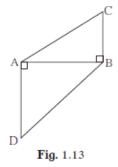
### **Practice Set 1.1**

# Q. 1. Base of a triangle is 9 and height is 5. Base of another triangle is 10 and height is 6. Find the ratio of areas of these triangles.

Answer : We know that area of triangle =  $\frac{1}{2} \times \text{Basex Height}$   $\Rightarrow \text{Area (triangle 1)} = \frac{1}{2} \times 9 \times 5$ =  $\frac{45}{2}$   $\Rightarrow \text{Area (triangle 2)} = \frac{1}{2} \times 10 \times 6$ = 30  $\therefore$  The ratio of areas of these triangles will be =  $\frac{\text{Area(triangle 1)}}{\text{Area(triangle 2)}}$ =  $\frac{\frac{45}{2}}{30}$ =  $\frac{45}{2} \times \frac{1}{30}$ =  $\frac{45}{2} \times \frac{1}{30}$ =  $\frac{3}{4}$ 

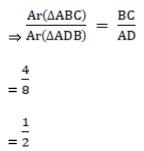
Q. 2. If figure 1.13 BC  $\perp$  AB, AD  $\perp$  AB, BC = 4, AD = 8, then find  $\frac{A(\Delta ABC)}{A(\Delta ADB)}$ 



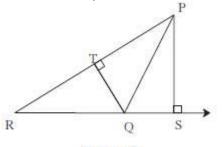
**Answer :** Here,  $\triangle ABC$  and  $\triangle ADB$  has common Base.

 $\frac{\operatorname{Ar}(\Delta ABC)}{\operatorname{Ar}(\Delta ADB)} = \frac{\operatorname{height} of \Delta ABC}{\operatorname{height} of \Delta ADB}$ 

(PROPERTY: Areas of triangles with equal bases are proportional to their corresponding heights.)

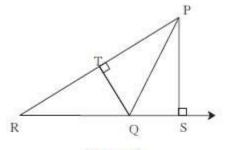


Q. 3. In adjoining figure 1.14 seg PS  $\perp$  seg RQ, seg QT  $\perp$  seg PR. If RQ = 6, PS = 6 and PR = 12, then find QT.





Answer :



**Fig. 1.14** Considering, Area of ( $\Delta$ PQR) with base QR

 $\Rightarrow$  PS will be the Height

Now, consider the Area of ( $\Delta PQR$ ) with base PR

 $\Rightarrow$  QT will be the Height

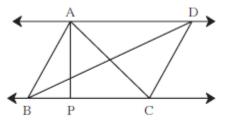
 $\therefore$  The triangle is the same

 $\Rightarrow$  The area will be the same irrespective of the base taken.

And we know that area of triangle =  $\frac{1}{2} \times \text{Base} \times \text{Height}$ 

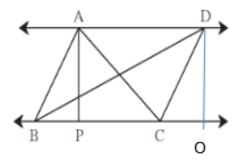
```
\Rightarrow \frac{1}{2} \times QR \times PS
= \frac{1}{2} \times PR \times QT
\Rightarrow \frac{1}{2} \times 6 \times 6
= \frac{1}{2} \times 12 \times QT
\Rightarrow QT = 3
```

Q. 4. In adjoining figure, AP  $\perp$  BC, AD || BC, then find A( $\Delta$ ABC) : A ( $\Delta$ BCD)





Answer:



We can re-draw the fig. 1.15 (as shown above) where we add DO

Which will be height of  $\Delta BCD$ .

 $\frac{A(\Delta ABC)}{A(\Delta BCD)} = \frac{AP}{DO}$ 

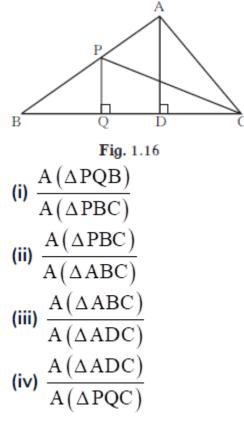
(PROPERTY: Areas of triangles with equal bases are proportional to their corresponding heights.)

 $\frac{A(\Delta ABC)}{A(\Delta BCD)} = \frac{AP}{DO}$  $\frac{A(\Delta ABC)}{A(\Delta BCD)} = \frac{1}{1}$ 

(: the distance between the two parallel lines is always equal  $\Rightarrow$  AP = DO)

 $\Rightarrow \frac{A(\Delta ABC)}{A(\Delta BCD)} = 1:1$ 

#### Q. 5. In adjoining figure PQ $\perp$ BC, AD $\perp$ BC then find following ratios.



**Answer :** We know that area of triangle =  $\frac{1}{2} \times \text{Base} \times \text{Height}$ 

 $\frac{A(\Delta PQB)}{A(\Delta PBC)} = \frac{BQ}{BC}$ 

(PROPERTY: Areas of triangles with equal heights are proportional to their corresponding bases.)

 $\frac{A(\Delta PBC)}{(ii)} = \frac{PQ}{AD}$ 

(PROPERTY: Areas of triangles with equal bases are proportional to their corresponding heights.)

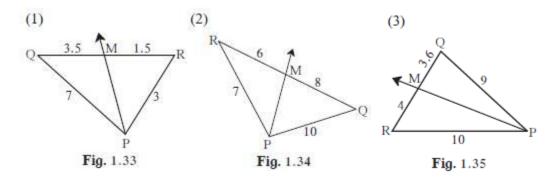
	$A(\Delta ABC)$	_	BC
(iii)	$A(\Delta ADC)$	_	DC

(PROPERTY: Areas of triangles with equal heights are proportional to their corresponding bases.)

 $\frac{A(\Delta ADC)}{(iv)} = \frac{\frac{1}{2} \times AD \times DC}{\frac{1}{2} \times PQ \times QC}$  $= \frac{AD \times DC}{PQ \times QC}$ 

#### Practice Set 1.2

Q. 1. Given below are some triangles and lengths of line segments. Identify in which figures, ray PM is the bisector of  $\angle OPR$ .



Answer :

**Theorem:** The bisector of an angle of a triangle divides the side opposite to the angle in the ratio of the remaining sides.

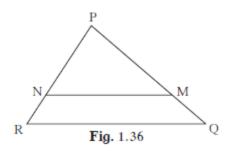
Therefore, we'll find the ratio for all the triangle. Hence, for

 $\frac{QM}{MR} = \frac{3.5}{1.5}$ = 2.33  $\operatorname{And} \frac{\operatorname{QP}}{\operatorname{PR}} = \frac{7}{3}$ = 2.33  $\frac{QM}{MR} = \frac{QP}{PR}$  $\Rightarrow$  In (1), ray PM is a bisector.  $\frac{RM}{MQ} = \frac{6}{8}$ = 0.75  $\frac{RP}{PQ} = \frac{7}{10}$ = 0.7  $\rightarrow \frac{RM}{MQ} \neq \frac{RP}{PQ}$  $\Rightarrow$  In (2), ray PM is not a bisector.  $\frac{RM}{MQ} = \frac{4}{3.6}$ = 1.1  $\frac{RP}{PQ} = \frac{10}{9}$ = 1.11

$$\stackrel{RM}{\Rightarrow} \frac{RM}{MQ} = \frac{RP}{PQ}$$

 $\Rightarrow$  In (3), ray PM is a bisector.

# Q. 2. In $\triangle$ PQR, PM = 15, PQ = 25, PR = 20, NR = 8. State whether line NM is parallel to side RQ. Give reason.



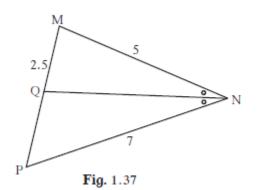
Answer : By Converse of basic Proportionality Theorem

(Theorem: If a line divides any two sides of a triangle in the same ratio, then the line is parallel to the third side.)

 $\frac{PN}{RR} = \frac{PM}{MQ}, \text{ then line NM is parallel to side RQ.}$   $\frac{PN}{RR} = \frac{PN}{NR} = \frac{PM}{MQ}.$   $\frac{PN}{RR} = \frac{PR-NR}{NR}$   $= \frac{20-8}{8}$   $= \frac{12}{8}$   $= \frac{3}{2}$   $And, \frac{PM}{MQ} = \frac{PM}{PQ-PM}$   $= \frac{15}{25-15}$ 

$=\frac{15}{10}$	
$=\frac{3}{2}$	
$\Rightarrow \frac{PN}{NR} = \frac{PM}{MQ} =$	<sup>3</sup> / <sub>2</sub> , therefore line NM    side RQ

Q. 3. In  $\triangle$  MNP, NQ is a bisector of  $\angle$ N. If MN = 5, PN = 7 MQ = 2.5 then find QP.



#### Answer :

Theorem: The bisector of an angle of a triangle divides the side opposite to the angle in the ratio of the remaining sides.

$$\frac{MQ}{QP} = \frac{MN}{NP}$$

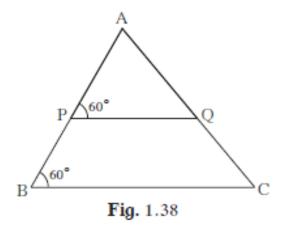
$$\frac{2.5}{QP} = \frac{5}{7}$$

$$\Rightarrow QP \times 5 = 2.5 \times 7$$

$$\Rightarrow QP = \frac{2.5 \times 7}{5}$$

$$\Rightarrow QP = 3.5$$

Q. 4. Measures of some angles in the figure are given. Prove that  $\frac{AP}{PB} = \frac{AQ}{OC}$ 



**Answer :** Here, PQ||BC ( $\because \angle APQ \cong \angle ABC$ )

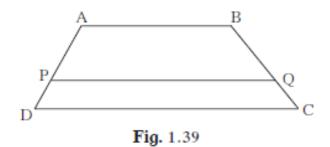
(PROPERTY: If a transversal intersects two lines so that corresponding angles are congruent, then the lines are parallel)

#### : By Basic Proportionality Theorem

(Theorem : If a line parallel to a side of a triangle intersects the remaining sides in two distinct points, then the line divides the sides in the same proportion.)

$$\stackrel{\text{AP}}{\Rightarrow} \stackrel{\text{PB}}{=} \frac{\text{AQ}}{\text{QC}}$$

Q. 5. In trapezium ABCD, side AB || side PQ || side DC, AP = 15, PD = 12, QC = 14, find BQ.

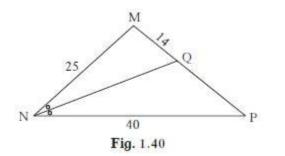


Answer : By Basic Proportionality Theorem

(Theorem : If a line parallel to a side of a triangle intersects the remaining sides in two distinct points, then the line divides the sides in the same proportion.)

$$\frac{AP}{PD} = \frac{BQ}{QC}$$
$$\Rightarrow \frac{15}{12} = \frac{BQ}{14}$$
$$\Rightarrow BQ = \frac{15 \times 14}{12}$$
$$\Rightarrow BQ = 17.5$$

Q. 6. Find QP using given information in the figure.

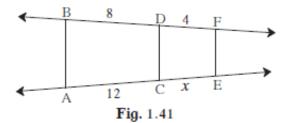


**Answer :** Theorem: The bisector of an angle of a triangle divides the side opposite to the angle in the ratio of the remaining sides.

And :: NQ is angle bisector of  $\angle N$ 

 $\frac{MQ}{\Rightarrow QP} = \frac{MN}{NP}$  $\frac{14}{\Rightarrow QP} = \frac{25}{40}$  $\Rightarrow QP = \frac{14 \times 40}{25}$  $\Rightarrow QP = 22.4$ 

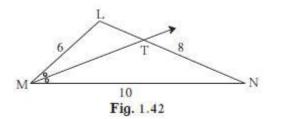
#### Q. 7. In figure 1.41, if AB || CD || FE then find x and AE.



**Answer :** Theorem: The ratio of the intercepts made on a transversal by three parallel lines is equal to the ratio of the corresponding intercepts made on any other transversal by the same parallel lines.

 $\frac{BD}{DF} = \frac{AC}{CE}$   $\Rightarrow \frac{8}{4} = \frac{12}{x}$   $\Rightarrow x = \frac{12 \times 4}{8}$   $\Rightarrow x = 6$ Now, AE = AC + CE = 12 + x = 12 + 6  $\Rightarrow AE = 18$ 

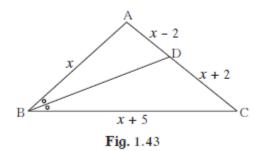
Q. 8. In  $\Delta$  LMN, ray MT bisects  $\angle$  LMN If LM = 6, MN = 10, TN = 8, then find LT.



**Answer :** Theorem: The bisector of an angle of a triangle divides the side opposite to the angle in the ratio of the remaining sides.

$$\frac{LT}{TN} = \frac{LM}{MN}$$
$$\Rightarrow LT = \frac{LM \times TN}{MN}$$
$$\Rightarrow LT = \frac{6 \times 8}{10}$$
$$\Rightarrow LT = 4.8$$

Q. 9. In  $\triangle$  ABC, seg BD bisects  $\angle$  ABC. If AB = x, BC = x + 5, AD = x - 2, DC = x + 2, then find the value of x.



**Answer :** Theorem: The bisector of an angle of a triangle divides the side opposite to the angle in the ratio of the remaining sides.

$$\frac{AD}{DC} = \frac{AB}{BC}$$

$$\Rightarrow \frac{x-2}{x+2} = \frac{x}{x+5}$$

$$\Rightarrow x(x+2) = (x-2)(x+5)$$

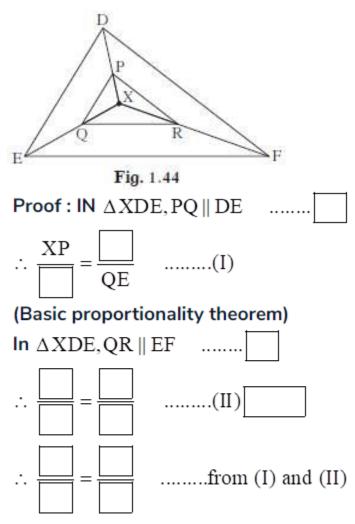
$$\Rightarrow x^{2} + 2x = x^{2} - 2x + 5x - 10$$

$$\Rightarrow x^{2} + 2x - x^{2} + 2x - 5x + 10 =$$

$$\Rightarrow x = 10$$

0

Q. 10. In the figure 1.44, X is any point in the interior of triangle. Point X is joined to vertices of triangle. Seg PQ || seg DE, seg QR || seg EF. Fill in the blanks to prove that, seg PR || seg DF.



∴ seg PR || seg DE ...... (Converse of basic proportionality theorem)

**Answer** : Proof: In ΔXDE, PQ||DE..... (Given)

 $\frac{XP}{XQ} = \frac{PD}{DE}$ ....(I)

(Basic proportionality theorem)

In ΔXDE, QR||EF .....(Given)

 $\frac{XR}{RF} = \frac{XQ}{QE}$ ....(II) (Basic Proportionality Theorem)

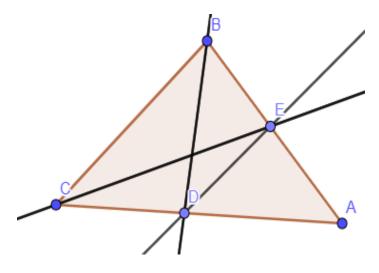
 $\frac{XP}{PD} = \frac{XR}{RF}$  ..... from (I) and (II)

∴ seg PR||Seg DE .....

(converse of basic proportionality theorem)

# Q. 11. In $\triangle ABC$ , ray BD bisects $\angle ABC$ and ray CE bisects $\angle ACB$ . If seg AB $\cong$ seg AC then prove that ED || BC.

Answer : PROOF:



Theorem: The bisector of an angle of a triangle divides the side opposite to the angle in the ratio of the remaining sides.

$$\frac{AD}{DC} = \frac{AB}{CB} \dots (1)$$
And  $\frac{AE}{EB} = \frac{AC}{CB} \dots (2)$  ( $\because$  BD and CE are angle bisectors of  $\angle B$  and  $\angle C$  respectively.)  
Now,  $\because$  seg AB  $\cong$  seg AC  
 $\Rightarrow AB = AC$   
 $\Rightarrow \frac{AB}{CB} = \frac{AC}{CB}$   
 $\Rightarrow R.H.S of (1) \& (2)$  are equal.  
 $\Rightarrow L.H.S of (1) \& (2)$  will be equal.

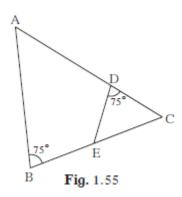
: Equating L.H.S of (1) &(2), we get-

$$\stackrel{\text{AD}}{\Rightarrow} \stackrel{\text{DC}}{\text{DC}} = \frac{\text{AE}}{\text{EB}}$$

 $\Rightarrow$  ED||BC (By converse basic proportionality theorem)

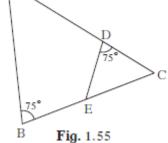
### **Practice Set 1.3**

Q. 1. In figure 1.55,  $\angle ABC = 75^\circ$ ,  $\angle EDC = 75^\circ$  state which two triangles are similar and by which test? Also write the similarity of these two triangles by a proper one to one correspondence.

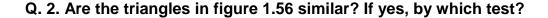


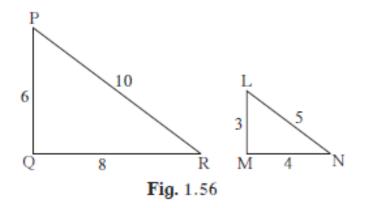
**Answer :** With one- to-one correspondence ABC  $\leftrightarrow$  EDC

 $\therefore \angle ABC \cong \angle EDC = 75^{\circ}$ ∠ACB  $\cong \angle ECD$  (Is common in both the triangles ABC and EDC)



 $\Rightarrow \Delta ABC \sim \Delta EDC \dots (By AA Test)$ 

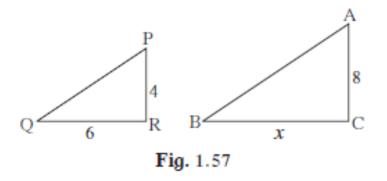




**Answer :** In  $\triangle$  PQR and  $\triangle$  LMN

 $\frac{PQ}{LM} = \frac{6}{3} = 2$   $And \frac{QR}{MN} = \frac{8}{4} = 2$   $And \frac{PR}{LN} = \frac{10}{5} = 2$   $\Rightarrow \frac{PQ}{LM} = \frac{QR}{MN} = \frac{PR}{LN} = 2$   $\Rightarrow \Delta PQR \sim \Delta LMN \dots (By SSS Similarity Test)$ 

Q. 3. As shown in figure 1.57, two poles of height 8 m and 4 m are perpendicular to the ground. If the length of shadow of smaller pole due to sunlight is 6 m then how long will be the shadow of the bigger pole at the same time?



Answer : :: The shadows are measured at the same time

 $\Rightarrow$  Angle of of elevation will be equal for both the pole

$$\Rightarrow \Delta PQR \sim \Delta ABC \dots (By AA Test)$$
$$\Rightarrow \frac{PR}{AC} = \frac{QR}{BC}$$
$$\Rightarrow BC = \frac{QR \times AC}{PR}$$
$$\Rightarrow x = \frac{6 \times 8}{4}$$
$$\Rightarrow x = 12 \text{ m}$$

Q. 4. In  $\triangle$ ABC, AP  $\perp$  BC, BQ  $\perp$  AC B- P-C, A-Q - C then prove that,  $\triangle$ CPA ~  $\triangle$ CQB. If AP = 7, BQ = 8, BC = 12 then find AC.

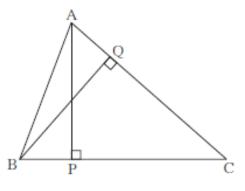


Fig. 1.58

Answer : From fig.

 $\Rightarrow \angle APC \cong \angle BQC$  (:: AP $\perp BC$  and BQ $\perp AC$ )

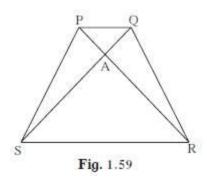
 $\Rightarrow$  Also,  $\angle$  ACP $\cong$   $\angle$  BCQ (Common)

 $\Rightarrow \Delta CPA \sim \Delta CQB$  (By AA Test)

$$\frac{AP}{BQ} = \frac{AC}{BC}$$
$$\Rightarrow AC = \frac{AP \times BC}{BQ}$$
$$\Rightarrow AC = \frac{7 \times 12}{8}$$

 $\Rightarrow AC = 10.5$ 

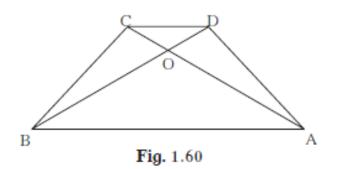
Q. 5. Given : In trapezium PQRS, side PQ || side SR, AR = 5AP, AS = 5AQ then prove that, SR = 5PQ



Answer : Given that, AR = 5AP and AS = 5AQ

 $\Rightarrow \frac{AR}{AP} = 5 \dots (1)$ And  $\frac{AS}{AQ} = 5 \dots (2)$   $\Rightarrow \frac{AR}{AP} = \frac{AS}{AQ}$ And,  $\angle SAR \cong \angle QAP \dots (Opposite angles)$   $\Rightarrow \Delta SAR \sim \Delta QAP \dots (SAS Test of similarity)$   $\Rightarrow \frac{AS}{AQ} = \frac{AR}{AP} = \frac{SR}{QP} (corresponding sides are proportional)$ But,  $\frac{AS}{AQ} = \frac{AR}{AP} = 5$   $\Rightarrow SR = 5PQ$ 

Q. 6. In trapezium ABCD, (Figure 1.60) side AB || side DC, diagonals AC and BD intersect in point O. If AB = 20, DC = 6, OB = 15 then find OD.



**Answer** : In  $\triangle$  AOB and  $\triangle$ COD

 $\Rightarrow \angle AOB \cong \angle COD$  (opposite angles)

 $\Rightarrow \angle CDO \cong \angle ABO$  (Alternate angles  $\therefore AB||DC$ )

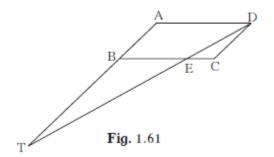
 $\Rightarrow \Delta AOB \sim \Delta COD$  (By AA Test)

 $\frac{AB}{DC} = \frac{OB}{OD}$  (corresponding sides are proportional)

 $\Rightarrow OD = \frac{OB \times DC}{AB}$  $\Rightarrow OD = \frac{15 \times 6}{20}$ 

⇒ OD = 4.5

Q. 7. ABCD is a parallelogram point E is on side BC. Line DE intersects ray AB in point T. Prove that  $DE \times BE = CE \times TE$ .



**Answer :** In  $\triangle$  CED and  $\triangle$ BET

 $\Rightarrow \angle CED \cong \angle BET$  (opposite angles)

 $\Rightarrow \angle CDE \cong \angle BTE$  (Alternate angles)

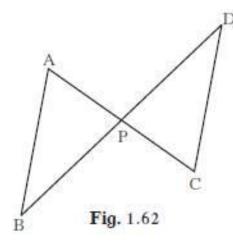
(:  $AB||DC \Rightarrow BT||DC$ , as BT is extension to AB)

 $\Rightarrow \Delta \text{ CED} \sim \Delta \text{ BET}$  (By AA Test)

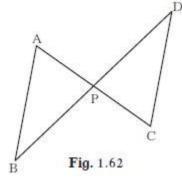
 $\frac{CE}{DE} = \frac{BE}{TE}$  (corresponding sides are proportional)

 $\Rightarrow$  DE x BE = CE x TE

Q. 8. In the figure, seg AC and seg BD intersect each other in point P and  $\frac{AP}{Cp} = \frac{BP}{DP}$ . Prove that,  $\triangle ABP \sim \triangle CDP$ 







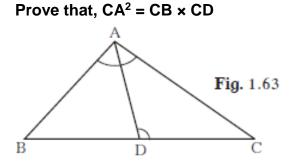
In  $\triangle$  APB &  $\triangle$  CPD

$$\Rightarrow \frac{AP}{CP} = \frac{BP}{DP} \dots (Given)$$

And,  $\angle APB = \angle DPC$  (vertically opposite angles)

 $\Rightarrow \Delta APB \sim \Delta CPD$  (By SAS Test)

Q. 9. In the figure, in  $\triangle ABC$ , point D on side BC is such that,  $\angle BAC = \angle ADC$ .



**Answer :** In  $\triangle$  BAC &  $\triangle$  ADC

 $\Rightarrow \angle BAC \cong \angle ADC \dots (Given)$ 

And,  $\angle ACB \cong \angle DCA \dots (common)$ 

 $\Rightarrow \Delta BAC \sim \Delta ADC$  (By AA Test)

 $\Rightarrow \frac{CA}{CD} = \frac{CB}{CA}$  (corresponding sides are proportional)

 $\Rightarrow$  CA<sup>2</sup> = CB × CD

#### **Practice Set 1.4**

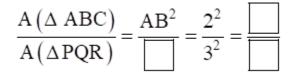
### Q. 1. The ratio of corresponding sides of similar triangles is 3 : 5; then find the ratio of their areas.

**Answer :** Theorem: When two triangles are similar, the ratio of areas of those triangles is equal to the ratio of the squares of their corresponding sides.

 $\Rightarrow$  Ratio of areas =  $3^2:5^2$ 

 $\Rightarrow$  Ratio of areas = 9 : 25

Q. 2. If  $\triangle ABC \sim \triangle PQR$  and AB: PQ = 2:3, then fill in the blanks.



**Answer :**  $\therefore \Delta$  ABC~ $\Delta$  PQR and AB:PQ = 2:3

 $\xrightarrow{A(\Delta ABC)}_{\Rightarrow \overline{A(\Delta PQR)}} = \frac{AB^2}{PQ^2} = \frac{2^2}{3^2} = \frac{4}{9}$ 

Q. 3. If  $\triangle ABC \sim \triangle PQR$ , A ( $\triangle ABC$ ) = 80, A( $\triangle PQR$ ) = 125, then fill in the blanks.

$A(\Delta ABC)$	80	_ AB _
Α(Δ)	125	PQ =

**Answer :**  $:: \Delta ABC \sim \Delta PQR$ 

 $\frac{A(\Delta ABC)}{A(\Delta PQR)} = \frac{80}{125} (:: A(\Delta PQR) = 125 \text{ is given})$   $\Rightarrow \frac{A(\Delta ABC)}{A(\Delta PQR)} = \frac{AB^2}{PQ^2}$   $\Rightarrow \frac{AB}{PQ} = \sqrt{\frac{A(\Delta ABC)}{A(\Delta PQR)}}$   $\Rightarrow \frac{AB}{PQ} = \frac{4}{5}$ 

Q. 4.  $\Delta$ LMN ~  $\Delta$ PQR, 9 × A( $\Delta$ PQR) = 16 × A ( $\Delta$ LMN). If QR = 20 then find MN.

**Answer :**  $:: \Delta ABC \sim \Delta PQR$ 

 $\Rightarrow$  Given that, 9 × A( $\triangle$  ABC) = 16× A( $\triangle$  PQR)

 $\frac{A(\Delta PQR)}{A(\Delta LMN)} = \frac{16}{9}$ 

 $\underset{\text{And, }\overline{A(\Delta \text{ PQR})}}{\text{And, }} = \frac{\text{QR}^2}{\text{MN}^2}$ 

$$\frac{QR^{2}}{MN^{2}} = \frac{16}{9}$$

$$\Rightarrow \frac{20^{2}}{MN^{2}} = \frac{16}{9}$$

$$\Rightarrow MN^{2} = \frac{400 \times 9}{16}$$

$$\Rightarrow MN = 15$$

### Q. 5. Areas of two similar triangles are 225 sq.cm & 81 sq.cm. If a side of the smaller triangle is 12 cm, then find corresponding side of the bigger triangle.

**Answer :** Let area of one(bigger) triangle be 'A', other(smaller) triangle be 'B', corresponding side of smaller triangle be 'a' and bigger triangle be 'b'.

$$\frac{A}{B} = \frac{b^2}{a^2}$$
 (By theorem)

And a = 12cm, A = 225 sq.cm, B = 81 sq.cm .....(Given)

$$\Rightarrow \frac{225}{81} = \frac{b^2}{12^2}$$
$$\Rightarrow b^2 = \frac{225 \times 144}{81}$$
$$\Rightarrow b = \sqrt{400}$$

 $\Rightarrow$  b = 20 cm

### Q. 6. $\triangle$ ABC and $\triangle$ DEF are equilateral triangles. If A( $\triangle$ ABC) : A( $\triangle$ DEF) = 1 : 2 and AB = 4, find DE.

Answer : We know that, all the angles of an equilateral triangles are equal, i.e., 60°.

 $\Rightarrow \Delta ABC \sim \Delta DEF \dots$  (By AAA Similarity Test)

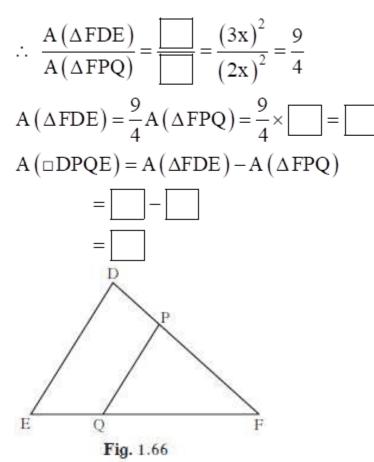
 $\frac{A(\Delta ABC)}{\Rightarrow A(\Delta DEF)} = \frac{AB^2}{DE^2}$   $\frac{A(\Delta ABC)}{And, A(\Delta DEF)} = \frac{1}{2} \text{ (Given)}$ 

 $\frac{AB^{2}}{DE^{2}} = \frac{1}{2}$   $\Rightarrow DE^{2} = 2 \times 4^{2} (\because AB = 4)$   $\Rightarrow DE = \sqrt{32}$   $\Rightarrow DE = 4\sqrt{2}$ 

Q. 7. In figure 1.66, seg PQ || seg DE, A( $\Delta$  PQF) = 20 units, PF = 2 DP, then find A(DPQE) by completing the following activity.

A( $\triangle$  PQF) = 20 units, PF = 2 DP, Let us assume DP = x.  $\therefore$  PF = 2x DF = DP +  $\square$  =  $\square$  +  $\square$  = 3x

In  $\Delta$  FDE and  $\Delta$  FPQ,  $\angle$ FDE  $\cong \angle$  ...... corresponding angles  $\angle$ FED  $\cong \angle$  ...... corresponding angles  $\therefore \Delta$  FDE  $\sim \Delta$  FPQ ...... AA test



**Answer :**  $A(\Delta PQF) = 20$  units, PF = 2DP, Let us assume DP = x,  $\therefore$  PF = 2x

 $\Rightarrow$  DF = DP + PF = x + 2x = 3x

In  $\Delta$  FDE &  $\Delta$  FPQ

 $\angle$  FDE  $\cong \angle$  FPQ (Corresponding angles)

 $\angle$  FEP  $\cong \angle$  FQP (Corresponding angles)

 $\therefore \Delta$  FDE~  $\Delta$  FPQ (AA Test)

 $\frac{A(\Delta FDE)}{A(\Delta FPQ)} = \frac{DF^2}{PF^2} = \frac{(3x)^2}{(2x)^2} = \frac{9}{4}$   $A(\Delta FDE) = \frac{9}{4}A(\Delta FPQ) = \frac{9}{4} \times 20 = 45$   $A(\Box DPQE) = A (\Delta FDE) - A(\Delta FPQ)$  = 45 - 20 = 25 sq. unit.

#### Problem Set 1

Q. 1. A. Select the appropriate alternative. In  $\triangle$  ABC and  $\triangle$ PQR, in a one to one correspondence  $\frac{AB}{QR} = \frac{BC}{PR} = \frac{CA}{PQ}$  then

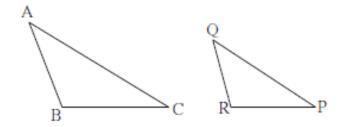


Fig. 1.67

A.  $\triangle$  PQR ~  $\triangle$  ABC

B.  $\triangle$  PQR ~  $\triangle$  CAB C.  $\triangle$  CBA ~  $\triangle$  PQR D.  $\triangle$  BCA ~  $\triangle$  PQR

Answer: 
$$\frac{AB}{QR} = \frac{BC}{PR} = \frac{CA}{PQ}$$

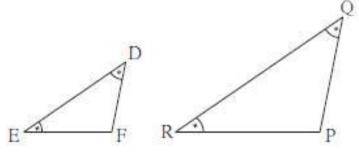
 $\Rightarrow \Delta CAB \sim \Delta PQR$ 

(A) doesn't match the solution.

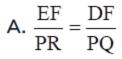
- (C) doesn't match the solution.
- (D) doesn't match the solution.

#### Q. 1. B. Select the appropriate alternative.

If in  $\triangle DEF$  and  $\triangle PQR$ ,  $\angle D \cong \angle Q$ ,  $\angle R \cong \angle E$  then which of the following statements is false?







B. 
$$\frac{DE}{PQ} = \frac{EF}{RP}$$
  
C.  $\frac{DE}{QR} = \frac{DF}{PQ}$   
D.  $\frac{EF}{RP} = \frac{DE}{QR}$ 

**Answer :** In  $\triangle$  DEF &  $\triangle$  PQR

 ${\it \angle} \ D {\cong} {\it \angle} \ Q \ and {\it \angle} \ R {\cong} {\it \angle} \ E \ (Given)$ 

 $\Rightarrow \Delta \text{ DEF} \sim \Delta \text{ PQR}$ 

 $\frac{DE}{PQ} = \frac{EF}{QR} = \frac{FD}{RP}$  (corresponding sides are proportional)

(A) Is matching the solution, hence can't be false.

(C) Is matching the solution, hence can't be false.

(D) Is matching the solution, hence can't be false.

Q. 1. C. Select the appropriate alternative.

In  $\Delta$  and  $\Delta$ DEF  $\angle$ B =  $\angle$ E,  $\angle$ F =  $\angle$ C and AB = 3DE then which of the statements regarding the two triangles is true?

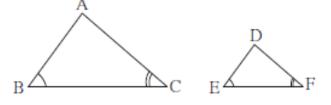


Fig. 1.69

A. The triangles are not congruent and not similar

- B. The triangles are similar but not congruent.
- C. The triangles are congruent and similar.
- D. None of the statements above is true.

**Answer :** In  $\triangle$  ABC &  $\triangle$  DEF

- $\angle B \cong \angle E$  and  $\angle C \cong \angle F$  (Given)
- $\Rightarrow \Delta ABC \sim \Delta DEF$  (By AA Test)
- $\Rightarrow$  The triangles are similar.

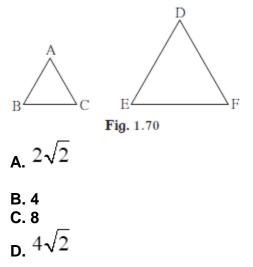
And,  $\triangle ABC \cong \triangle DEF$ , if AB = DE.

But, given that - AB = 3DE.

- $\Rightarrow$  The triangles are not congruent.
- (A) doesn't match the solution.
- (C) doesn't match the solution.
- (D) doesn't match the solution.

Q. 1. D. Select the appropriate alternative.

 $\triangle$ ABC and  $\triangle$ DEF are equilateral triangles, A( $\triangle$ ABC) : A( $\triangle$ DEF) = 1 : 2. If AB = 4 then what is length of DE?



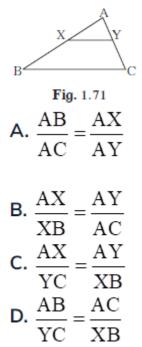
**Answer :** Solution: We know that, all the angles of an equilateral triangles are equal, i.e., 60°.

 $\Rightarrow \Delta ABC \sim \Delta DEF \dots$  (By AAA Similarity Test)

 $\frac{A(\Delta ABC)}{A(\Delta DEF)} = \frac{AB^{2}}{DE^{2}}$   $And, \frac{A(\Delta ABC)}{A(\Delta DEF)} = \frac{1}{2} \text{ (Given)}$   $\frac{AB^{2}}{\Rightarrow DE^{2}} = \frac{1}{2}$   $\Rightarrow DE^{2} = 2 \times 4^{2} (\because AB = 4)$   $\Rightarrow DE = \sqrt{32}$   $\Rightarrow DE = 4\sqrt{2}$ (A) doesn't match the solution. (B) doesn't match the solution. (C) doesn't match the solution.

#### Q. 1. E. Select the appropriate alternative.

In figure 1.71, seg XY || seg BC, then which of the following statements is true?



**Answer :**  $\because$  segXY|| segBC  $\Rightarrow \angle AXY \cong \angle ABC$ 

And,  $\angle XAY \cong \angle BAC$  (Common)

 $\Rightarrow \Delta AXY \sim \Delta ABC$  (By AA Test)

 $\frac{AX}{AB} = \frac{AY}{AC} = \frac{XY}{BC}$  (corresponding sides are proportional)

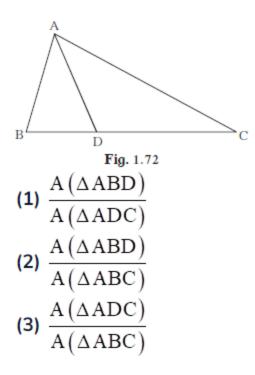
 $\stackrel{AB}{\Rightarrow} \frac{AB}{AC} = \frac{AX}{AY}$ 

(B) doesn't match the solution.

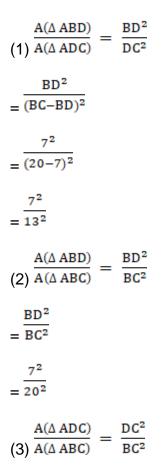
(C) doesn't match the solution.

(D) doesn't match the solution.

#### Q. 2. In $\triangle$ ABC, B - D – C and BD = 7, BC = 20 then find following ratios.



**Answer :** Theorem: When two triangles are similar, the ratio of areas of those triangles is equal to the ratio of the squares of their corresponding sides.



$$= \frac{(BC-BD)^2}{BC^2}$$
$$= \frac{(20-7)^2}{20^2}$$
$$= \frac{13^2}{20^2}$$

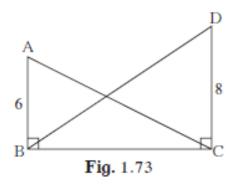
# Q. 3. Ratio of areas of two triangles with equal heights is 2 : 3. If base of the smaller triangle is 6 cm then what is the corresponding base of the bigger triangle?

**Answer :** (PROPERTY: Areas of triangles with equal heights are proportional to their corresponding bases.)

 $\frac{A(\text{smaller triangle})}{A(\text{bigger triangle})} = \frac{\text{base(smaller triangle})}{\text{base(bigger triangle})}$  $\frac{2}{3} = \frac{6}{\text{base(bigger triangle})}$ 

 $\Rightarrow$  Base (bigger triangle) = 9 cm

Q. 4. In figure 1.73,  $\angle ABC = \angle DCB = 90^{\circ} AB = 6$ , DC = 8 then  $\frac{A (\triangle ABC)}{A (\triangle DCB)}$ ?



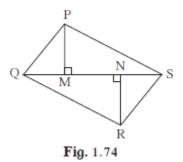
**Answer :** We know that, Area of triangle =  $\frac{1}{2} \times \text{base} \times \text{height}$ 

$$\stackrel{A(\Delta ABC)}{\Rightarrow} = \frac{\frac{1}{2} \times BC \times AB}{\frac{1}{2} \times BC \times DC}$$

 $= \frac{AB}{DC}$ 

 $=\frac{6}{8}$  $=\frac{3}{4}$ 

Q. 5. In figure 1.74, PM = 10 cm A( $\Delta$  PQS) = 100 sq.cm A ( $\Delta$ QRS) = 110 sq.cm then find NR.

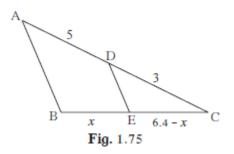


**Answer :** We know that, Area of triangle =  $\frac{1}{2} \times \text{base} \times \text{height}$ 

 $\Rightarrow \frac{A(\Delta PQS)}{A(\Delta QRS)} = \frac{\frac{1}{2} \times QS \times PM}{\frac{1}{2} \times QS \times NR}$  $\Rightarrow \frac{100}{110} = \frac{PM}{NR}$  $\Rightarrow \frac{100}{110} = \frac{10}{NR}$  $\Rightarrow NR = 11 \text{ cm}$ 

Q. 6.  $\Delta$ MNT ~  $\Delta$ QRS. Length of altitude drawn from point T is 5 and length of altitude drawn from point S is 9. Find the ratio  $\frac{A(\Delta MNT)}{A(\Delta QRS)}$ .

Answer:  $\frac{A(\Delta MNT)}{A(\Delta QRS)} = \frac{(altitude from T)^2}{(altitude frm S)^2}$ =  $\frac{5^2}{9^2}$ =  $\frac{25}{81}$  Q. 7. In figure 1.75, A – D – C and B – E – C seg DE || side AB If AD = 5, DC = 3, BC = 6.4 then find BE.

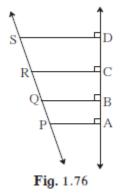


Answer : By Basic Proportionality Theorem-

 $\frac{CD}{DA} = \frac{CE}{EB}$  $\Rightarrow \frac{3}{5} = \frac{6.4 - x}{x}$  $\Rightarrow 3x = 32 - 5x$  $\Rightarrow 8x = 32$  $\Rightarrow x = 4 = BE$ 

Q. 8. In the figure 1.76, seg PA, seg QB, seg RC and seg SD are perpendicular to line AD.

AB = 60, BC = 70, CD = 80, PS = 280 then find PQ, QR and RS.



**Answer :** (PROPERTY: If line AX || line BY || line CZ and line I and line m are their transversals then)

 $\frac{AB}{BC} = \frac{XY}{YZ}$ 

$$AB = PQ = QR$$

$$AB = PQ = QR$$

$$PQ = \frac{6}{7}$$

$$PQ = \frac{6}{7}$$

$$PQ = \frac{6}{7} QR$$

$$And CD = QR = \frac{1}{7}$$

$$\frac{BC}{RS} = \frac{QR}{RS}$$

$$And CD = \frac{QR}{RS}$$

$$RS = \frac{7}{8}$$

$$RS = \frac{8}{7} QR$$

$$PS = 280$$
[2]

$$\Rightarrow$$
 PQ + QR + RS = 280 .....(3)

From [1] and [2], we have

$$\Rightarrow \frac{6}{7}QR + QR + \frac{8}{7}QR = 280$$
$$\Rightarrow \frac{14}{7}QR + QR = 280$$
$$\Rightarrow 2QR + QR = 280$$
$$\Rightarrow 3QR = 280$$
$$\Rightarrow QR = \frac{280}{3}$$

$$PQ = \frac{6}{7}QR$$

From [1]

$$\Rightarrow PQ = \frac{6}{7} \times \frac{280}{3} = 80$$
$$RS = \frac{8}{7} \times \frac{280}{3} = \frac{320}{3}$$

From [2]

Q. 9. In  $\triangle$ PQR seg PM is a median. Angle bisectors of  $\angle$ PMQ and  $\angle$ PMR intersect side PQ and side PR in points X and Y respectively. Prove that XY || QR.

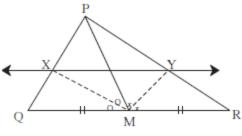
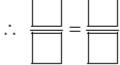
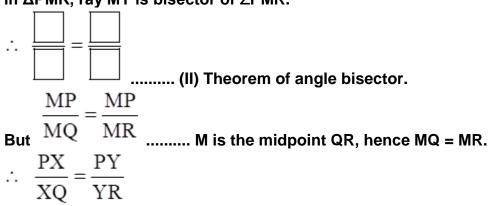


Fig. 1.77

Complete the proof by filling in the boxes. In  $\Delta PMQ$ , ray MX is bisector of  $\angle PMQ$ .





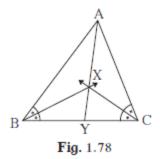
:: XY || QR ..... converse of basic proportionality theorem.

**Answer** :  $\therefore \frac{PM}{MQ} = \frac{PX}{XQ}$  ..... (I) theorem of angle bisector.

And

 $\frac{PM}{MR} = \frac{PY}{YR}$ .....(II) Theorem of angle bisector.

Q. 10. In fig 1.78, bisectors of  $\angle B$  and  $\angle C$  of  $\triangle ABC$  intersect each other in point X. Line AX intersects side BC in point Y. AB = 5, AC = 4, BC = 6 then find  $\frac{AX}{XY}$ .

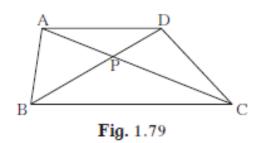


Answer : By Bisector Theorem-

 $\frac{AX}{XY} = \frac{AB}{BY} \dots (1)$   $\Rightarrow And, \frac{AX}{XY} = \frac{AC}{CY} \dots (2)$ Equating (1) & (2), we get- $\frac{AB}{\Rightarrow BY} = \frac{AC}{CY}$   $\Rightarrow \frac{AB}{AC} = \frac{BY}{CY}$   $\Rightarrow \frac{AB + AC}{AC} = \frac{BY + CY}{CY}$   $= \frac{BC}{CY}$   $\Rightarrow \frac{5 + 4}{4} = \frac{6}{CY}$   $\Rightarrow CY = \frac{8}{3}$ 

Now, 
$$\frac{AX}{XY} = \frac{AC}{CY}$$
  
 $\Rightarrow \frac{AX}{XY} = \frac{4}{\frac{8}{2}}$   
 $\Rightarrow \frac{AX}{XY} = \frac{3}{2}$ 

Q. 11. In  $\square$ ABCD, seg AD || seg BC. Diagonal AC and diagonal BD intersect each other in point P. Then show that  $\frac{AP}{PD} = \frac{PC}{BP}$ 



**Answer :** In  $\triangle$  APD and  $\triangle$ CPB

 $\Rightarrow \angle APD \cong \angle CPB$  (opposite angles)

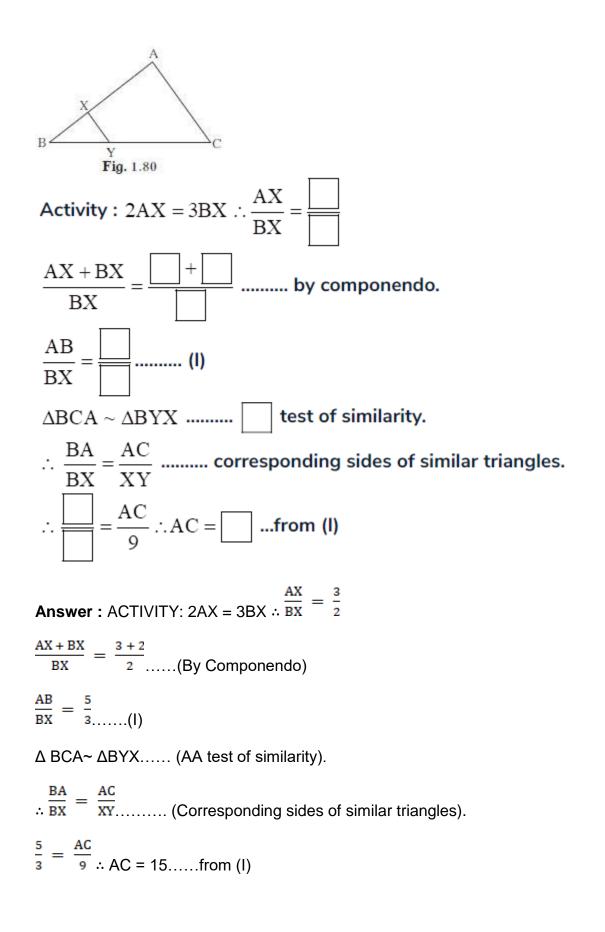
 $\Rightarrow \angle ADP \cong \angle PBC$  (Alternate angles  $\therefore AD||BC$ )

 $\Rightarrow \Delta \text{ APD} \sim \Delta \text{ CPB}$  (By AA Test)

 $\Rightarrow \frac{AP}{PC} = \frac{PD}{BP}$  (corresponding sides are proportional)

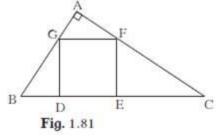
$$\Rightarrow \frac{AP}{PD} = \frac{PC}{BP}$$

Q. 12. In fig 1.80, XY || seg AC. If 2AX = 3BX and XY = 9. Complete the activity to find the value of AC.



Q. 13. In figure 1.81, the vertices of square DEFG are on the sides of  $\triangle ABC$ ,  $\angle A = 90^{\circ}$ . Then prove that  $DE^2 = BD \times EC$ 

(Hint : Show that  $\triangle$ GBD is similar to  $\triangle$ DFE. Use GD = FE = DE.)



**Answer :** Proof: In  $\square$  DEFG is a square

⇒ GF||DE

⇒ GF||BC

Now, In  $\triangle$  AGF and  $\triangle$  DBG

 $\Rightarrow \angle AGF \cong \angle DBG$  (corresponding angles)

 $\Rightarrow \angle \text{GDB} \cong \angle \text{FAG}$  (Both are 90°)

 $\Rightarrow \Delta AGF \sim \Delta DBG \dots(1)$  (AA similarity)

Now, In  $\triangle$  AGF and  $\triangle$  EFC

 $\Rightarrow \angle AFG \cong \angle ECF$  (corresponding angles)

 $\Rightarrow \angle GAF \cong \angle FEC$  (Both are 90°)

 $\Rightarrow \Delta \text{ AGF} \sim \Delta \text{ EFC} \dots (2)$  (AA similarity)

From (1) & (2), we have-

 $\Rightarrow \Delta EFC \sim \Delta DBG$ 

 $\Rightarrow \frac{EF}{BD} = \frac{EC}{DG}$ 

 $\Rightarrow$  EF x DG = BDx EC

Now, : DEFG is a square

 $\Rightarrow$  DE = EF = DG

### $\Rightarrow$ DE x DE = BD x EC

 $\Rightarrow DE^2 = BD \times EC$