}_{\mathrm{i}} \mathrm{f}_{\mathrm{i}}}{\sum \mathrm{f}_{\mathrm{i}}}$
$\Rightarrow$ Mean $=510000 / 120$
$\Rightarrow$ Mean $=4250$
Thus, mean weekly wages is Rs. 4250.
Q. 5. The following frequency distribution table shows the amount of aid given to 50 flood affected families. Find the mean of the amount of aid.

| Amount of aid <br> (Thosand rupees) | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of families | 7 | 13 | 20 | 6 | 4 |

## Answer :

| Class <br> (Amount of aid <br> in Rs. 1000 ) | Class Mark <br> $x_{i}$ | Frequency <br> (No. of families) <br> $f_{i}$ | Class Mark $\times$ <br> Frequency <br> $x_{i} f_{i}$ |
| :---: | :---: | :---: | :---: |
| $50-60$ | 55 | 7 | 385 |
| $60-70$ | 65 | 13 | 845 |
| $70-80$ | 75 | 20 | 1500 |
| $80-90$ | 85 | 6 | 510 |
| $90-100$ | 95 | 4 | 380 |
| TOTAL |  | $\Sigma f_{i}=50$ | $\Sigma x_{i} f_{i}=3620$ |

Mean is given by

Mean $=\frac{\sum \mathrm{x}_{\mathrm{i}} \mathrm{f}_{\mathrm{i}}}{\sum \mathrm{f}_{\mathrm{i}}}$
$\Rightarrow$ Mean $=3620 / 50$
$\Rightarrow$ Mean $=72.4$
Now, since the amount of aid is given in thousand rupees.
Then, Mean $=72.4 \times 1000$
$\Rightarrow$ Mean $=72400$
Thus, mean amount of aid is Rs. 72,400.
Q. 6. The distances covered by 250 public transport buses in a day is shown in the following frequency distribution table. Find the median of the distances.

| Distance (km) | $200-210$ | $210-220$ | $220-230$ | $230-240$ | $240-250$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of buses | 40 | 60 | 80 | 50 | 20 |

Answer : Let us prepare cumulative frequency table:

| Class <br> (Distance in <br> km ) | Frequency <br> (No. of buses) <br> F | Cumulative <br> frequency <br> cf |
| :---: | :---: | :---: |
| $200-210$ | 40 | 40 |
| $210-220$ | 60 | 100 |
| $220-230$ | 80 | 180 |
| $230-240$ | 50 | 230 |
| $240-250$ | 20 | 250 |

Here, $\mathrm{N}=250$
$\mathrm{N} / 2=250 / 2=125$
Since, cumulative frequency 180 is just greater than $125 . \Rightarrow$ median class $=220-230$ Median is given by

Median $=\mathrm{L}+\left[\frac{\frac{\mathrm{N}}{2}-\mathrm{cf}}{\mathrm{f}}\right] \times \mathrm{h}$

Where I = lower limit of the median class
$\mathrm{N}=$ Sum of frequencies
$\mathrm{h}=$ class interval of the median class
cf = Cumulative frequency of the class preceding the median class
$f=$ Frequency of the median class
Here, Median class = 220-230
$L=220$
$\mathrm{N} / 2=125$
$h=10$
cf $=100$
$\mathrm{f}=80$

Putting all these values in the median formula, we get
Median $=220+\left[\frac{125-100}{80}\right] \times 10$
$\Rightarrow$ Median $=220+250 / 80$
$\Rightarrow$ Median $=220+3.125=223.125$
Or Median is approximately 223.13 km
Thus, median of the distances is $\mathbf{2 2 3 . 1 3} \mathbf{~ k m}$.
Q. 7. The prices of different articles and demand for them is shown in the following frequency distribution table. Find the median of the prices.

| Price (Rupees) | 20 less than | $20-40$ | $40-60$ | $60-80$ | $80-100$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of articles | 140 | 100 | 80 | 60 | 20 |

Answer : Let us prepare cumulative frequency table:

| Class <br> (Price in Rs.) | Frequency <br> (No. of articles) <br> f | Cumulative <br> frequency <br> cf |
| :---: | :---: | :---: |
| $0-20$ | 140 | 140 |
| $20-40$ | 100 | 240 |
| $40-60$ | 80 | 320 |
| $60-80$ | 60 | 380 |
| $80-100$ | 20 | 400 |

Here, $N=400$
$N / 2=400 / 2=200$
Since, cumulative frequency 240 is just greater than $200 \Rightarrow$ median class $=20-40$
Median is given by
Median $=\mathrm{L}+\left[\frac{\frac{\mathrm{N}}{2}-\mathrm{cf}}{\mathrm{f}}\right] \times \mathrm{h}$
Where I = lower limit of the median class
$\mathrm{N}=$ Sum of frequencies
$\mathrm{h}=$ class interval of the median class
cf $=$ Cumulative frequency of the class preceding the median class
$f=$ Frequency of the median class
Here, Median class $=20-40$
$L=20$
$\mathrm{N} / 2=200$
$h=20$
cf $=140$
$f=100$
Putting all these values in the median formula, we get

Median $=20+\left[\frac{200-140}{100}\right] \times 20$
$\Rightarrow$ Median $=20+1200 / 100$
$\Rightarrow$ Median $=20+12=32$
Thus, median of the prices is Rs. 32.
Q. 8. The following frequency table shows the demand for a sweet and the number of customers. Find the mode of demand of sweet.

| Weight of sweet (gram) | $0-250$ | $250-500$ | $500-750$ | $750-1000$ | $1000-1250$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of customers | 10 | 60 | 25 | 20 | 15 |

Answer : Given the distribution table, notice that maximum number of customers has demand for $250-500$ grams. (Since, 60 is the maximum number of customers)

So, modal class $=250-500$
Mode is given by
Mode $=\mathrm{L}+\left[\frac{\mathrm{f}_{1}-\mathrm{f}_{0}}{2 \mathrm{f}_{1}-\mathrm{f}_{0}-\mathrm{f}_{2}}\right] \times \mathrm{h}$
Where $\mathrm{L}=$ lower class limit of the modal class
$\mathrm{h}=$ class interval of the modal class
$f_{1}=$ frequency of the modal class
$f_{0}=$ frequency of the class preceding the modal class
$\mathrm{f}_{2}=$ frequency of the class succeeding the modal class
Here, Modal class $=250-500$
$\mathrm{L}=250$
$h=250$
$\mathrm{f}_{1}=60$
$\mathrm{f}_{0}=10$
$f_{2}=25$
Putting these values in the formula,
Mode $=250+\left[\frac{60-10}{2 \times 60-10-25}\right] \times 250$
$\Rightarrow$ Mode $=250+\left[\frac{50}{85}\right] \times 250$
$\Rightarrow$ Mode $=250+147.06$
$\Rightarrow$ Mode $=397.06$
Thus, mode of demand of sweet is 397.06 grams.

## Q. 9. Draw a histogram for the following frequency distribution.

| Use of electricity <br> (Unit) | $50-70$ | $70-90$ | $90-110$ | $110-130$ | $130-150$ | $150-170$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of families | 150 | 400 | 460 | 540 | 600 | 350 |

Answer : Let values in use of electricity be $x$-values and values in no. of families be $y$ axis.


Thus, this is the histogram.
Q. 10. In a handloom factory different workers take different periods of time to weave a saree. The number of workers and their required periods are given below. Present the information by a frequency polygon.

| No. of days | $8-10$ | $10-12$ | $12-14$ | $14-16$ | $16-18$ | $18-20$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of workers | 5 | 16 | 30 | 40 | 35 | 14 |

Answer : First, draw a frequency table.

| Class | Class mark | Frequency |
| :---: | :---: | :---: |
| $8-10$ | 9 | 5 |
| $10-12$ | 11 | 16 |
| $12-14$ | 13 | 30 |
| $14-16$ | 15 | 40 |
| $16-18$ | 17 | 35 |
| $18-20$ | 19 | 14 |

Drawing it into a frequency polygon.
Frequency Polygon

Q. 11. The time required for students to do a science experiment and the number of students is shown in the following grouped frequency distribution table. Show the information by a histogram and also by a frequency polygon.

| Time required for <br> Experiment (minutes) | $20-22$ | $22-24$ | $24-26$ | $26-28$ | $28-30$ | $30-32$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 8 | 16 | 22 | 18 | 14 | 12 |

Answer : First, draw a frequency table.

| Class | Class <br> mark | Frequency |
| :---: | :---: | :---: |
| $20-22$ | 21 | 8 |
| $22-24$ | 23 | 16 |
| $24-26$ | 25 | 22 |
| $26-28$ | 27 | 18 |
| $28-30$ | 29 | 14 |
| $30-32$ | 31 | 12 |

Drawing it on a histogram.
Let time required for experiment (minutes) be x -values and number of students be y axis.

Histogram


Drawing it into a frequency polygon.

Q. 12. Draw a frequency polygon for the following grouped frequency distribution table.

| Age of donor <br> (Yrs.) | $20-24$ | $25-29$ | $30-34$ | $35-39$ | $40-44$ | $45-49$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of blood doners | 38 | 46 | 35 | 24 | 15 | 12 |

Answer : First, draw a frequency table.

| Class | Continuous <br> class | Class mark | Frequency |
| :---: | :---: | :---: | :---: |
| $20-24$ | $19.5-24.5$ | 22 | 38 |
| $25-29$ | $24.5-29.5$ | 27 | 46 |
| $30-34$ | $29.5-34.5$ | 32 | 35 |
| $35-39$ | $34.5-39.5$ | 37 | 24 |
| $40-44$ | $39.5-44.5$ | 42 | 15 |
| $45-49$ | $44.5-49.5$ | 47 | 12 |

The representation into a frequency polygon will be as such.
Frequency Polygon

Q. 13. The following table shows the average rainfall in 150 towns. Show the information by a frequency polygon.

| Average rainfall (cm) | $0-20$ | $20-40$ | $40-60$ | $60-80$ | $80-100$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of towns | 14 | 12 | 36 | 48 | 40 |

Answer: First, draw a frequency table.

| Class | Class <br> mark | Frequency |
| :---: | :---: | :---: |
| $0-20$ | 10 | 14 |
| $20-40$ | 30 | 12 |
| $40-60$ | 50 | 36 |
| $60-80$ | 70 | 48 |
| $80-100$ | 90 | 40 |

Representing the information into a frequency polygon.

Q. 14. Observe the adjacent pie diagram. It shows the percentages of number of vehicles passing a signal in a town between 8 am and 10 am
(1) Find the central angle for each type of vehicle.
(2) If the number of two-wheelers is $\mathbf{1 2 0 0}$, find the number of all vehicles.

fig 6.15
Answer : (1) To find central angle for cars:

Given that, percentage of cars passing a signal in a town $=30 \%$
$\Rightarrow$ Number of cars $=30$
\& Total number of vehicles $=100$
Central angle for cars is given by,
Central angle for cars $=\frac{\text { Number of cars }}{\text { Total number of vehicles }} \times 360^{\circ}$
$\Rightarrow$ Central angle for cars $=\frac{30}{100} \times 360^{\circ}$
$\Rightarrow$ Central angle for cars $=108^{\circ}$
Thus, central angle for cars is $108^{\circ}$.
To find central angle for tempos:
Given that, percentage of tempos passing a signal in a town $=12 \%$
$\Rightarrow$ Number of tempos $=12$
\& Total number of vehicles $=100$
Central angle for tempos is given by,
Central angle for tempos $=\frac{\text { Number of tempos }}{\text { Total number of vehicles }} \times 360^{\circ}$
$\Rightarrow$ Central angle for tempos $=\frac{12}{100} \times 360^{\circ}$
$\Rightarrow$ Central angle for tempos $=43.2^{\circ}$
By approximating, we get
Central angle for tempos $=43^{\circ}$
Thus, central angle for tempos is $43.2^{\circ}$.
To find central angle for buses:
Given that, percentage of buses passing a signal in a town $=8 \%$
$\Rightarrow$ Number of buses $=8$
\& Total number of vehicles $=100$
Central angle for buses is given by,
Central angle for buses $=\frac{\text { Number of buses }}{\text { Total number of vehicles }} \times 360^{\circ}$
$\Rightarrow$ Central angle for buses $=\frac{8}{100} \times 360^{\circ}$
$\Rightarrow$ Central angle for buses $=28.8^{\circ}$
By approximating, we get
Central angle for buses $=29^{\circ}$
Thus, central angle for buses is $29^{\circ}$.
To find central angle for auto-rikshaws:
Given that, percentage of auto-rikshaws passing a signal in a town $=10 \%$
$\Rightarrow$ Number of auto-rikshaws $=10$
\& Total number of vehicles $=100$
Central angle for auto-rikshaws is given by,
Central angle for auto - rikshaws $=\frac{\text { Number of auto }- \text { rikshaws }}{\text { Total number of vehicles }} \times 360^{\circ}$
$\Rightarrow$ Central angle for auto - rikshaws $=\frac{10}{100} \times 360^{\circ}$
$\Rightarrow$ Central angle for auto-rikshaws $=36^{\circ}$
Thus, central angle for auto-rikshaws is $36^{\circ}$.
To find central angle for two-wheelers:
Given that, percentage of two-wheelers passing a signal in a town $=40 \%$
$\Rightarrow$ Number of two-wheelers $=40$
\& Total number of vehicles $=100$
Central angle for two-wheelers is given by,
Central angle for two - wheelers $=\frac{\text { Number of two }- \text { wheelers }}{\text { Total number of vehicles }} \times 360^{\circ}$
$\Rightarrow$ Central angle for two - wheelers $=\frac{40}{100} \times 360^{\circ}$
$\Rightarrow$ Central angle for two-wheelers $=144^{\circ}$
Thus, central angle for two-wheelers is $144^{\circ}$.
Check: Add all central angles for vehicles (cars + tempos + buses + auto-rikshaws + two-wheelers) $=108^{\circ}+43^{\circ}+29^{\circ}+36^{\circ}+144^{\circ}=360^{\circ}$

Hence, it's correct.
(2). Given: Number of two-vehicles $=1200$

And central angle for two-vehicles $=144^{\circ}$ (as found in part (1))
Then,
Central angle for two - wheelers $=\frac{\text { Number of two }- \text { wheelers }}{\text { Total number of vehicles }} \times 360^{\circ}$
$\Rightarrow$ Total number of vehicles $=\frac{\text { Number of two-wheelers }}{\text { Central angle for two-vehicles }} \times 360^{\circ}$
$\Rightarrow$ Total number of vehicles $=\frac{1200}{144^{\circ}} \times 360^{\circ}$
$\Rightarrow$ Total number of vehicles $=3000$
Thus, there are total $\mathbf{3 0 0 0}$ vehicles in all.
Q. 15. The following table shows causes of noise pollution. Show it by a pie diagram.

| Construction | Traffic | Aricraft <br> take offs | Industry | Trains |
| :---: | :---: | :---: | :---: | :---: |
| $10 \%$ | $50 \%$ | $9 \%$ | $20 \%$ | $11 \%$ |

Answer : Let us find the measures of central angles and show them in a table.
Know that,
Measures of central angles $=\frac{\text { No. of scores }}{\text { Total number of scores }} \times 360^{\circ}$

| Component | Percentage (\%) | Measure of central <br> angles |
| :---: | :---: | :---: |
| Construction | 10 | $\frac{10}{100} \times 360^{\circ}=36^{\circ}$ |
| Traffic | 50 | $\frac{50}{100} \times 360^{\circ}=180^{\circ}$ |
| Aircraft <br> takeoffs | 9 | $\frac{9}{100} \times 360^{\circ}=32.4^{\circ}$ |
| Industry | 20 | $\frac{20}{100} \times 360^{\circ}=72^{\circ}$ |
| Trains | 11 | $\frac{11}{100} \times 360^{\circ}=39.6^{\circ}$ |
| Total | 100 | $360^{\circ}$ |

Now we shall show the table into a pie chart.

Q. 16. A survey of students was made to know which game they like. The data obtained in the survey is presented in the adjacent pie diagram. If the total number of students are 1000,
(1) How many students like cricket?
(2) How many students like football?
(3) How many students prefer other games?

fig 6.16
Answer : (1) Central angle for cricket $=81^{\circ}$
Total number of students $=1000$
Then,
Central angle for cricket $=\frac{\text { Number of students who like cricket }}{\text { Total number of students }} \times 360^{\circ}$
$\Rightarrow$ Number of students who like cricket $=\frac{\text { Central angle for cricket } \times \text { Total number of students }}{360^{\circ}}$
$\Rightarrow$ Number of students who like cricket $=\frac{81^{\circ} \times 1000}{360^{\circ}}$
$\Rightarrow$ Number of students who like cricket $=225$
Thus, 225 students like cricket.
(2) Central angle for football $=63^{\circ}$

Total number of students $=1000$
Then,
Central angle for football $=\frac{\text { Number of students who like football }}{\text { Total number of students }} \times 360^{\circ}$

Number of students who like football $=$
$\Rightarrow \frac{\text { Central angle for football } \times \text { Total number of students }}{360^{\circ}}$
$\Rightarrow$ Number of students who like football $=\frac{63^{\circ} \times 1000}{360^{\circ}}$
$\Rightarrow$ Number of students who like football $=175$
Thus, 175 students like football.
(3) Central angle for other games $=72^{\circ}$

Total number of students $=1000$

Then,
Central angle for other games

$$
=\frac{\text { Number of students who like other games }}{\text { Total number of students }} \times 360^{\circ}
$$

Number of students who like other games $=$
$\Rightarrow$ Central angle for other games $\times$ Total number of students $360^{\circ}$
$\Rightarrow$ Number of students who like other games $=\frac{72^{\circ} \times 1000}{360^{\circ}}$
$\Rightarrow$ Number of students who like other games $=200$
Thus, 200 students like other games.
Q. 17. Medical check up of 180 women was conducted in a health centre in a village. 50 of them were short of haemoglobin, 10 suffered from cataract and 25 had respiratory disorders. The remaining women were healthy. Show the information by a pie diagram.

Answer : First lets show it by a table.
Know that,
Measures of central angles $=\frac{\text { No. of scores }}{\text { Total number of scores }} \times 360^{\circ}$

| Component | Values | Measure of central <br> angles |
| :---: | :---: | :---: |
| Haemoglobin | 50 | $\frac{50}{180} \times 360^{\circ}=100^{\circ}$ |
| Cataract | 10 | $\frac{10}{180} \times 360^{\circ}=20^{\circ}$ |
| Respiratory <br> disorders | 25 | $\frac{25}{180} \times 360^{\circ}=50^{\circ}$ |
| Healthy | $180-(50+10+$ <br> $25)=180-85=$ <br> 95 | $\frac{95}{180} \times 360^{\circ}=190^{\circ}$ |
| Total | 180 | $360^{\circ}$ |

Now we shall show the table into a pie chart.
Pie Chart

Q. 18

# On an environment day, students in a school planted 120 trees under plantation project. The information regarding the project is shown in the following table. Show it by a pie diagram. 

| Tree name | Karanj | Behada | Arjun | Bakul | Kadunimb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of trees | 20 | 28 | 24 | 22 | 26 |

Answer :
First lets show it by a table.

Know that,

Measures of central angles $=\frac{\text { No. of trees }}{\text { Total number of trees }} \times 360^{\circ}$

| Tree name | No. of trees | Measure of central angles |
| :---: | :---: | :---: |
| Karanj | 20 | $\frac{20}{120} \times 360^{\circ}=60^{\circ}$ |
| Behada | 28 | $\frac{28}{120} \times 360^{\circ}=84^{\circ}$ |
| Arjun | 24 | $\frac{24}{120} \times 360^{\circ}=72^{\circ}$ |
| Bakul | 22 | $\frac{22}{120} \times 360^{\circ}=66^{\circ}$ |
| Kadunimb | 26 | $\frac{26}{120} \times 360^{\circ}=78^{\circ}$ |
| Total | 120 | $360^{\circ}$ |

Now we shall show the table into a pie chart.


First lets show it by a table.
Know that,
Measures of central angles $=\frac{\text { No. of trees }}{\text { Total number of trees }} \times 360^{\circ}$

| Tree name | No. of trees | Measure of central angles |
| :---: | :---: | :---: |
| Karanj | 20 | $\frac{20}{120} \times 360^{\circ}=60^{\circ}$ |
| Behada | 28 | $\frac{28}{120} \times 360^{\circ}=84^{\circ}$ |
| Arjun | 24 | $\frac{24}{120} \times 360^{\circ}=72^{\circ}$ |
| Bakul | 22 | $\frac{22}{120} \times 360^{\circ}=66^{\circ}$ |
| Kadunimb | 26 | $\frac{26}{120} \times 360^{\circ}=78^{\circ}$ |
| Total | 120 | $360^{\circ}$ |

Now we shall show the table into a pie chart.

Pie Chart


■ Karanj Behada $\quad$ Arjun Bakul $\quad$ Kadunimb

