# Practice Set 2.1

Q. 1. Identify, with reason, which of the following are Pythagorean triplets.
(i) (3, 5, 4)
(ii) (4, 9, 12)
(iii) (5, 12, 13)
(iv) (24, 70, 74)
(v) (10, 24, 27)
(vi) (11, 60, 61)

**Answer :** In a triangle with sides (a,b,c), the Pythagoran's theorem states that

 $a^2 + b^2 = c^2$ . If this condition is satisfied then (a,b,c)are Pythagorean triplets.

 $1^{st}$  case:  $3^2 + 4^2 = 5^2$ . Thus this a triplet.

 $2^{nd}$  case:  $4^2 + 9^2 \neq 12^2$ 

 $3^{rd}$  case:  $5^2 + 12^2 = 13^2$ . Thus this is a triplet.

 $4^{\text{th}}$  case:  $24^2 + 70^2 = 74^2$ . Thus this is a triplet.

5<sup>th</sup> case:  $10^2 + 24^2 \neq 27^2$ 

 $6^{\text{th}}$  case:  $11^2 + 60^2 = 61^2$ . Thus this is a triplet.

Q. 2. In figure 2.17,  $\angle$ MNP = 90°, seg NQ  $\perp$  seg MP, MQ = 9, QP = 4, find NQ.



**Answer :** In  $\triangle$ MNP,  $\angle$  MNP = 90<sup>0</sup>,

 $MN^2 + NP^2 = MP^2$ 

$$\Rightarrow MN^{2} + NP^{2} = (MQ + QP)^{2}$$
  

$$\Rightarrow MN^{2} + NP^{2} = (13)^{2}$$
  

$$\Rightarrow MN^{2} + NP^{2} = 169 \dots (1)$$
  
In  $\Delta MQN, \ \Delta MQN = 90^{0},$   
 $QN^{2} + MQ^{2} = MN^{2}$   

$$\Rightarrow QN^{2} + 9^{2} = MN^{2}$$
  

$$\Rightarrow QN^{2} + 81 = MN^{2} \dots (2)$$
  
In  $\Delta PQN, \ \Delta PQN = 90^{0},$   
 $QN^{2} + PQ^{2} = PN^{2}$   

$$\Rightarrow QN^{2} + 4^{2} = PN^{2}$$
  

$$\Rightarrow QN^{2} + 4^{2} = PN^{2} \dots (3)$$
  
Now (2) + (3)  

$$\Rightarrow QN^{2} + 81 + QN^{2} + 16 = MN^{2} + PN^{2}$$
  

$$\Rightarrow 2QN^{2} + 97 = 169 [from (1)]$$
  

$$\Rightarrow 2QN^{2} = 72$$
  

$$\Rightarrow QN^{2} = 36$$
  
Thus NQ = 6.

Q. 3. In figure 2.18,  $\angle$ QPR = 90°, seg PM  $\perp$  seg QR and Q – M – R,PM = 10, QM = 8, find QR.



Answer :



- In  $\triangle PMQ$ ,  $\angle PMQ = 90^{\circ}$
- So  $PM^2 + QM^2 = PQ^2$
- $\Rightarrow 10^2 + 8^2 = PQ^2$
- $\Rightarrow$  100 + 64 = PQ<sup>2</sup>
- $PQ^2 = 164 ...(1)$
- In  $\triangle$ PQR,  $\angle$ RPQ = 90<sup>0</sup>
- So  $PQ^2 + PR^2 = QR^2$
- $\Rightarrow$  164 + PR<sup>2</sup> = QR<sup>2</sup>
- $\Rightarrow PR^2 = QR^2 164 \dots (2)$
- In  $\triangle$ PMR,  $\angle$ PMR = 90<sup>0</sup>
- So  $PM^2 + MR^2 = PR^2$

⇒ 
$$10^{2} + (QR - QM)^{2} = QR^{2} - 164$$
  
⇒  $100 + (QR - QM)^{2} = QR^{2} - 164$   
⇒  $100 + QR^{2} - 2.QR.QM + QM^{2} = QR^{2} - 164$   
⇒  $100 - 2.QR.8 + 64 = -164$   
⇒  $16QR = 2 \times 164$   
⇒  $QR = 20.5$ 

Thus QR = 20.5

# Q. 4. See figure 2.19. Find RP and PS using the information given in $\Delta$ PSR.



Ans. RP = 12, PS =  $6\sqrt{3}$ 

Answer : In  $\triangle PSR$ ,  $\angle PSR = 90^{\circ}$ So  $PS^{2} + SR^{2} = RP^{2}$  $\Rightarrow 6^{2} + (RP \cos(30^{\circ}))^{2} = RP^{2}$  $\Rightarrow 6^{2} + RP^{2} \times \frac{3}{4} = RP^{2}$  $\Rightarrow 6^{2} = \frac{RP^{2}}{4}$  $\Rightarrow RP^{2} = 4 \times 36$ Thus RP = 12. PS = RP cos(30^{\circ})  $\Rightarrow PS = 12 \times \frac{\sqrt{3}}{2}$ PS =  $6\sqrt{3}$ . Q. 5. For finding AB and BC with the help of information given in figure 2.20, complete following activity.



**Answer :** In  $\triangle ABC$ ,  $\angle ABC = 90^{\circ}$ 

So 
$$AB^2 + BC^2 = AC^2$$
  
 $\Rightarrow 2AB^2 = 5$   
 $\Rightarrow AB^2 = \frac{5}{2}$   
 $\Rightarrow AB = \sqrt{\frac{5}{2}} = X(Say)$   
 $AB = BC = \sqrt{\frac{5}{2}}$   
 $\angle BAC = 45^0$  Since  $AB = BC$   
Now  $\sqrt{\frac{5}{2}} = X\sqrt{5}$ 

$$X = \frac{1}{\sqrt{2}}$$
  
Similarly,  $X2\sqrt{2} = \sqrt{\frac{5}{2}}$   
$$X = \frac{1}{\sqrt{2}}$$
  
Similarly,  $X\sqrt{8} = \sqrt{\frac{5}{2}}$ 

$$X = \frac{1}{\sqrt{2}}$$

# Q. 6. Find the side and perimeter of a square whose diagonal is 10 cm.

**Answer :** In a square of side say a cm, any diagonal divide the square into two right triangles of equal dimensions.



Thus 
$$a^2 + a^2 = 10^2$$

 $\Rightarrow 2a^2 = 100$ 

 $\Rightarrow a^2 = 50$ 

$$a = 5\sqrt{2}$$
 cm

Perimeter = 4a

$$= 4 \times 5 \sqrt{2}$$
$$= 20 \sqrt{2}$$

Perimeter of square =  $20\sqrt{2}$  cm

Q. 7. In figure 2.21,  $\angle$ DFE = 90°, FG  $\perp$  ED, If GD = 8, FG = 12, find (1) EG (2) FD and (3) EF



Fig. 2.21

**Answer :** In  $\triangle$ DGF,  $\angle$ DGF = 90°

 $FD^2 = DG^2 + GF^2$  $\Rightarrow$  FD<sup>2</sup> = 64 + 144  $\Rightarrow FD^2 = 208$  $FD = 4\sqrt{13}$ In  $\triangle DEF$ ,  $\angle DFE = 90^{\circ}$  $\mathsf{E}\mathsf{D}^2 = \mathsf{D}\mathsf{F}^2 + \mathsf{E}\mathsf{F}^2$  $\Rightarrow (EG + 8)^2 = 208 + EF^2 \dots (1)$ In  $\triangle$ EGF,  $\angle$ FGE = 90<sup>0</sup>  $EF^2 = EG^2 + GF^2$  $\Rightarrow (EG + 8)^2 - 208 = EG^2 + 144$  $\Rightarrow$  EG<sup>2</sup> + 2.EG.8 + 64 - 208 = EG<sup>2</sup> + 144 (As we know (a+b)<sup>2</sup> = a<sup>2</sup>+b<sup>2</sup>+2ab EG = 18 From (1)  $\Rightarrow$  (EG + 8)2 = 208 + EF<sup>2</sup>  $EF = 6\sqrt{13}$ .

# Q. 8. Find the diagonal of a rectangle whose length is 35 cm and breadth is 12 cm.

**Answer** : The diagonal =  $\sqrt{[length^2 + breadth^2]}$ 

$$= \sqrt{(35^2 + 12^2)}$$
  
=  $\sqrt{(1225 + 144)}$   
=  $\sqrt{1369}$ 

Thus the diagonal is 37 cm.





Answer :  $\ln \triangle PRQ, \angle PRQ = 90^{\circ}$   $PQ^{2} = PR^{2} + QR^{2} - - - 1$   $\ln \triangle PRM, \angle PRM = 90^{\circ}$   $PM^{2} = PR^{2} + MR^{2}$   $\Rightarrow PM^{2} = PR^{2} + \frac{QR}{2}^{2}$  [M is midpoint]  $\Rightarrow 4(PM^{2} - PR^{2}) = QR^{2} - - 2$ 1 And 2 implies  $PQ^{2} = PR^{2} + 4(PM^{2} - PR^{2})$  $\Rightarrow PQ^{2} = 4PM^{2} - 3PR^{2}$  PROVED.

Q. 10. Walls of two buildings on either side of a street are parallel to each other. A ladder 5.8 m long is placed on the street such that its top just reaches the window of a building at the height of 4 m. On turning the ladder over to the other side of the street, its top touches the window of the other building at a height 4.2 m. Find the width of the street.

**Answer :** Let us consider a distance x m on the street from one building and a distance y m from the other one.

Now according to question,

In the 1<sup>st</sup> case,

 $5.8^2 = 4^2 + x^2$ 

 $\Rightarrow x^2 = 17.64$ 

 $\Rightarrow$  x = 4.2

Similarly for the second building,

 $5.8^{2} = 4.2^{2} + y^{2}$   $\Rightarrow y^{2} = 16$   $\Rightarrow y = 4$ Total width = x + y = 4 + 4.2

= 8.2

Thus the total width is 8.2m.

# Practice Set 2.2

Q. 1. In  $\Delta$ PQR, point S is the midpoint of side QR. If PQ = 11, PR = 17, PS = 13, find QR.

Answer :



Given PS = 13, PQ = 11, PR = 17

# By Apollonius's Theorem,

$$PS^{2} = \frac{PQ^{2} + PR^{2}}{2} - \frac{QR^{2}}{4}$$
$$\Rightarrow 169 = \frac{121 + 289}{2} - \frac{QR^{2}}{4}$$
$$\Rightarrow \frac{QR^{2}}{4} = 36$$
$$\Rightarrow QR^{2} = 144$$
$$QR = 12$$

Q. 2. In  $\triangle ABC$ , AB = 10, AC = 7, BC = 9 then find the length of the median drawn from point C to side AB

Answer : The figure is given below:



According to Pythagoras theorem,

 $Median2 = \frac{AC^2 + BC^2}{2} - \frac{AB^2}{4}$  $\Rightarrow Median2 = \frac{49 + 81}{2} - \frac{100}{4}$  $\Rightarrow Median2 = 40$  $Median = 2\sqrt{10}$ 

Thus the median is  $2\sqrt{10}$ 

Q. 3. In the figure 2.28 seg PS is the median of  $\Delta$ PQR and PT  $\perp$  QR. Prove that,

(1) 
$$PR^2 = PS^2 + QR \times ST + \left(\frac{QR}{2}\right)^2$$
  
(2)  $PQ^2 = PS^2 - QR \times ST + \left(\frac{QR}{2}\right)^2$ 



Answer : According to the question,

 $QS = SR = \frac{QR}{2}, \angle T = 90^{\circ}$ Now in  $\triangle$ PTR,  $\angle$ PTR = 90<sup>0</sup>  $PT^2 + TR^2 = PR^2$  $\Rightarrow PR^2 = PT^2 + (ST + \frac{QR}{2})^2$  $\Rightarrow \mathsf{PR}^2 = \mathsf{PT}^2 + (\mathsf{ST} + \frac{\mathsf{QR}}{2})^2$  $\Rightarrow PR^2 = PT^2 + ST^2 + 2.ST. \frac{QR}{2} + \frac{QR^2}{4} - - - 1$ Similarly in  $\triangle PTS$  $PS^2 = PT^2 + ST^2 - - - 2$ 1 and 2 implies,  $PR^{2} = PS^{2} - ST^{2} + ST^{2} + 2.ST. \frac{QR}{2} + \frac{QR^{2}}{4}$  $\Rightarrow \mathsf{PR}^2 = \mathsf{PS}^2 + \mathsf{ST}.\mathsf{QR} + \frac{\mathsf{QR}^2}{4}$ PROVED. Now in  $\triangle PTQ$ ,  $\angle PTQ = 90^{\circ}$  $PT^2 + TQ^2 = PQ^2$ 

$$\Rightarrow PR^{2} = PT^{2} + (ST + \frac{QR}{2})^{2}$$

$$\Rightarrow PR^{2} = PT^{2} + (\frac{QR}{2} - ST)^{2}$$

$$\Rightarrow PR^{2} = PT^{2} + ST^{2} - 2. ST. \frac{QR}{2} + \frac{QR^{2}}{4} \dots 1$$
Similarly in  $\Delta PTS$ 

$$PS^{2} = PT^{2} + ST^{2} \dots 2$$
1 and 2 implies,
$$PR^{2} = PS^{2} - ST^{2} + ST^{2} - 2.ST. \frac{QR}{2} + \frac{QR^{2}}{4}$$

$$\Rightarrow PR^{2} = PS^{2} - ST.QR + \frac{QR^{2}}{4}$$

PROVED.

Q. 4. In  $\triangle ABC$ , point M is the mid point of side BC.

If,  $AB^2 + AC^2 = 290 \text{ cm}^2$ , AM = 8 cm, find BC.



Answer : Given  $AB^2 + AC^2 = 290 \text{ cm}^2$ , AM = 8 cm, BM = MC

According to formula,

$$AM^{2} = \frac{AB^{2} + AC^{2}}{2} - \frac{BC^{2}}{4}$$
$$\Rightarrow 64 = \frac{290}{2} - \frac{BC^{2}}{4}$$

$$\Rightarrow 64 - \frac{290}{2} = -\frac{BC^2}{4}$$
$$\Rightarrow BC^2 = 324$$
$$BC = 18.$$
Thus BC = 18 cm.

Q. 5. In figure 2.30, point T is in the interior of rectangle PQRS, Prove that,  $TS^2 + TQ^2 = TP^2 + TR^2$ (As shown in the figure, draw seg AB || side SR and A – T – B)



Answer : From figure,

- In  $\triangle PAT$ ,  $\angle PAT = 90^{\circ}$
- $TP^2 = AT^2 + PA^2 \dots 1$
- In  $\triangle AST$ ,  $\angle SAT = 90^{\circ}$
- $\mathsf{T}\mathsf{S}^2=\mathsf{A}\mathsf{T}^2+\mathsf{S}\mathsf{A}^2\ldots 2$
- In  $\triangle QBT$ ,  $\angle QBT = 90^{\circ}$
- $TQ^2 = BT^2 + QB^2 \dots 3$
- In  $\triangle$ BTR,  $\angle$ RBT = 90<sup>0</sup>
- $TR^2 = BT^2 + BR^2 ...4$
- $TS^2 + TQ^2 = AT^2 + SA^2 + BT^2 + QB^2$  [Adding 2 and 3]
- $\Rightarrow TS^2 + TQ^2 = AT^2 + PA^2 + BT^2 + BR^2 [SA = BR, QB = AP]$
- $\Rightarrow$  TS<sup>2</sup> + TQ<sup>2</sup> = TP<sup>2</sup> + TR<sup>2</sup> [From 1 and 4]

PROVED.

# Problem Set 2

# Q. 1. A. Some questions and their alternative answers are given. Select the correct alternative.

Out of the following which is the Pythagorean triplet? A. (1, 5, 10)

B. (3, 4, 5) C. (2, 2, 2) D. (5, 5, 2)

Answer : A Pythagorean triplet consists of three positive integers (I, b, h) such that

 $l^2 + b^2 = h^2$ 

And (3, 4, 5) is a Pythagorean triplet as,

 $5^2 = 3^2 + 4^2$ 

Q. 1. B. Some questions and their alternative answers are given. Select the correct alternative.

In a right-angled triangle, if sum of the squares of the sides making right angle is 169 then what is the length of the hypotenuse? A. 15

B. 13 C. 5 D. 12

Answer : Given,

Sum of the squares of the sides making right angle = 169

 $\Rightarrow$  (base)<sup>2</sup> + (perpendicular)<sup>2</sup> = 169

But we know, By Pythagoras's theorem

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

 $\Rightarrow$  (Hypotenuse)<sup>2</sup> = 169

 $\Rightarrow$  Hypotenuse = 13 units.

Q. 1. C. Some questions and their alternative answers are given. Select the correct alternative.

Out of the dates given below which date constitutes a Pythagorean triplet? A. 15/08/17

B. 16/08/16 C. 3/5/17 D. 4/9/15

Answer : A Pythagorean triplet consists of three positive integers (I, b, h) such that

 $l^2 + b^2 = h^2$ 

And 15/08/17 is a Pythagorean triplet as,

 $15^2 + 8^2 = 17^2$ 

i.e. 225 + 64 = 289

Q. 1. D. Some questions and their alternative answers are given. Select the correct alternative.

If a, b, c are sides of a triangle and  $a^2 + b^2 = c^2$ , name the type of triangle. A. Obtuse angled triangle

B. Acute angled triangleC. Right angled triangleD. Equilateral triangle

Answer : As, the sides of right-angled triangles satisfies the Pythagoras theorem, i.e.

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

Q. 1. E. Some questions and their alternative answers are given. Select the correct alternative.

Find perimeter of a square if its diagonal is 10 2 cm. A. 10 cm B.  $40\sqrt{2}$  cm C. 20 cm D. 40 cm

Answer : We know that,

Diagonal of a square =  $\sqrt{2}$  a

Where 'a' is the side of the triangle.

 $\Rightarrow \sqrt{2} a = 10\sqrt{2}$ 

 $\Rightarrow$  a = 10 cm

Also, we know

Perimeter of square = 4a

Where 'a' is the side of the triangle

 $\therefore$  Perimeter of given square = 4(10) = 40 cm

Q. 1. F. Some questions and their alternative answers are given. Select the correct alternative.

Altitude on the hypotenuse of a right angled triangle divides it in two parts of lengths 4 cm and 9 cm. Find the length of the altitude.

A. 9 cm B. 4 cm C. 6 cm D.  $2\sqrt{6}$  cm

Answer :



Let ABC be a right-angled triangle, at B, and BP be the altitude on hypotenuse that divides it in two parts such that,

AP = 4 cm

PC = 9 cm

As, ABC, ABP and CBP are right-angled triangles, therefore they all satisfy Pythagoras theorem i.e.

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ ∴ In ∆ABC  $AB^2 + BC^2 = AC^2$  $\Rightarrow AB^2 + BC^2 = (AP + CP)^2$  $\Rightarrow AB^{2} + BC^{2} = (4 + 9)^{2} = 13^{2}$  $\Rightarrow AB^2 + BC^2 = 169[1]$ ∴ In ∆ABP  $AP^2 + BP^2 = AB^2$  $AP^2 + 4^2 = AB^2$  [2]  $\therefore$  In  $\triangle CBP$  $CP^2 + BP^2 = BC^2$  $\Rightarrow$  9<sup>2</sup> + BP<sup>2</sup> = BC<sup>2</sup> [3] Adding [2] and [3], we get  $AP^{2} + 4^{2} + 9^{2} + BP^{2} = AB^{2} + BC^{2}$  $\Rightarrow$  2AP<sup>2</sup> + 16 + 81 = 169 [From 1]  $\Rightarrow$  2AP<sup>2</sup> = 72  $\Rightarrow AP^2 = 36$  $\Rightarrow AP = 6 cm$ 

Hence, length of Altitude is 6 cm.

Q. 1. G. Some questions and their alternative answers are given. Select the correct alternative.

Height and base of a right angled triangle are 24 cm and 18 cm find the length of its hypotenuse

A. 24 cm B. 30 cm C. 15 cm D. 18 cm

Answer : By Pythagoras theorem

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

Given,

Base = 18 cm

Perpendicular = Height = 24 cm

 $\Rightarrow$  Hypotenuse<sup>2</sup> = 24<sup>2</sup> + 18<sup>2</sup>

 $\Rightarrow$  Hypotenuse<sup>2</sup> = 576 + 324

 $\Rightarrow$  Hypotenuse<sup>2</sup> = 900

 $\Rightarrow$  Hypotenuse = 30 cm

Q. 1. H. Some questions and their alternative answers are given. Select the correct alternative.

In D ABC, AB =  $6\sqrt{3}$  cm, AC = 12 cm, BC = 6 cm. Find measure of  $\angle A$ . A. 30°

B. 60° C. 90° D. 45°

Answer : As,

 $(6\sqrt{3})^2 + 6^2 = 12^2$ 

 $\Rightarrow AB^2 + BC^2 = AC^2$ 

i.e. sides of the triangle ABC satisfy the Pythagoras theorem

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

: ABC is a right-angled triangle with hypotenuse as AC

Now,

$$BC = \frac{1}{2}AC$$

By converse of 30°-60°-90° triangle theorem i.e.

In a right-angled triangle, if one side is half of the hypotenuse then the angle

Opposite to that side is 30°.

∠A = 30°

# Q. 2. A. Solve the following examples.

Find the height of an equilateral triangle having side 2a.

Answer :



Let ABC be an equilateral triangle,

Let AP be a perpendicular on side BC from A.

To find : Height of triangle = AP

As, ABC is an equilateral triangle we have

AB = BC = CA = 2a

Also, we know that Perpendicular from a vertex to corresponding side in an equilateral triangle bisects the side

$$\Rightarrow$$
 BP = CP =  $\frac{1}{2}$ BC = 'a'

Now, In  $\triangle ABP$ , By Pythagoras theorem

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

 $\Rightarrow AB^2 = BP^2 + AP^2$ 

$$\Rightarrow$$
 (2a)<sup>2</sup> = a<sup>2</sup> + AP<sup>2</sup>

$$\Rightarrow AP^2 = 4a^2 - a^2$$

 $\Rightarrow AP^2 = 3a^2$ 

 $\Rightarrow$  AP = a $\sqrt{3}$ 

#### Q. 2. B. Solve the following examples.

#### Do sides 7 cm , 24 cm, 25 cm form a right angled triangle ? Give reason.

Answer : Yes,

Because

 $7^2 + 24^2 = 25^2$  [i.e. 49 + 576 = 625]

As, sides satisfy the Pythagoras theorem, i.e.

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

They do form a right-angled triangle.

#### Q. 2. C. Solve the following examples.

Find the length a diagonal of a rectangle having sides 11 cm and 60cm.

Answer :



Let ABCD be a rectangle, with

AB = CD = 60 cm

BC = DA = 11 cm

And AC be a diagonal.

As, ∠A = 90°

ADC is a right-angled triangle, By Pythagoras Theorem i.e.

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

$$AC^2 = (CD)^2 + (DA)^2$$

 $\Rightarrow AC^2 = 60^2 + 11^2$ 

 $\Rightarrow AC^2 = 3600 + 121$ 

- $\Rightarrow AC^2 = 3721$
- $\Rightarrow$  AC = 61 cm

# Q. 2. D. Solve the following examples.

Find the length of the hypotenuse of a right angled triangle if remaining sides are 9 cm and 12 cm.

**Answer :** In a right-angled triangle

By Pythagoras theorem

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

Given,

Other sides are 9 cm and 12 cm

- $\Rightarrow$  Hypotenuse<sup>2</sup> = 9<sup>2</sup> + 12<sup>2</sup>
- $\Rightarrow$  Hypotenuse<sup>2</sup> = 81 + 144
- $\Rightarrow$  Hypotenuse<sup>2</sup> = 225

⇒ Hypotenuse = 15 cm

# Q. 2. E. Solve the following examples.

# A side of an isosceles right angled triangle is x. Find its hypotenuse.

Answer : In a right-angled triangle

By Pythagoras theorem

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

As, the triangle is isosceles

Base = Perpendicular = x

[Hypotenuse can't be equal to any of the sides, because hypotenuse is the greatest side in a right-angled triangle and it must be greater than other two sides]

 $\Rightarrow$  (Hypotenuse)<sup>2</sup> = x<sup>2</sup> + x<sup>2</sup>

- $\Rightarrow$  (Hypotenuse)<sup>2</sup> = 2x<sup>2</sup>
- $\Rightarrow$  Hypotenuse =  $x\sqrt{2}$

# Q. 2. F. Solve the following examples.

In  $\triangle$  PQR; PQ =  $\sqrt{8}$ , QR =  $\sqrt{5}$ , PR =  $\sqrt{3}$  Is  $\triangle$  PQR a right angled triangle? If yes, which angle is of 90°?

Answer : As,

 $(\sqrt{5})^2 + (\sqrt{3})^2 = (\sqrt{8})^2$ 

$$\Rightarrow$$
 QR<sup>2</sup> + PR<sup>2</sup> = PQ<sup>2</sup>

i.e. sides of the triangle ABC satisfy the Pythagoras theorem

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

: PQR is a right-angled triangle at R [As hypotenuse is PQ].

Q. 3. In  $\triangle RAT$ ,  $\angle S = 90^{\circ}$ ,  $\angle T = 30^{\circ}$ , RT = 12 cm then find RS and ST.

Answer :



As,  $\angle S = 90^{\circ}$ , and  $\angle T = 30^{\circ}$  and RT = 12 cm is given.

Clearly, RTS is a 30°-60°-90° triangle.

We know, Property of 30°-60°-90° triangle i.e.

If acute angles of a right angled-triangle are 30° and 60°, then the side opposite

30° angle is half of the hypotenuse and the side opposite to 60° angle is  $\frac{\sqrt{3}}{2}$  times of hypotenuse.

$$\Rightarrow RS = \frac{1}{2} \times RT = \frac{1}{2}(12) = 6 \text{ cm}$$

And

$$ST = \frac{\sqrt{3}}{2} \times RT = \frac{\sqrt{3}}{2} \times 12 = 6\sqrt{3} \text{ cm}$$

Q. 4. Find the diagonal of a rectangle whose length is 16 cm and area is 192 sq.cm.

Answer : Given,

Length of rectangle, I = 16 cm

Breadth of rectangle = b

Area of rectangle = length  $\times$  breadth

⇒ 192 = 16b

 $\Rightarrow$  b = 12 cm

Also, we know that

Length of diagonal =  $\sqrt{(l^2 + b^2)}$ 

Where, I = Iength and b = breadth

 $\Rightarrow$  Length of diagonal =  $\sqrt{(16^2 + 12^2)}$ 

 $=\sqrt{(256 + 144)} = 20 \text{ cm}$ 

Q. 5. Find the length of the side and perimeter of an equilateral triangle whose height is  $\sqrt{3}$  cm.

Answer :



Let ABC be an equilateral triangle,

Let AP be a perpendicular on side BC from A.

To find : Height of triangle = AP

As, ABC is an equilateral triangle we have

AB = BC = CA = 'a'

Also, we know that Perpendicular from a vertex to corresponding side in an equilateral triangle bisects the side

$$\Rightarrow BP = CP = \frac{1}{2}BC = \frac{1}{2}a$$

Now, In  $\triangle ABP$ , By Pythagoras theorem

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

$$\Rightarrow AB^2 = BP^2 + AP^2$$

$$\Rightarrow a^{2} = \left(\frac{1}{2}a\right)^{2} + AP^{2}$$
$$\Rightarrow AP^{2} = a^{2} - \frac{1}{4}a^{2} = \frac{3}{4}a^{2}$$
$$\Rightarrow AP = \frac{\sqrt{3}}{2}a$$

Given,

Height =  $\sqrt{3}$ 

$$\Rightarrow \frac{\sqrt{3}}{2}a = \sqrt{3}$$

 $\Rightarrow$  a = 2 cm

Also, Perimeter of equilateral triangle = 3a

Where 'a' depicts side of equilateral triangle.

 $\therefore$  Perimeter = 3(2) = 6 cm

Q. 6. In  $\triangle$ ABC seg AP is a median. If BC = 18, AB<sup>2</sup> + AC<sup>2</sup> = 260 Find AP.

Answer :



We know, By Apollonius theorem

In ΔABC,

If P is the midpoint of side BC, then  $AB^2 + AC^2 = 2AP^2 + 2BP^2$ 

Given that, AP is median i.e. P is the mid-point of BC

$$BP = CP = \frac{1}{2}BC = 9$$
  
And BC = 18 cm  
And AB<sup>2</sup> + AC<sup>2</sup> = 260  
 $\Rightarrow 260 = 2AP^2 + 2(9)^2$   
 $\Rightarrow 260 = 2AP^2 + 162$   
 $\Rightarrow 98 = 2AP^2$   
 $\Rightarrow AP^2 = 49$   
 $\Rightarrow AP = 7$  units

Q. 7.  $\triangle$  ABC is an equilateral triangle. Point P is on base BC such that  $PC = -\frac{1}{3}BC$ . if AB = 6 cm find AP.





ABC be an equilateral triangle,

Point P is on base BC, such that

$$PC = \frac{1}{3}BC$$

Let us construct AM perpendicular on side BC from A.

As, ABC is an equilateral triangle we have

AB = BC = CA = 6 cm

Also, we know that Perpendicular from a vertex to corresponding side in an equilateral triangle bisects the side

$$\Rightarrow$$
 BM = CM =  $\frac{1}{2}$ BC = 3 cm

Now, In  $\triangle$ ACM, By Pythagoras theorem

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

$$\Rightarrow CA^2 = CM^2 + AM^2$$

$$\Rightarrow (6)^2 = (3)^2 + AM^2$$

 $\Rightarrow$  36 = 9 + AM<sup>2</sup>

$$\Rightarrow AM^{2} = 27 [1]$$
As,  

$$PC = \frac{1}{3}BC$$

$$CM = \frac{1}{2}BC$$
We have,  

$$CM - PC = PM$$

$$\Rightarrow PM = \frac{1}{2}BC - \frac{1}{3}BC$$

$$\Rightarrow PM = \frac{1}{6}BC = \frac{1}{6}(6)$$

$$\Rightarrow PM = 1 \text{ cm}$$
Now, In right angled triangle AMP, By Pythagoras theorem  

$$(AP)^{2} = (AM)^{2} + (PM)^{2}$$

$$\Rightarrow (AP)^{2} = 27 + 1^{2}$$

 $\Rightarrow AP^2 = 28$ 

 $\Rightarrow$  AP = 2 $\sqrt{7}$  cm

Q. 8. From the information given in the figure 2.31, prove that PM = PN =  $\sqrt{3} \times a$ 



Answer : In  $\Delta PQS$  and  $\Delta PSR$ , By Pythagoras theorem

i.e. 
$$(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$$
  
 $PQ^2 = QS^2 + PS^2 [1]$   
 $PR^2 = SR^2 + PS^2 [2]$   
Subtracting [2] from [1],  
 $PQ^2 - PR^2 = QS^2 - SR^2$   
 $\Rightarrow a^2 - a^2 = QS^2 - SR^2$   
 $\Rightarrow QS^2 = SR^2$   
 $\Rightarrow QS = SR$   
 $\Rightarrow QS = SR$   
 $\Rightarrow QS = SR = \frac{1}{2}QR = \frac{a}{2}$   
Also,  
 $MS = MQ + QS$   
 $\Rightarrow MS = a + \frac{a}{2} = \frac{3a}{2}$   
And  
 $SN = SR + RN$   
 $\Rightarrow SN = \frac{a}{2} + a = \frac{3a}{2}$   
In  $\Delta PSM$  and  $\Delta PSN$ , By Pythagoras theorem  
 $PM^2 = PS^2 + MS^2$ 

$$\Rightarrow PN^{2} = PS^{2} + \left(\frac{3a}{2}\right)^{2} [4]$$

 $PN^2 = PS^2 + SN^2$ 

$$\Rightarrow PN^2 = PS^2 + \left(\frac{3a}{2}\right)^2 [4]$$

From [3] and [4]

 $PM^2 = PN^2$ 

 $\Rightarrow$  PM = PN

Hence Proved.

Q. 9. Prove that the sum of the squares of the diagonals of a parallelogram is equal to the sum of the squares of its sides.

**Answer :** Let ABCD be a parallelogram, with AB = CD;  $AB \parallel CD$  and BC = AD;  $BC \parallel AD$ .

Construct AE  $\perp$  CD and extend CD to F such that, BF  $\perp$  CF.



In  $\Delta AED$  and  $\Delta BCF$ 

AE = BF [Distance between two parallel lines i.e. AB and CD]

AD = BC [opposite sides of a parallelogram are equal]

 $\angle AED = \angle BFC [Both 90^{\circ}]$ 

 $\Delta AED \cong \Delta BCF$  [By Right Angle - Hypotenuse - Side Criteria]

 $\Rightarrow$  DE = CF [Corresponding sides of congruent triangles are equal] [1]

In  $\triangle$ BFD, By Pythagoras theorem i.e.

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

 $BD^2 = DF^2 + BF^2$  $\Rightarrow$  BD<sup>2</sup> = (CD + CF)<sup>2</sup> + BF<sup>2</sup> [2] In  $\triangle AEC$ , By Pythagoras theorem  $AC^2 = AE^2 + CE^2$  $\Rightarrow AC^2 = AE^2 + (CD - AE)^2$  $\Rightarrow$  AC<sup>2</sup> = BF<sup>2</sup> + (CD - CF)<sup>2</sup> [As, AE = BF and CF = AE] [2] In  $\triangle$ BCF, By Pythagoras theorem,  $BC^2 = BF^2 + CF^2$  $BF^2 = BC^2 - CF^2$  [3] Adding [2] and [3]  $BD^{2} + AC^{2} = 2BF^{2} + (CD + CF)^{2} + (CD - CF)^{2}$  $\Rightarrow BD^{2} + AC^{2} = 2BC^{2} - 2CF^{2} + CD^{2} + CF^{2} + 2CD.CF + CD^{2} + CF^{2} - 2CD.CF$  $\Rightarrow$  BD<sup>2</sup> + AC<sup>2</sup> = 2BC<sup>2</sup> + 2CD<sup>2</sup>  $\Rightarrow$  BD<sup>2</sup> + AC<sup>2</sup> = BC<sup>2</sup> + BC<sup>2</sup> + CD<sup>2</sup> + CD<sup>2</sup>  $\Rightarrow$  BD<sup>2</sup> + AC<sup>2</sup> = AB<sup>2</sup> + BC<sup>2</sup> + CD<sup>2</sup> + AD<sup>2</sup> [since BC = AD and AB = CD]

Hence, the sum of the squares of the diagonals of a parallelogram is equal to the sum of the squares of its sides.

Q. 10. Pranali and Prasad started walking to the East and to the North respectively, from the same point and at the same speed. After 2 hours distance between them was  $15\sqrt{2}$  km. Find their speed per hour.

Answer :



Let their speed be 'x' km/h

We know, distance = speed × time

In two hours,

Distance travelled by both = '2x' km

Let their starting point be 'O', and Pranali and Prasad reach the point A in the East and point B in the north direction respectively.

Clearly, AOB is a right-angled triangle, So By Pythagoras theorem

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

 $(AB)^2 = (OA)^2 + (OB)^2$ 

As, AB = distance between them =  $15\sqrt{2}$  km

And OA = OB = distance travelled by each = 2x

 $\Rightarrow (15\sqrt{2})^2 = (2x)^2 + (2x)^2$ 

- $\Rightarrow 450 = 8x^2$
- $\Rightarrow x^2 = 56.25$

 $\Rightarrow$  x = 7.5 km/h

Q. 11. In  $\triangle ABC$ ,  $\angle BAC = 90^{\circ}$ , seg BL and seg CM are medians of  $\triangle ABC$ . Then prove that : 4(BL<sup>2</sup> + CM<sup>2</sup>) = 5 BC<sup>2</sup>



#### Answer :

We know, By Apollonius theorem

In  $\triangle$ ABC, if L is the midpoint of side AC, then AB<sup>2</sup> + BC<sup>2</sup> = 2BL<sup>2</sup> + 2AL<sup>2</sup>

Given that, BL is median i.e. L is the mid-point of CA

$$CL = AL = \frac{1}{2}AC$$
  

$$\Rightarrow AB^{2} + BC^{2} = 2BL^{2} + 2AL^{2}$$
  

$$\Rightarrow AB^{2} + BC^{2} = 2BL^{2} + 2\left(\frac{AC}{2}\right)^{2}$$
  

$$\Rightarrow AB^{2} + BC^{2} = 2BL^{2} + \frac{AC^{2}}{2}$$
[1]

Also, if M is the midpoint of side AB, then  $AC^2 + BC^2 = 2CM^2 + 2BM^2$ 

Given that, CM is median i.e. M is the mid-point of BA

$$AM = BM = \frac{1}{2}AB$$
  

$$\Rightarrow AC^{2} + BC^{2} = 2CM^{2} + 2BM^{2}$$
  

$$\Rightarrow AC^{2} + BC^{2} = 2CM^{2} + 2\left(\frac{AB}{2}\right)^{2}$$
  

$$\Rightarrow AC^{2} + BC^{2} = 2CM^{2} + \frac{AB^{2}}{2}$$
[2]

Also, In  $\triangle$ ABC, By Pythagoras theorem i.e.

$$(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$$

$$\Rightarrow$$
 BC<sup>2</sup> = AC<sup>2</sup> + AB<sup>2</sup> [3]

Adding [1] and [2]

$$\Rightarrow AB^{2} + BC^{2} + AC^{2} + BC^{2} = 2BL^{2} + \frac{AC^{2}}{2} + 2CM^{2} + \frac{AB^{2}}{2}$$
$$\Rightarrow \frac{AB^{2}}{2} + \frac{AC^{2}}{2} + 2BC^{2} = 2BL^{2} + 2CM^{2}$$
$$\Rightarrow AB^{2} + AC^{2} + 4BC^{2} = 4(BL^{2} + CM^{2})$$
$$\Rightarrow BC^{2} + 4BC^{2} = 4(BL^{2} + CM^{2}) [From 3]$$
$$\Rightarrow 5BC^{2} = 4(BL^{2} + CM^{2})$$

Hence Proved.

# Q. 12. Sum of the squares of adjacent sides of a parallelogram is 130 sq.cm and length of one of its diagonals is14 cm. Find the length of the other diagonal.

**Answer :** Let ABCD be a parallelogram, with AB = CD;  $AB \parallel CD$  and BC = AD;  $BC \parallel AD$ .

Construct AE  $\perp$  CD and extend CD to F such that, BF  $\perp$  CF.



Given: sum of squares of adjacent side = 130

 $\Rightarrow$  CD<sup>2</sup> + BC<sup>2</sup> = 130 and

Length of one diagonal = 14 cm [let it be AC]

To Find: length of the other diagonal, BD

In  $\triangle AED$  and  $\triangle BCF$ 

AE = BF [Distance between two parallel lines i.e. AB and CD]

AD = BC [opposite sides of a parallelogram are equal]

 $\angle AED = \angle BFC [Both 90^\circ]$ 

 $\Delta AED \cong \Delta BCF$  [By Right Angle - Hypotenuse - Side Criteria]

 $\Rightarrow$  DE = CF [Corresponding sides of congruent triangles are equal] [1]

In  $\triangle$ BFD, By Pythagoras theorem i.e.

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

 $\mathsf{B}\mathsf{D}^2 = \mathsf{D}\mathsf{F}^2 + \mathsf{B}\mathsf{F}^2$ 

 $\Rightarrow \mathsf{B}\mathsf{D}^2 = (\mathsf{C}\mathsf{D} + \mathsf{C}\mathsf{F})^2 + \mathsf{B}\mathsf{F}^2 \, [2]$ 

In  $\triangle AEC$ , By Pythagoras theorem

$$AC^2 = AE^2 + CE^2$$

 $\Rightarrow AC^2 = AE^2 + (CD - AE)^2$ 

$$\Rightarrow$$
 AC<sup>2</sup> = BF<sup>2</sup> + (CD - CF)<sup>2</sup> [As, AE = BF and CF = AE] [2]

In ΔBCF, By Pythagoras theorem,

 $BC^{2} = BF^{2} + CF^{2}$   $BF^{2} = BC^{2} - CF^{2} [3]$ Adding [2] and [3]  $BD^{2} + AC^{2} = 2BF^{2} + (CD + CF)^{2} + (CD - CF)^{2}$   $\Rightarrow BD^{2} + AC^{2} = 2BC^{2} - 2CF^{2} + CD^{2} + CF^{2} + 2CD.CF + CD^{2} + CF^{2} - 2CD.CF$   $\Rightarrow BD^{2} + AC^{2} = 2BC^{2} + 2CD^{2}$   $\Rightarrow BD^{2} + 14^{2} = 2(130)$   $\Rightarrow BD^{2} + 196 = 260 [Using given data]$   $\Rightarrow BD^{2} = 64$   $\Rightarrow BD = 8 cm$ 

Hence, length of other diagonal is 8 cm.

Q. 13. In  $\triangle$  ABC, seg AD  $\perp$  seg BC DB = 3CD. Prove that : 2AB<sup>2</sup> = 2AC<sup>2</sup> + BC<sup>2</sup>



Answer : Given,

DB = 3CD

Also,

BC = CD + DB = CD + 3CD

 $\Rightarrow$  BC = 4CD [1]

```
As, AD \perp BC, By Pythagoras theorem i.e.
```

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

 $\ln\Delta\,ACD$ 

 $AC^2 = AD^2 + CD^2$  [2]

In **ΔABD** 

 $\mathsf{A}\mathsf{B}^2=\mathsf{A}\mathsf{D}^2+\mathsf{D}\mathsf{B}^2$ 

 $\Rightarrow AB^2 = AD^2 + (3CD)^2$ 

 $\Rightarrow AB^2 = AD^2 + 9CD^2$  [3]

Subtracting [2] from [3]

 $\Rightarrow AB^2 - AC^2 = 9CD^2 - CD^2$ 

 $\Rightarrow AB^2 = AC^2 + 8CD^2$ 

 $\Rightarrow$  2AB<sup>2</sup> = 2AC<sup>2</sup> + 16CD<sup>2</sup>

 $\Rightarrow$  2AB<sup>2</sup> = 2AC<sup>2</sup> + (4CD)<sup>2</sup>

 $\Rightarrow$  2AB<sup>2</sup> = 2AC<sup>2</sup> + BC<sup>2</sup> [From 1]

Hence Proved.

Q. 14. In an isosceles triangle, length of the congruent sides is 13 cm and its base is 10 cm. Find the distance between the vertex opposite the base and the centroid.

Answer :



Let ABC be an isosceles triangle, In which AB = AC = 13 cm

And BC = 10 cm

Let AM be median on BC such that

$$BM = CM = \frac{1}{2}BC = 5 \ cm$$

Let P be centroid on median BC

To Find : AP [Distance between vertex opposite the base and centroid]

We know, By Apollonius theorem

In  $\triangle$ ABC, if M is the midpoint of side BC, then AB<sup>2</sup> + AC<sup>2</sup> = 2AM<sup>2</sup> + 2BM<sup>2</sup>

Putting values, we get

$$(13)^2 + (13)^2 = 2AM^2 + 2(5)^2$$

- $\Rightarrow 169 + 169 = 2AM^2 + 50$
- $\Rightarrow 2AM^2 = 288$
- $\Rightarrow AM^2 = 144$
- $\Rightarrow$  AM = 12 cm

Let P be the centroid

As, Centroid divides median in a ratio 2 : 1

 $\Rightarrow AP = 2PM$ 

Now, AM = AP + PM

$$\Rightarrow AM = AP + \frac{AP}{2} = \frac{3}{2}AP$$
$$\Rightarrow AP = \frac{2}{3}AM = \frac{2}{3}(12) = 8 \ cm$$

Q. 15. In a trapezium ABCD, seg AB || seg DC seg BD  $\perp$  seg AD, seg AC  $\perp$  seg BC, If AD = 15, BC = 15 and AB = 25. Find  $A(\Box ABCD)$ 



Answer :



Construct DE  $\perp$  AB and CF  $\perp$  AB

In  $\triangle$ ADB, as BD  $\perp$  AD, By Pythagoras theorem i.e.

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

 $(AB)^2 = (AD)^2 + (BD)^2$ 

 $\Rightarrow 25^2 = 15^2 + BD^2$ 

 $\Rightarrow BD^2 = 625 - 225 = 400$ 

 $\Rightarrow$  BD = 20 cm

Similarly,

AC = 20 cm

Now, In  $\triangle AED$  and  $\triangle ABD$ 

 $\angle AED = \angle ADB$  [Both 90°]

 $\angle DAE = \angle DAE$  [Common]

ΔAED ~ ΔABD [By Angle-Angle Criteria]

 $\Rightarrow \frac{DE}{BD} = \frac{AD}{AB} = \frac{AE}{AD}$  [Property of similar triangles]

As AD = 15 cm, BD = 20 cm and AB = 25 cm

 $\Rightarrow \frac{DE}{20} = \frac{15}{25}$   $\Rightarrow DE = 12 \text{ cm}$ Also,  $\frac{DE}{BD} = \frac{AE}{AD}$   $\Rightarrow \frac{12}{20} = \frac{AE}{15}$   $\Rightarrow AE = 9 \text{ cm}$ Similarly, BF = 9 cm

Now,

DC = EF [By construction]

DC = AB - DE - AE

DC = 25 - 9 - 9 = 7 cm

Also, we know

Area of trapezium =  $\frac{1}{2} \times ($ Sum of Parallel Sides $) \times$  Height

$$= \frac{1}{2} \times (DC + AB) \times DE$$
$$= \frac{1}{2} \times (7 + 25) \times 12$$

 $= 192 \text{ cm}^2$ 

Q. 16. In the figure 2.35,  $\triangle$  P20QR is an equilateral triangle. Point S is on seg QR such that  $QS = \frac{1}{3}QR$ .





Answer : As, PQR is an equilateral triangle,

Point S is on base QR, such that

$$QS = \frac{1}{3}QR$$

PT is perpendicular on side QR from P.

As, PQR is an equilateral triangle we have

$$PQ = QR = PR[1]$$

Also, we know that Perpendicular from a vertex to corresponding side in an equilateral triangle bisects the side

$$\Rightarrow QT = TR = \frac{1}{2}QR = \frac{1}{2}PQ$$

Now, In  $\Delta PTQ$ , By Pythagoras theorem

 $(Hypotenuse)^2 = (base)^2 + (Perpendicular)^2$ 

$$\Rightarrow PQ^{2} = PT^{2} + QT^{2}$$

$$\Rightarrow PQ^{2} = PT^{2} + \left(\frac{1}{2}PQ\right)^{2}$$

$$\Rightarrow PQ^{2} = PT^{2} + \frac{1}{4}PQ^{2}$$

$$\Rightarrow PT^{2} = \frac{3}{4}PQ^{2}$$
[2]

As,

$$QS = \frac{1}{3}QR$$
$$QT = \frac{1}{2}QR$$

We have,

QT - QS = ST  
⇒ ST = 
$$\frac{1}{2}$$
QR -  $\frac{1}{3}$ QR  
⇒ ST =  $\frac{1}{6}$ QR =  $\frac{1}{6}$ PQ

Now, In right angled triangle PST, By Pythagoras theorem

$$(PS)^{2} = (ST)^{2} + (PT)^{2}$$

$$\Rightarrow PS^{2} = \left(\frac{1}{6}PQ\right)^{2} + \frac{3}{4}PQ^{2} \text{ [From 2]}$$

$$\Rightarrow PS^{2} = \frac{PQ^{2}}{36} + \frac{3}{4}PQ^{2}$$

$$\Rightarrow PS^{2} = \frac{PQ^{2} + 27PQ^{2}}{36}$$

$$\Rightarrow 36 PS^{2} = 28 PQ^{2}$$

$$\Rightarrow 9 PS^{2} = 7 PQ^{2}$$
Hence Proved.

# Q. 17. Seg PM is a median of $\triangle$ PQR. If PQ = 40, PR = 42 and PM = 29, find QR.

Answer :



We know, By Apollonius theorem

In  $\Delta$ PQR, if M is the midpoint of side QR, then PQ<sup>2</sup> + PR<sup>2</sup> = 2PM<sup>2</sup> + 2QM<sup>2</sup>

Given that, PM is median i.e. M is the mid-point of QR

$$QM = MR = \frac{1}{2}QR$$

And PQ = 40, PR = 42, PM = 29

Putting values,

- $\Rightarrow (40)^{2} + (42)^{2} = 2(29)^{2} + 2(QM)^{2}$  $\Rightarrow 1600 + 1764 = 1682 + 2QM^{2}$  $\Rightarrow QM^{2} = 1682$  $\Rightarrow QM = 29$
- $\Rightarrow$  QR = 2(29) = 58

Q. 18. Seg AM is a median of  $\triangle$  ABC. If AB = 22, AC = 34, BC = 24, find AM

Answer :





In  $\triangle$ ABC, if M is the midpoint of side BC, then AB<sup>2</sup> + AC<sup>2</sup> = 2AM<sup>2</sup> + 2BM<sup>2</sup>

Given that,

AB = 22, AC = 34, BC = 24

AP is median i.e. P is the mid-point of BC

$$\Rightarrow BP = CP = \frac{1}{2}BC = 12$$

Putting values in equation

$$\Rightarrow 22^2 + 34^2 = 2AM^2 + 2(12)^2$$

- $\Rightarrow$  484 + 1156 = 2AM<sup>2</sup> + 288
- $\Rightarrow 1352 = 2AM^2$
- $\Rightarrow AM^2 = 676$
- $\Rightarrow AM = 26$